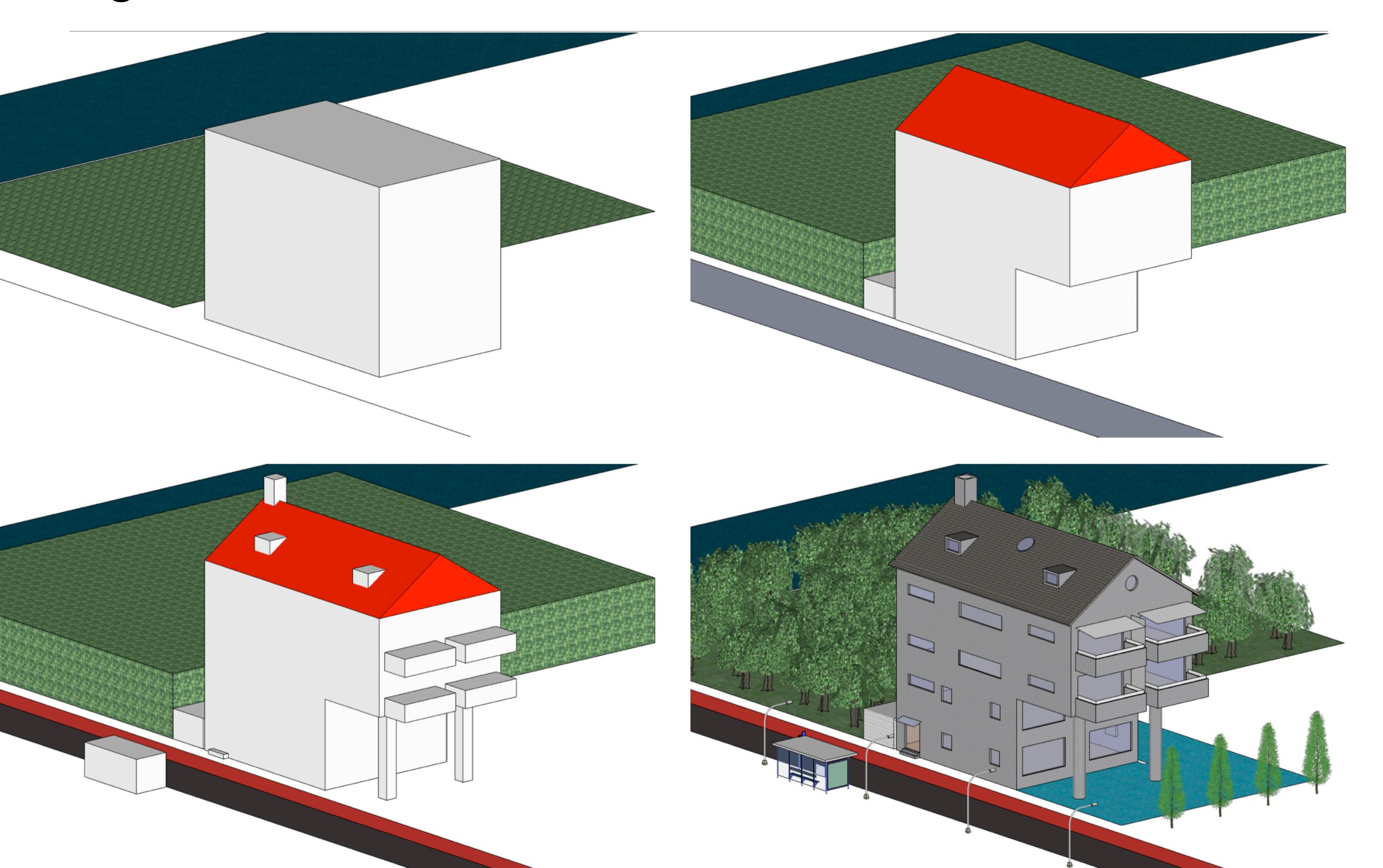
Using extrusion to generate higher-dimensional GIS datasets

Ken Arroyo Ohori Hugo Ledoux

November 6, 2013 ACM SIGSPATIAL GIS 2013

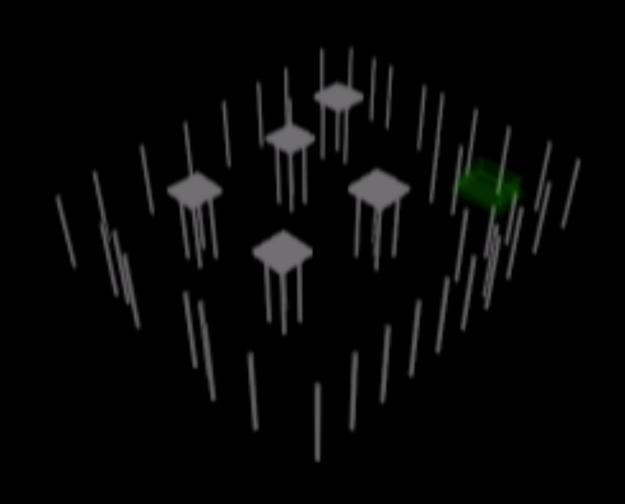


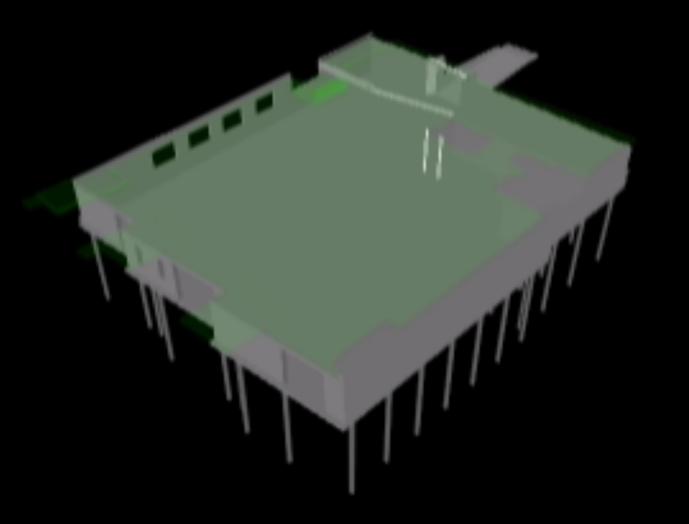
From multiple representation to higher dimensional GIS

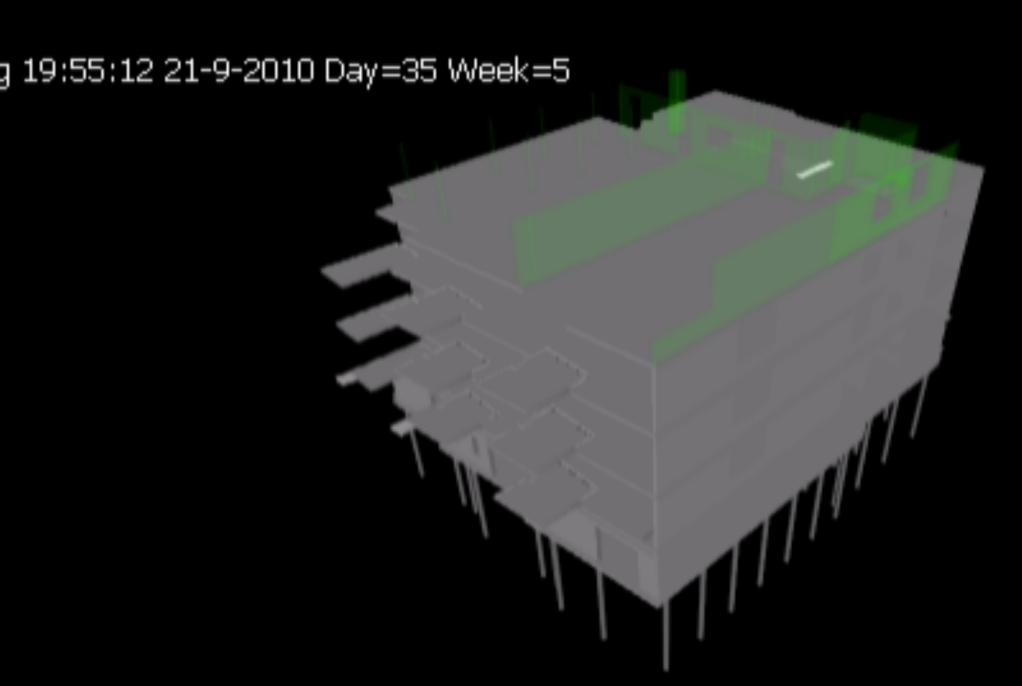


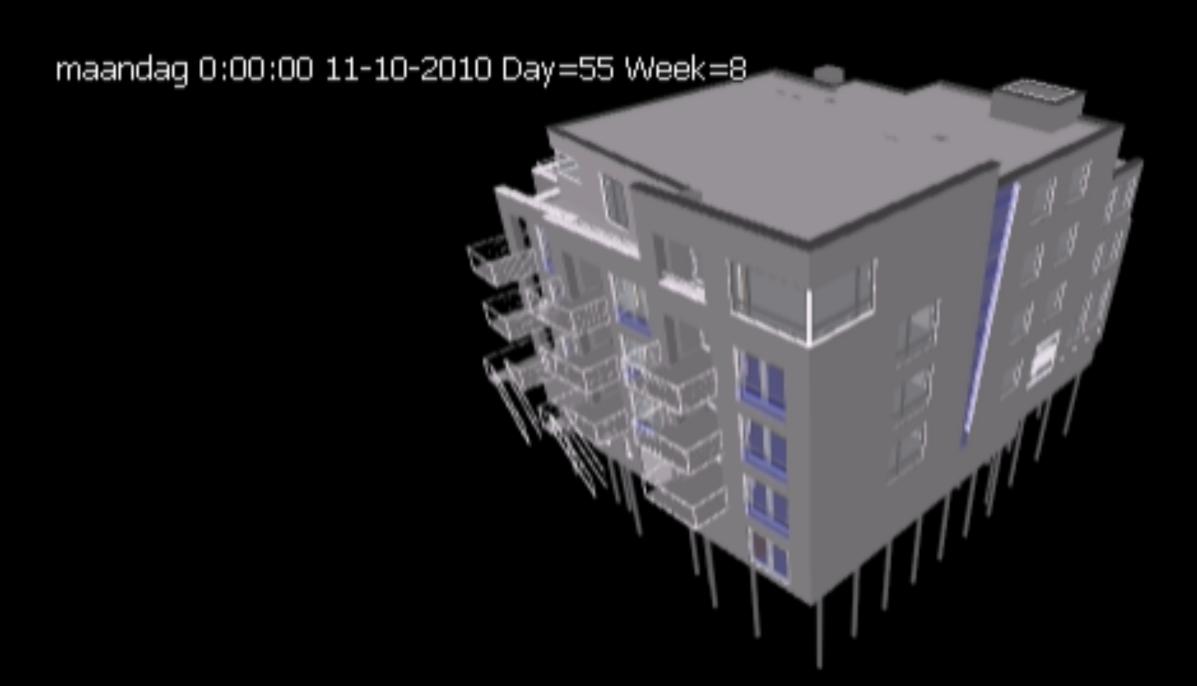
From multiple representation to higher dimensional GIS

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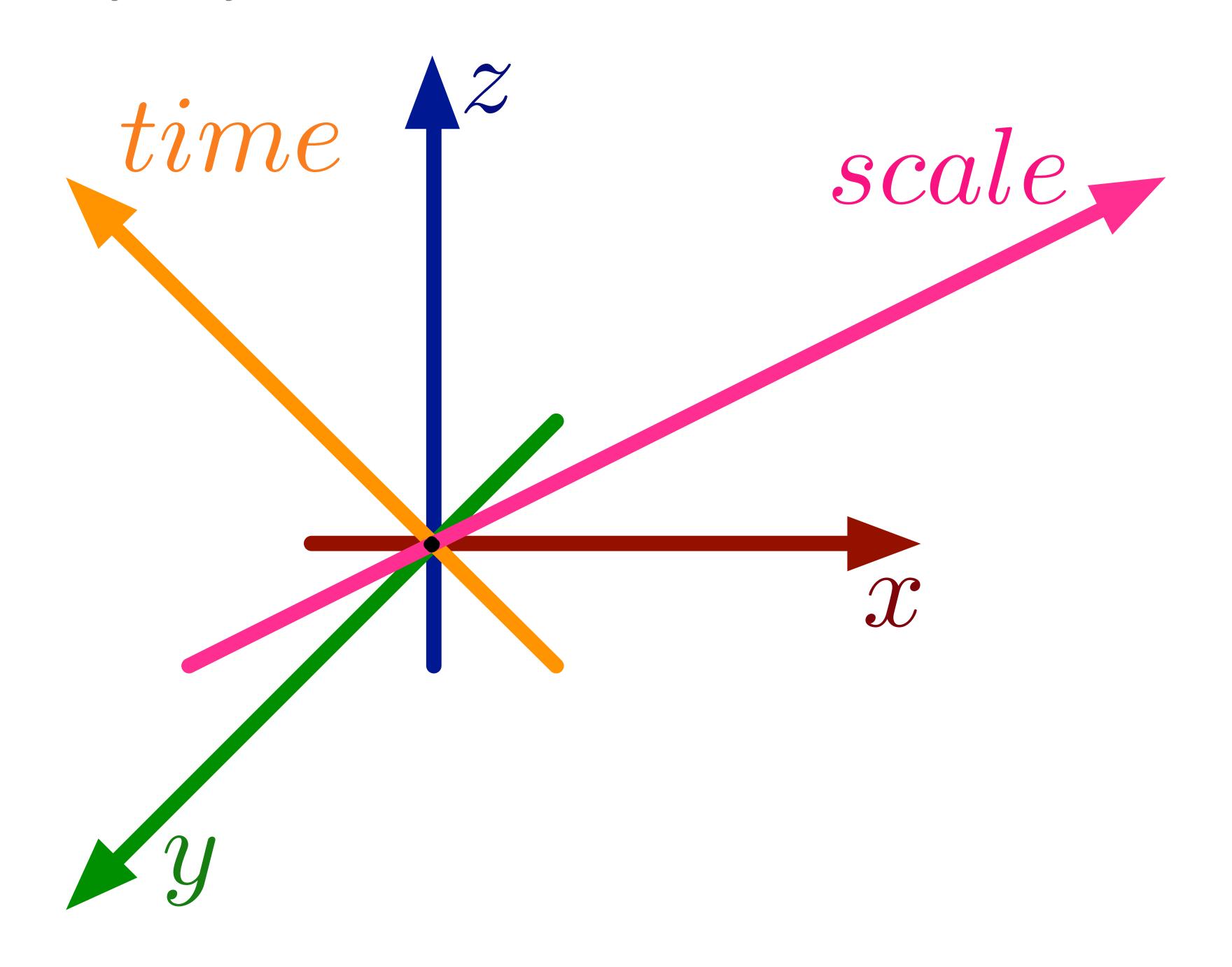






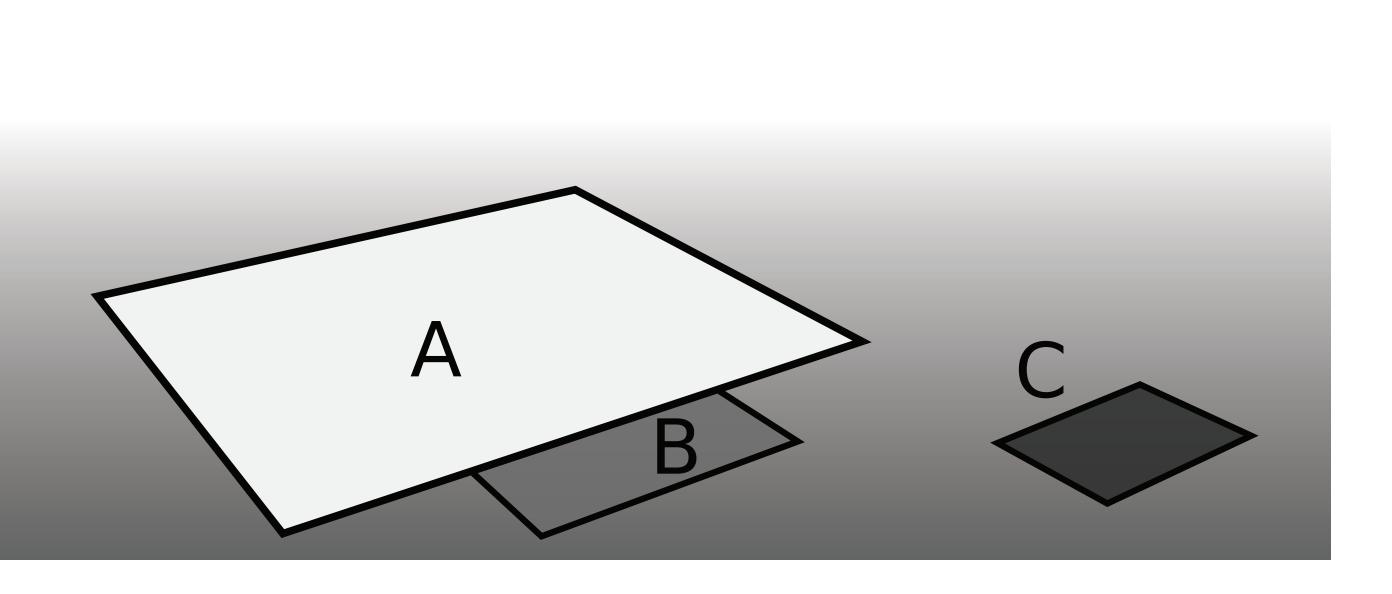
From multiple representation to higher dimensional GIS

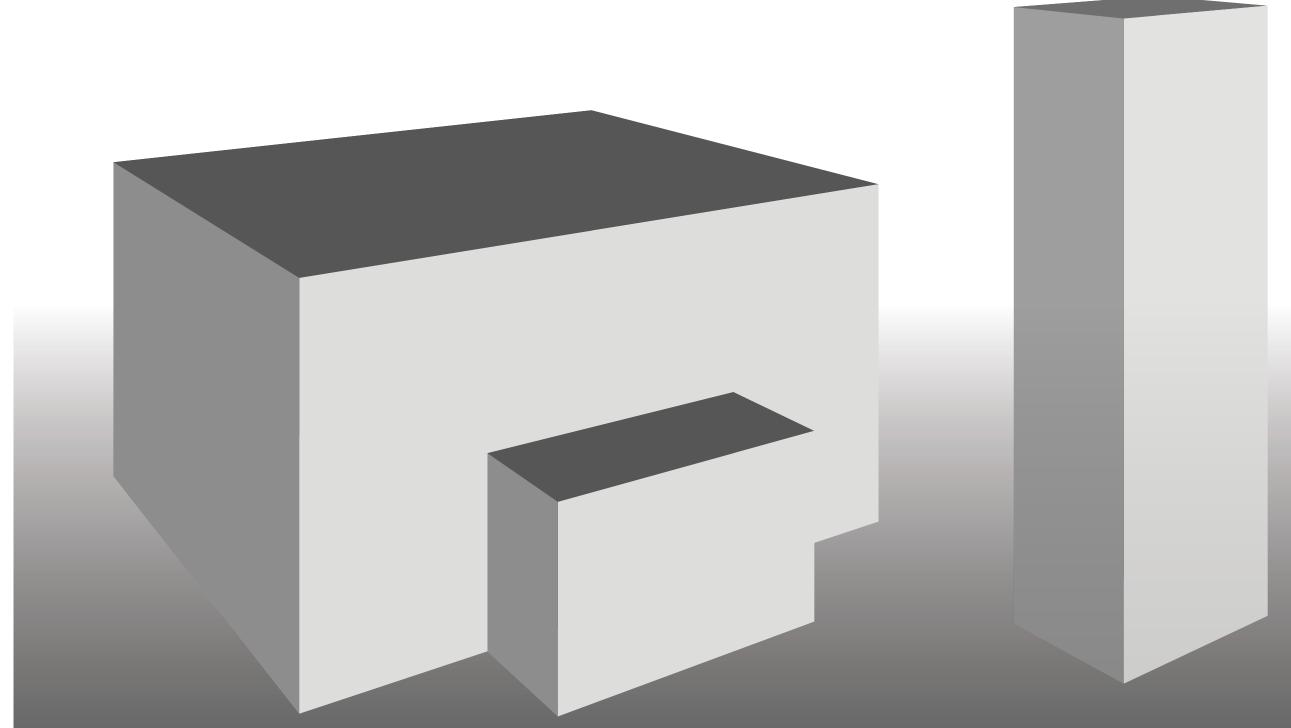
Mathematically easy but tools are needed



2D to 3D extrusion

•2D footprint + height → 3D

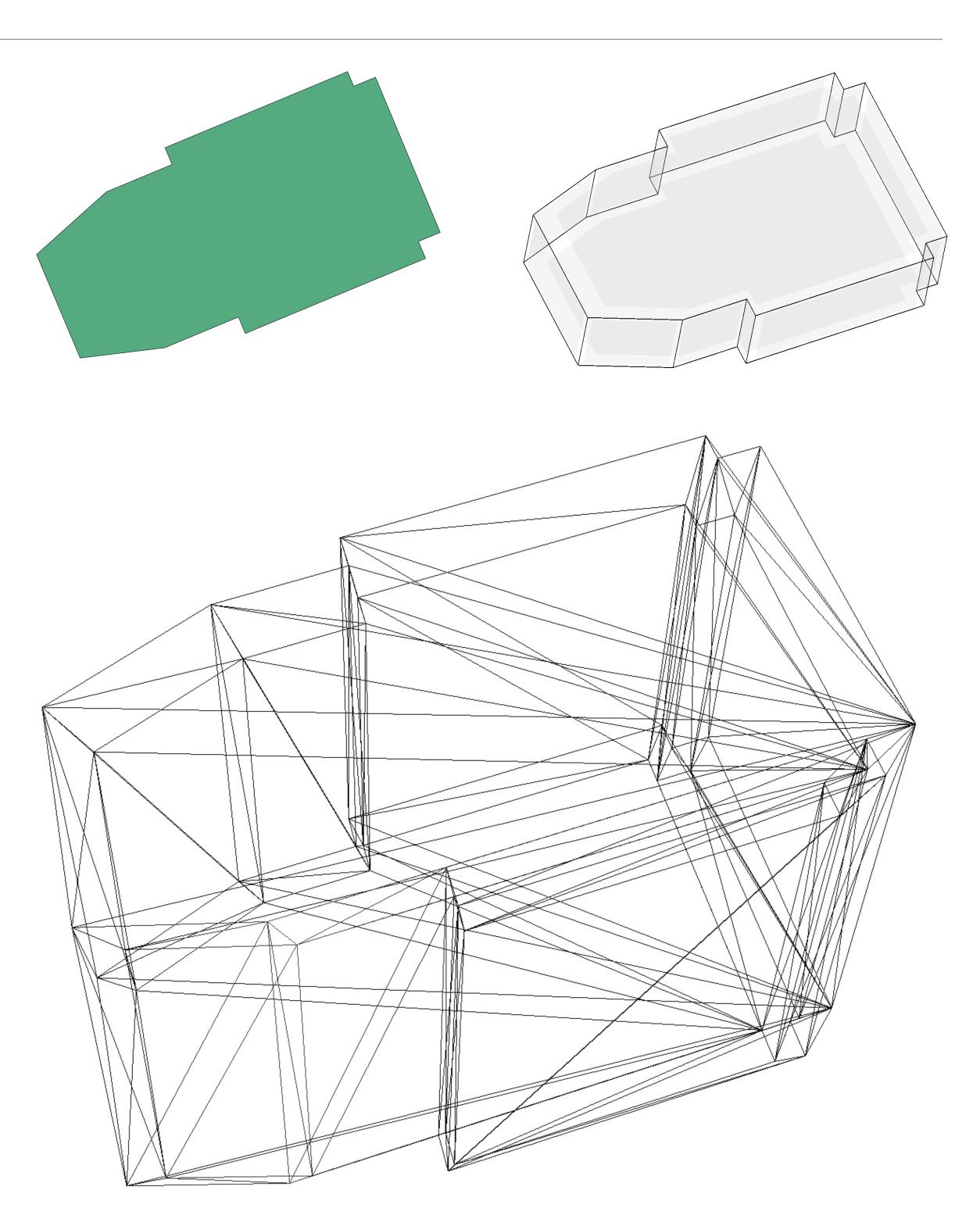




n-D extrusion

•
$$(n-1)$$
-D + range $\rightarrow n$ -D





Thank you!

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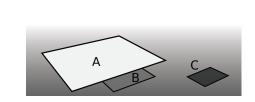


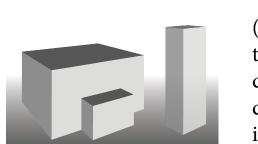
Using extrusion to generate higher-dimensional GIS datasets

Ken Arroyo Ohori* and Hugo Ledoux Delft University of Technology, The Netherlands

TUDelft

1. Introduction





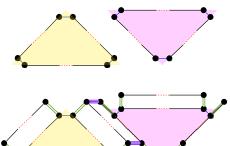
There is a growing interest in the use of higher-dimensional (>4D) digital objects, but their use is hampered by a lack of methods and algorithms.

Akin to 2D to 3D extrusion (left), *n*D extrusion allows us to create an (n+1)dimensional model from an ndimensional one by assigning it a range along the (n+1)-th dimension.

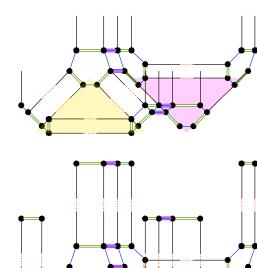
We present here a dimensionindependent extrusion algorithm for linear geometries using generalised maps. It is optimal and straightforward to implement.

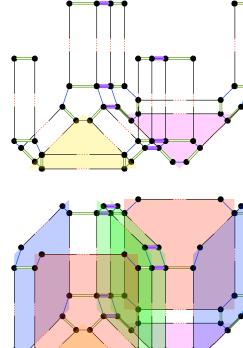
We have implemented it in Python and made experiments in which 2D real-world GIS datasets were extruded to 3D and 4D.

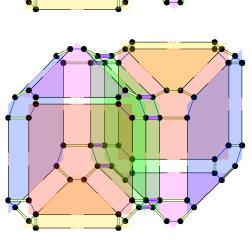
3. Extrusion algorithm



Our extrusion algorithm takes two input arguments: an (n-1)-Gmap, and a given range $[r_{\min}, r_{\max}]$ where these will exist along an nth dimension. Its result is an n-G-map representing a set of prismatic *n*-polytopes.







Algorithm 1: EmbeddingsExtrusion

```
Input :E,[r_{\min},r_{\max}]
Output: E', base, top, ex
foreach e \in E do
     base(e), top(e), ex(e) \leftarrow e
     if e.dimension = 0 then
           Append r_{\min} to base(e)'s coordinates
          Append r_{
m max} to top(e)'s coordinates
     ex(e).dimension \leftarrow ex(e).dimension + 1
     Put base(e), top(e) and ex(e) in E'
```

Algorithm 2: GMAPEXTRUSION

```
Input : G = (D, \alpha_0, \alpha_1, \dots, \alpha_{n-1}), E, E', base, top, ex, e, e'
Output: G' = (D', \alpha'_0, \alpha'_1, \dots, \alpha'_n)
for dim \leftarrow n to 0 do
      GMapLayer(G, G', dim, 1, last, E, E', e, e', base, ex)
for dim \leftarrow 0 to n do
      GMAPLAYER (G, G', dim, 0, last, E, E', e, e', top, ex)
```

Algorithm 3: GMAPLAYER

```
Input : G = (D, \alpha_0, \alpha_1, \dots, \alpha_{n-1}), G' = (D', \alpha'_0, \alpha'_1, \dots, \alpha'_n),
          dim, offset, last, E, E', e, e', el, ex
Output: G' = (D', \alpha'_0, \alpha'_1, \dots, \alpha'_n), last, cur, e'
foreach d \in D do
     cur(d) \leftarrow \text{new dart}
     Put cur(d) in D'
\mathbf{foreach}\ d \in D\ \mathbf{do}
      for inv \leftarrow 0 to dim - 1 do
         | \alpha'_{inv}(cur(d)) \leftarrow cur(\alpha_{inv}(d)) 
      \alpha'_{dim+offset}(cur(d)) \leftarrow last(d)
      \alpha'_{dim+offset}(last(d)) \leftarrow cur(d)
      for inv \leftarrow dim + 2 to n do
           \alpha'_{inv}(cur(d)) \leftarrow cur(\alpha_{inv-1}(d))
      for emb \leftarrow 0 to dim do
            e'_{emb}(cur(d)) \leftarrow el(e_{emb}(d))
      for emb \leftarrow dim + 1 to n do
            e'_{emb}(cur(d)) \leftarrow ex(e_{emb-1}(d))
```

5. Discussion

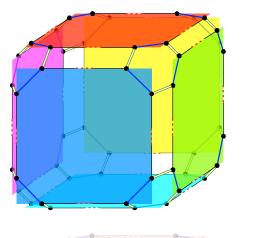
We have shown that it is possible to use our algorithm to extrude (n-1)-dimensional cell complexes represented as G-maps into ndimensional ones. Our algorithm is optimal in time, easy to implement and addresses both the geometry and the topology of the objects.

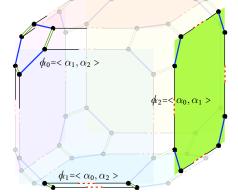
References

Pascal Lienhardt. N-dimensional generalized combinatorial maps and cellular quasi-manifolds. International Journal of Computational Geometry and *Applications*, 4(3):275-324, 1994.

Hugo Ledoux and Martijn Meijers. Topologically consistent 3D city models obtained by extrusion. International Journal of Geographical Information *Science*, 25(4):557-574, 2011.

2. Generalised maps





simple implementation (right) is based on structures per dart and per geometric embedding.

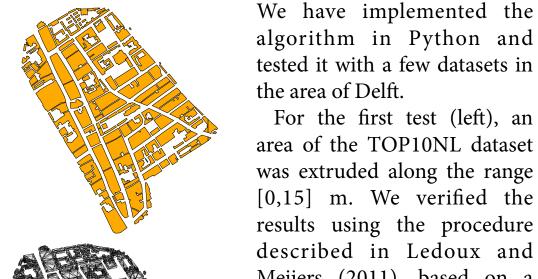
Generalised maps (G-maps) are a topological model in arbitrary dimensions developed by Lienhardt (1994). It is composed of darts and involutions (left). A dart is a combination of a cell of every dimension. Involutions connect darts related along a certain dimension.

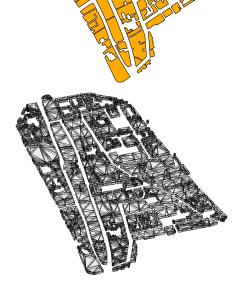
```
Dart *involutions[n+1];
    Embeddings **embeddings[n+1];
struct Embedding {
    Dart *referenceDart;
   Embedding *holes[];
    int dimension;
    float red, green, blue;
```

struct Dart {

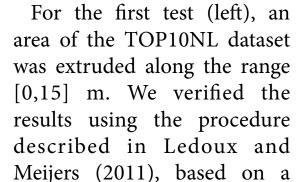
struct PointEmbedding : Embedding { float x, y, z;

4. Experiments

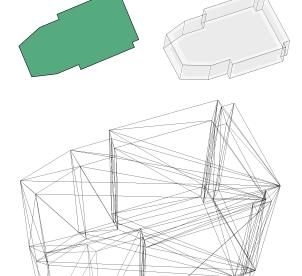




For the second test (right), we used a building footprint from the GBKN dataset. It was extruded along the range [0,25] m, and extruded again along the range [1960,2060] yr for a 4D (3D+time) model.



Meijers (2011), based on a constrained tetrahedralisation of the dataset.



Contact

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