





Lecture Camera Calibration

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Today's Agenda



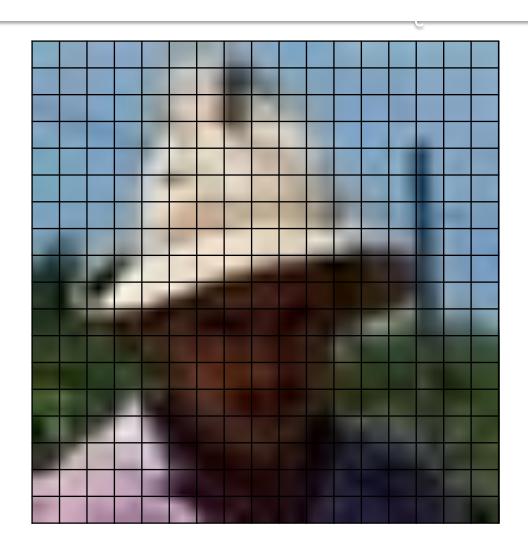
• Review: Camera models



- Camera calibration
- A1: Camera calibration

Images





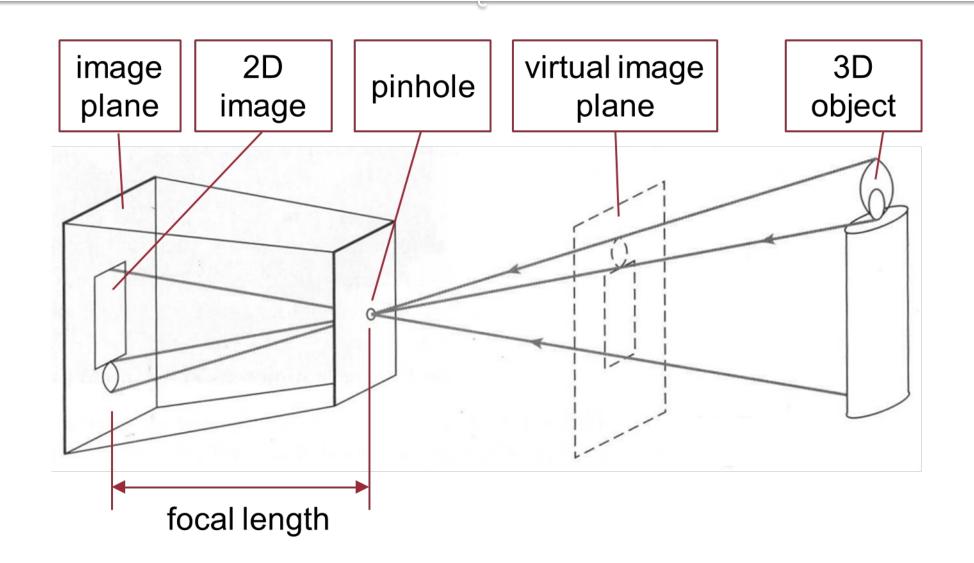
A color image: R, G, B channels

$$f(x,y) = \begin{bmatrix} r(x,y) \\ g(x,y) \\ b(x,y) \end{bmatrix}$$

"vector-valued" function

Pinhole camera model

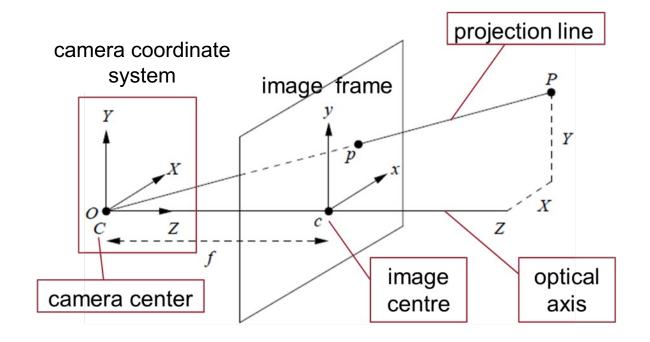




Pinhole camera model



• 3D point $P = (X, Y, Z)^T$ projected to 2D image $p = (x, y)^T$



$$x = f \frac{X}{Z}, \qquad y = f \frac{Y}{Z}$$





• Pinhole camera
$$x = f \frac{X}{Z}$$
, $y = f \frac{Y}{Z}$

- Change of unit: physical measurements -> pixels
 - If k = l, camera sensor's pixels are exactly square

$$x = kf\frac{X}{Z}, \qquad y = lf\frac{Y}{Z}$$



Denote $\alpha = kf$, $\beta = lf$

$$x = \alpha \frac{X}{Z}, \qquad y = \beta \frac{Y}{Z}$$

- x, y: image coordinates (pixels)
- k, l: scale parameters (pixels/mm)
- f: focal length (mm)





• Pinhole camera
$$x = f \frac{X}{Z}$$
, $y = f \frac{Y}{Z}$

- Change of unit: physical measurements -> pixels $x = \alpha \frac{X}{7}$, $y = \beta \frac{Y}{7}$
- Change of coordinate system
 - Image plane coordinates have origin at image center
 - Digital image coordinates have origin at top-left corner

$$x = \alpha \frac{X}{Z} + c_x$$
, $y = \beta \frac{Y}{Z} + c_y$





• Pinhole camera
$$x = f \frac{X}{Z}$$
, $y = f \frac{Y}{Z}$

- Change of unit: physical measurements -> pixels $x = \alpha \frac{X}{Z}$, $y = \beta \frac{Y}{Z}$ Change of coordinate system $x = \alpha \frac{X}{Z} + c_x$, $y = \beta \frac{Y}{Z} + c_y$
- Account for skewness
 - Image frame may not be exactly rectangular due to sensor manufacturing errors

$$\hat{y}$$
 \hat{y}
 \hat{x}

$$x = \alpha \frac{X}{Z} - \alpha \cot \theta \frac{Y}{Z} + c_x, \qquad y = \frac{\beta}{\sin \theta} \frac{Y}{Z} + c_y$$
\text{\theta: skew angle between x- and y-axis}

$$y = \frac{\rho}{\sin \theta} \frac{1}{Z} + c_{y}$$





$$x = \alpha \frac{X}{Z} - \alpha \cot \theta \frac{Y}{Z} + c_x, \qquad y = \frac{\beta}{\sin \theta} \frac{Y}{Z} + c_y$$

Rewrite in matrix-vector product form

$$P = [X, Y, Z]^T$$
, $p = [x, y, 1]^T$

(homogeneous coordinates)

$$\mathbf{p} = K\mathbf{P}, K = \begin{bmatrix} \alpha & -\alpha \cot \theta & c_x \\ 0 & \frac{\beta}{\sin \theta} & c_y \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} f_x & s & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}$$





Camera motion

- World frame may not align with the camera frame
- Camera can move and rotate

$$\mathbf{P}^C = R_W^C \mathbf{P}^W + \mathbf{t}_W^C$$
 World frame

- 1. Coordinates of 3D scene point in camera frame.
- 2. Coordinates of 3D scene point in world frame.
- 3. Rotation matrix of world frame in camera frame.
- 4. Position of world frame's origin in camera frame.

Perspective projection model



The complete transformation

$$\mathbf{p} = M\mathbf{P}$$

$$= K \begin{bmatrix} R & \mathbf{t} \end{bmatrix} \mathbf{P}$$
Internal (intrinsic) parameters

External (extrinsic) parameters

- R: rotation matrix of the world coordinate system defined in the camera coordinate system
- t: the position of world coordinate system's origin in camera coordinate system

(Note: \mathbf{t} is often mistakenly interpreted as the position of the camera position in the world coordinate system) $_{11}$

Today's Agenda



- Review: Camera models
- Camera calibration



• A1: Camera calibration



- Why is camera calibration necessary?
 - Given 3D scene, knowing the precise 3D to 2D projection requires
 - Intrinsic and extrinsic parameters
 - Reconstructing 3D geometry from images also requires these parameters

$$\mathbf{p} = M\mathbf{P}$$

$$= K \begin{bmatrix} R & \mathbf{t} \end{bmatrix} \mathbf{P}$$
Internal (intrinsic) parameters

External (extrinsic) parameters





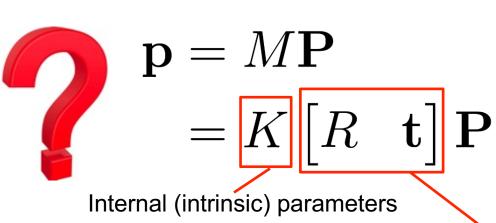
- Why is camera calibration necessary?
- What information do we have?
 - Images only







- Why is camera calibration necessary?
- What information do we have?
- Camera calibration
 - Recovering K
 - Recovering R and t
- How many parameters



External (extrinsic) parameters



- How many parameters to recover?
 - How many intrinsic parameters?

$$K = \begin{bmatrix} f_x & s & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{p} = M\mathbf{P}$$

$$= K \begin{bmatrix} R & \mathbf{t} \end{bmatrix} \mathbf{P}$$
 Internal (intrinsic) parameters



- How many parameters to recover?
 - How many intrinsic parameters?
 - How many extrinsic parameters?

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix}, \ \mathbf{t} = \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

$$\mathbf{p} = M\mathbf{P}$$

$$= K \begin{bmatrix} R & \mathbf{t} \end{bmatrix} \mathbf{P}$$
External (extrinsic) parameters



- How many parameters to recover: 11
 - 5 intrinsic parameters
 - 2 for focal lengths
 - 2 for offset (image center, or principal point)
 - 1 for skewness
 - 6 extrinsic parameters
 - 3 for rotation
 - 3 for translation

$$K = \begin{bmatrix} f_x & s & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}, \quad R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix}, \quad \mathbf{t} = \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$



What information to use?

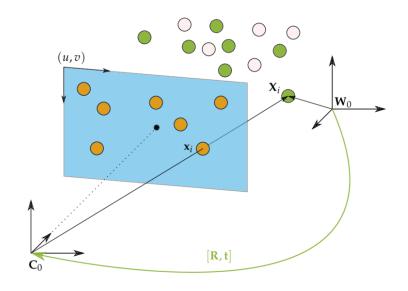






Corresponding 3D-2D point pairs

$$\mathbf{p} = M\mathbf{P}$$
$$= K \begin{bmatrix} R & \mathbf{t} \end{bmatrix} \mathbf{P}$$

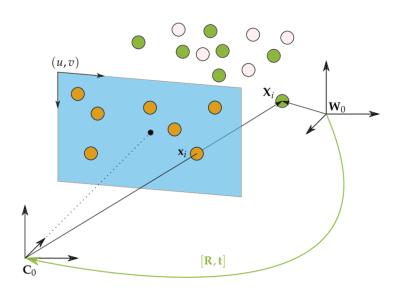




- What information to use?
 - Corresponding 3D-2D point pairs
 - How many pairs do we need?



$$\mathbf{p} = M\mathbf{P}$$
$$= K \begin{bmatrix} R & \mathbf{t} \end{bmatrix} \mathbf{P}$$





- What information to use?
 - Corresponding 3D-2D point pairs
 - How many pairs do we need?
 - How much information does each pair of corresponding point provide?

$$\mathbf{p} = M\mathbf{P} \implies \mathbf{p}_i = \begin{bmatrix} u_i \\ v_i \end{bmatrix} = M\mathbf{P}_i = \begin{bmatrix} \frac{\mathbf{P}_i^T \mathbf{m}_1}{\mathbf{P}_i^T \mathbf{m}_3} \\ \frac{\mathbf{P}_i^T \mathbf{m}_2}{\mathbf{P}_i^T \mathbf{m}_3} \end{bmatrix}$$



- What information to use?
 - Corresponding 3D-2D point pairs
 - How many pairs do we need?
 - Each 3D-2D point pair -> 2 equations
 - 11 unknown -> 6 point correspondence
 - Use more to handle noisy data

$$\mathbf{p} = M\mathbf{P} \implies \mathbf{p}_i = \begin{bmatrix} u_i \\ v_i \end{bmatrix} = M\mathbf{P}_i = \begin{bmatrix} \frac{\mathbf{P}_i^T \mathbf{m}_1}{\mathbf{P}_i^T \mathbf{m}_3} \\ \frac{\mathbf{P}_i^T \mathbf{m}_2}{\mathbf{P}_i^T \mathbf{m}_3} \end{bmatrix} \implies \begin{aligned} \mathbf{P}_i^T \mathbf{m}_1 - u_i(\mathbf{P}_i^T \mathbf{m}_3) &= 0 \\ \mathbf{P}_i^T \mathbf{m}_2 - v_i(\mathbf{P}_i^T \mathbf{m}_3) &= 0 \end{aligned}$$



$$\mathbf{P}_{i}^{T}\mathbf{m}_{1}-u_{i}(\mathbf{P}_{i}^{T}\mathbf{m}_{3})=0$$
 $\mathbf{P}_{i}^{T}\mathbf{m}_{2}-v_{i}(\mathbf{P}_{i}^{T}\mathbf{m}_{3})=0$

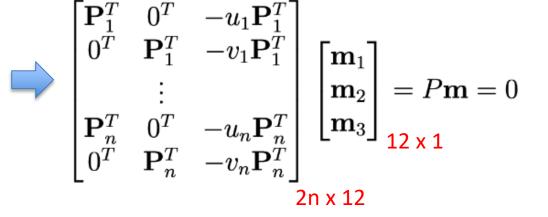
$$\mathbf{P}_{1}^{T}\mathbf{m}_{1}-u_{1}(\mathbf{P}_{1}^{T}\mathbf{m}_{3})=0$$

$$\mathbf{P}_{1}^{T}\mathbf{m}_{2}-v_{1}(\mathbf{P}_{1}^{T}\mathbf{m}_{3})=0$$

$$\vdots$$

$$\mathbf{P}_{n}^{T}\mathbf{m}_{1}-u_{n}(\mathbf{P}_{n}^{T}\mathbf{m}_{3})=0$$

$$\mathbf{P}_{n}^{T}\mathbf{m}_{2}-v_{n}(\mathbf{P}_{n}^{T}\mathbf{m}_{3})=0$$



Constraints from one pair

Equations from n pairs



What is the dimension of the *P* matrix? What is the dimension of **m**?



• The equations $\mathbf{p} = M\mathbf{P}$ $[X,Y,Z]^T \to [u,v]^T$

$$[X,Y,Z]^T \rightarrow [u,v]^T$$



$$su = m_{11}X + m_{12}Y + m_{13}Z + m_{14}$$

$$sv = m_{21}X + m_{22}Y + m_{23}Z + m_{24}$$

$$s = m_{31}X + m_{32}Y + m_{33}Z + m_{34}$$

$$v = \frac{m_{11}X + m_{12}Y + m_{13}Z + m_{14}}{m_{31}X + m_{32}Y + m_{33}Z + m_{34}}$$

$$v = \frac{m_{21}X + m_{22}Y + m_{23}Z + m_{24}}{m_{31}X + m_{32}Y + m_{33}Z + m_{34}}$$

$$u = \frac{m_{11}X + m_{12}Y + m_{13}Z + m_{14}}{m_{31}X + m_{32}Y + m_{33}Z + m_{34}}$$
$$v = \frac{m_{21}X + m_{22}Y + m_{23}Z + m_{24}}{m_{31}X + m_{32}Y + m_{33}Z + m_{34}}$$



The equations

$$u = \frac{m_{11}X + m_{12}Y + m_{13}Z + m_{14}}{m_{31}X + m_{32}Y + m_{33}Z + m_{34}}$$
$$v = \frac{m_{21}X + m_{22}Y + m_{23}Z + m_{24}}{m_{31}X + m_{32}Y + m_{33}Z + m_{34}}$$



$$(m_{31}X + m_{32}Y + m_{33}Z + m_{34}) u = m_{11}X + m_{12}Y + m_{13}Z + m_{14}$$
$$(m_{31}X + m_{32}Y + m_{33}Z + m_{34}) v = m_{21}X + m_{22}Y + m_{23}Z + m_{24}$$



$$m_{11}X + m_{12}Y + m_{13}Z + m_{14} - m_{31}uX - m_{32}uY - m_{33}uZ - m_{34}u = 0$$

$$m_{21}X + m_{22}Y + m_{23}Z + m_{24} - m_{31}vX - m_{32}vY - m_{33}vZ - m_{34}v = 0$$

The equations

For every pair of 3D-2D corresponding points

$$m_{11}X + m_{12}Y + m_{13}Z + m_{14} - m_{31}uX - m_{32}uY - m_{33}uZ - m_{34}u = 0$$

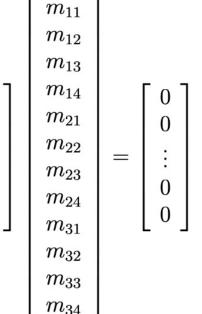
$$m_{21}X + m_{22}Y + m_{23}Z + m_{24} - m_{31}vX - m_{32}vY - m_{33}vZ - m_{34}v = 0$$

Given n pairs of 3D-2D corresponding points

$$egin{bmatrix} m_{11} \\ m_{12} \\ m_{13} \\ m_{14} \\ m_{21} \\ m_{22} \\ m_{23} \\ m_{24} \\ m_{31} \\ m_{32} \\ m_{33} \\ m_{34} \end{bmatrix} = egin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ 0 \end{bmatrix}$$



The equations





Simplified notation

$$\begin{bmatrix} \mathbf{P}_1^T & \mathbf{0}^T & -u_1 \mathbf{P}_1^T \\ \mathbf{0}^T & \mathbf{P}_1^T & -v_1 \mathbf{P}_1^T \\ & \vdots & \\ \mathbf{P}_n^T & \mathbf{0}^T & -u_n \mathbf{P}_n^T \\ \mathbf{0}^T & \mathbf{P}_n^T & -v_n \mathbf{P}_n^T \end{bmatrix} \begin{bmatrix} \mathbf{m}_1 \\ \mathbf{m}_2 \\ \mathbf{m}_3 \end{bmatrix} = P\mathbf{m} = 0$$



- How to solve it?
 - It is a homogeneous linear system
 - It is overdetermined



$$\begin{bmatrix} \mathbf{P}_1^T & \mathbf{0}^T & -u_1 \mathbf{P}_1^T \\ \mathbf{0}^T & \mathbf{P}_1^T & -v_1 \mathbf{P}_1^T \\ & \vdots & \\ \mathbf{P}_n^T & \mathbf{0}^T & -u_n \mathbf{P}_n^T \\ \mathbf{0}^T & \mathbf{P}_n^T & -v_n \mathbf{P}_n^T \end{bmatrix} \begin{bmatrix} \mathbf{m}_1 \\ \mathbf{m}_2 \\ \mathbf{m}_3 \end{bmatrix} = P\mathbf{m} = 0$$



- How to solve it?
 - $-\mathbf{m} = 0$ is always a trivial solution
 - If $\mathbf{m} \neq 0$ is a solution, then any $k * \mathbf{m}$ is also a solution

$$\begin{bmatrix} \mathbf{P}_1^T & 0^T & -u_1 \mathbf{P}_1^T \\ 0^T & \mathbf{P}_1^T & -v_1 \mathbf{P}_1^T \\ & \vdots & \\ \mathbf{P}_n^T & 0^T & -u_n \mathbf{P}_n^T \\ 0^T & \mathbf{P}_n^T & -v_n \mathbf{P}_n^T \end{bmatrix} \begin{bmatrix} \mathbf{m}_1 \\ \mathbf{m}_2 \\ \mathbf{m}_3 \end{bmatrix} = P\mathbf{m} = 0$$



- How to solve it?
 - $-\mathbf{m} = 0$ is always a trivial solution
 - If $\mathbf{m} \neq 0$ is a solution, then any $k * \mathbf{m}$ is also a solution
 - Constrained optimization

$$\begin{bmatrix} \mathbf{P}_1^T & \mathbf{0}^T & -u_1 \mathbf{P}_1^T \\ \mathbf{0}^T & \mathbf{P}_1^T & -v_1 \mathbf{P}_1^T \\ \vdots & & \\ \mathbf{P}_n^T & \mathbf{0}^T & -u_n \mathbf{P}_n^T \\ \mathbf{0}^T & \mathbf{P}_n^T & -v_n \mathbf{P}_n^T \end{bmatrix} \begin{bmatrix} \mathbf{m}_1 \\ \mathbf{m}_2 \\ \mathbf{m}_3 \end{bmatrix} = P\mathbf{m} = 0 \quad \Longrightarrow \quad \begin{array}{c} \text{minimize} & \|P\mathbf{m}\|^2 \\ \text{subject to} & \|\mathbf{m}\|^2 = 1 \\ \end{array}$$

SVD



Singular Value Decomposition

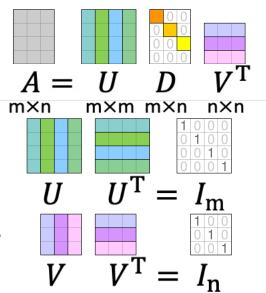
Generalization of the eigen-decomposition of a square matrix to any
 m by n matrix

$$A = UDV^{\mathsf{T}} \qquad D = \begin{bmatrix} \sigma_1 & & & \\ & \sigma_2 & & \\ & & & \\ & & & \sigma_N \end{bmatrix}$$

U: an m by m orthogonal matrix

D: an m by n diagonal matrix; entries on diagonal called **singular values**

V: an n by n orthogonal *matrix*

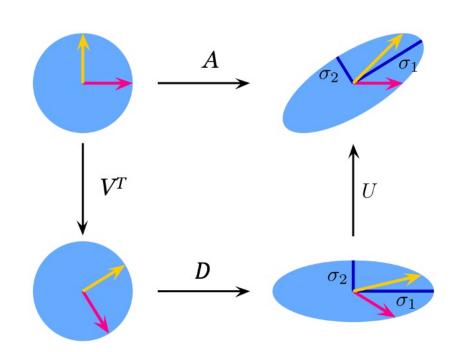


SVD



Geometric meaning

$$A = UDV^{\mathrm{T}}$$

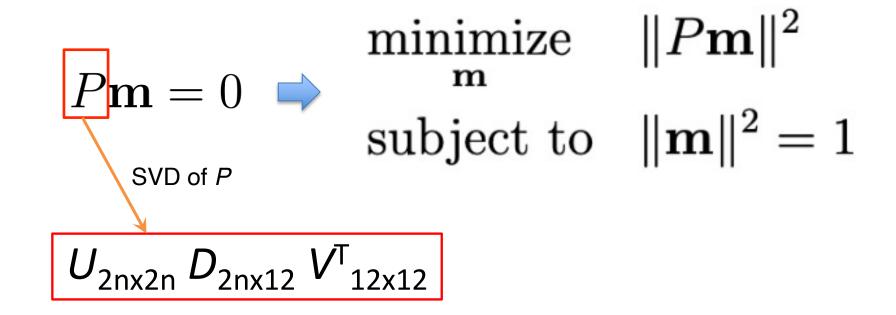


Example (square matrix)

$$\begin{bmatrix} 3 & -2 \\ 1 & 5 \end{bmatrix} = \begin{bmatrix} -.40 & .916 \\ .916 & .40 \end{bmatrix} \cdot \begin{bmatrix} 5.39 & 0 \\ 0 & 3.154 \end{bmatrix} \cdot \begin{bmatrix} -.05 & .999 \\ .999 & .05 \end{bmatrix}$$
 Transformation Rotation Scaling Rotation



Calibration: solve for projection matrix



Last column of V gives m

(Why? See page 593 of Hartley & Zisserman. Multiple View Geometry in Computer Vision)



Least-squares solution of homogeneous equations

This problem is solvable as follows. Let $A = UDV^T$. The problem then requires us to minimize $\|UDV^T\mathbf{x}\|$. However, $\|UDV^T\mathbf{x}\| = \|DV^T\mathbf{x}\|$ and $\|\mathbf{x}\| = \|V^T\mathbf{x}\|$. Thus, we need to minimize $\|DV^T\mathbf{x}\|$ subject to the condition $\|V^T\mathbf{x}\| = 1$. We write $\mathbf{y} = V^T\mathbf{x}$, and the problem is: minimize $\|D\mathbf{y}\|$ subject to $\|\mathbf{y}\| = 1$. Now, D is a diagonal matrix with its diagonal entries in descending order. It follows that the solution to this problem is $\mathbf{y} = (0, 0, \dots, 0, 1)^T$ having one non-zero entry, 1 in the last position. Finally $\mathbf{x} = V\mathbf{y}$ is simply the last column of V. The method is summarized in algorithm A5.4.

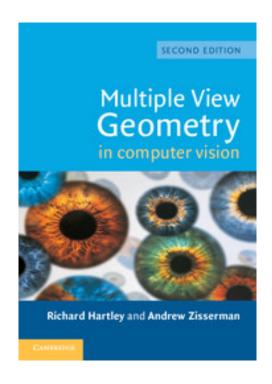
Objective

Given a matrix A with at least as many rows as columns, find x that minimizes $\|\mathbf{A}\mathbf{x}\|$ subject to $\|\mathbf{x}\| = 1$.

Solution

x is the last column of V, where $A = UDV^T$ is the SVD of A.

Algorithm A5.4. Least-squares solution of a homogeneous system of linear equations.





Camera parameters from project matrix

$$M = K \begin{bmatrix} R & \mathbf{t} \end{bmatrix}$$

$$K = \begin{bmatrix} f_x & s & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \alpha & -\alpha \cot \theta & c_x \\ 0 & \frac{\beta}{\sin \theta} & c_y \\ 0 & 0 & 1 \end{bmatrix}, R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix}, \mathbf{t} = \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

$$egin{aligned} R = egin{bmatrix} \mathbf{r}_1^T \ \mathbf{r}_2^T \ \mathbf{r}_3^T \end{bmatrix}, \ \mathbf{t} = egin{bmatrix} t_x \ t_y \ t_z \end{bmatrix} \end{aligned}$$

$$M = \begin{bmatrix} \alpha \mathbf{r}_1^T - \alpha \cot \theta \mathbf{r}_2^T + c_x \mathbf{r}_3^T & \alpha t_x - \alpha \cot \theta t_y + c_x t_z \\ \frac{\beta}{\sin \theta} \mathbf{r}_2^T + c_y \mathbf{r}_3^T & \frac{\beta}{\sin \theta} t_y + c_y t_z \\ \mathbf{r}_3^T & t_z \end{bmatrix}$$

SVD-solved projection matrix



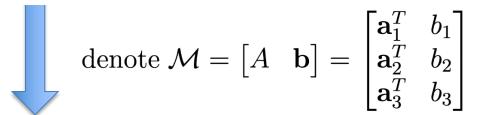
SVD-solved projection matrix is known up to scale, i.e., $ho\mathcal{M}=M$ — The true values of project matrix

$$\mathcal{M} = \frac{1}{\rho} M = \frac{1}{\rho} \begin{bmatrix} \alpha \mathbf{r}_1^T - \alpha \cot \theta \mathbf{r}_2^T + c_x \mathbf{r}_3^T & \alpha t_x - \alpha \cot \theta t_y + c_x t_z \\ \frac{\beta}{\sin \theta} \mathbf{r}_2^T + c_y \mathbf{r}_3^T & \frac{\beta}{\sin \theta} t_y + c_y t_z \\ \mathbf{r}_3^T & t_z \end{bmatrix}$$

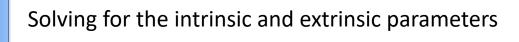


Camera parameters from project matrix

$$\mathcal{M} = \frac{1}{\rho} \begin{bmatrix} \alpha \mathbf{r}_1^T - \alpha \cot \theta \mathbf{r}_2^T + c_x \mathbf{r}_3^T & \alpha t_x - \alpha \cot \theta t_y + c_x t_z \\ \frac{\beta}{\sin \theta} \mathbf{r}_2^T + c_y \mathbf{r}_3^T & \frac{\beta}{\sin \theta} t_y + c_y t_z \\ \mathbf{r}_3^T & t_z \end{bmatrix}$$



$$\frac{1}{\rho} \begin{bmatrix} \alpha \mathbf{r}_1^T - \alpha \cot \theta \mathbf{r}_2^T + c_x \mathbf{r}_3^T & \alpha t_x - \alpha \cot \theta t_y + c_x t_z \\ \frac{\beta}{\sin \theta} \mathbf{r}_2^T + c_y \mathbf{r}_3^T & \frac{\beta}{\sin \theta} t_y + c_y t_z \\ \mathbf{r}_3^T & t_z \end{bmatrix} = \begin{bmatrix} \mathbf{a}_1^T & b_1 \\ \mathbf{a}_2^T & b_2 \\ \mathbf{a}_3^T & b_3 \end{bmatrix}$$





Camera parameters from project matrix

Intrinsic parameters:

$$\rho = \pm \frac{1}{\|\mathbf{a_3}\|}$$

$$c_x = \rho^2 (\mathbf{a_1} \cdot \mathbf{a_3})$$

$$c_y = \rho^2 (\mathbf{a_2} \cdot \mathbf{a_3})$$

$$\cos \theta = -\frac{(\mathbf{a_1} \times \mathbf{a_3}) \cdot (\mathbf{a_2} \times \mathbf{a_3})}{\|\mathbf{a_1} \times \mathbf{a_3}\| \cdot \|\mathbf{a_2} \times \mathbf{a_3}\|}$$

$$\alpha = \rho^2 \|\mathbf{a_1} \times \mathbf{a_3}\| \sin \theta$$

$$\beta = \rho^2 \|\mathbf{a_2} \times \mathbf{a_3}\| \sin \theta$$

Extrinsic parameters:

$$\mathbf{r_1} = \frac{\mathbf{a_2} \times \mathbf{a_3}}{\|\mathbf{a_2} \times \mathbf{a_3}\|}$$

$$\mathbf{r_3} = \rho \mathbf{a_3}$$

$$\mathbf{r_2} = \mathbf{r_3} \times \mathbf{r_1}$$

$$\mathbf{t} = \rho K^{-1} \mathbf{b}$$





- At least 6 3D-2D point pairs
 - 3D points with known 3D coordinates
 - Corresponding image points with known 2D coordinates



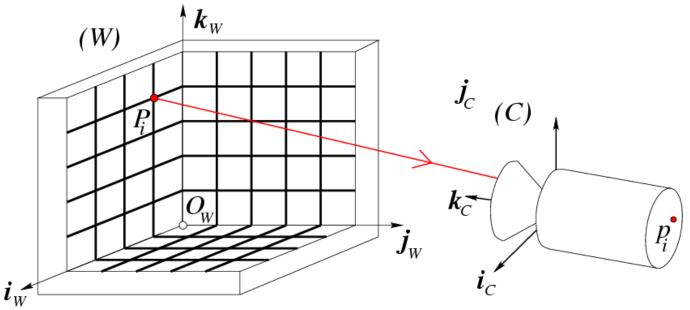






Find 3D-2D corresponding points

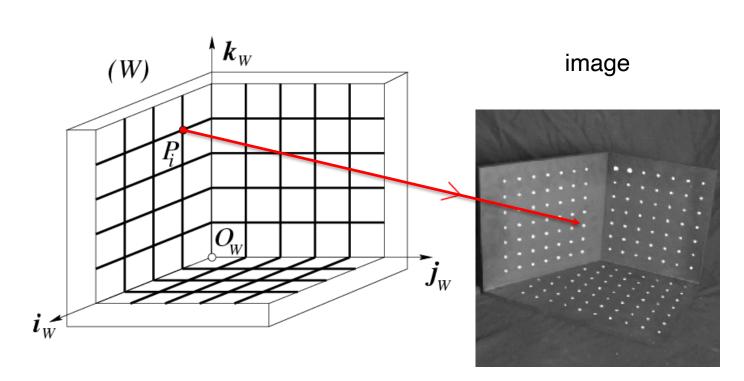
- Calibration rig a special apparatus
 - $-P_1, \dots P_n$ with known positions in $[O_w, i_w, j_w, k_w]$







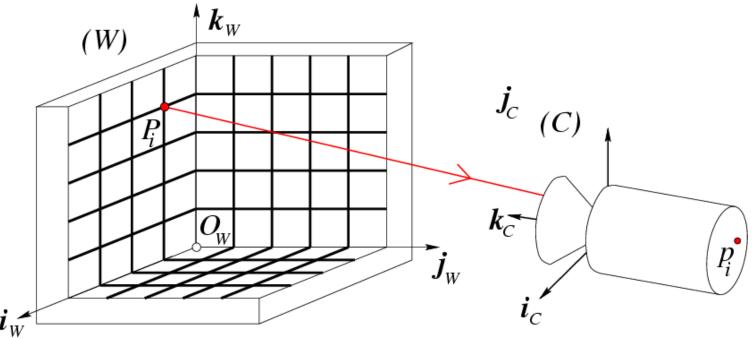
- Calibration rig a special apparatus
 - $-P_1, \dots P_n$ with known positions in $[O_w, i_w, j_w, k_w]$
 - $-p_1, \dots p_n$ known positions in the image
 - At least 6 pairs
- Goal
 - Intrinsic parameters
 - Extrinsic parameters



Calibration



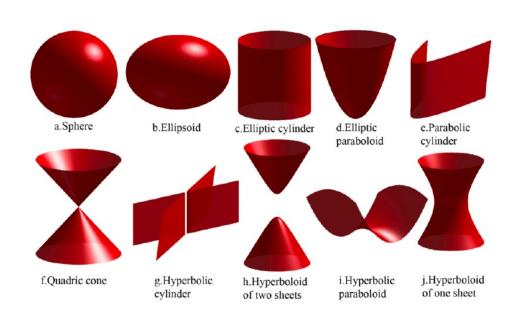
Always solvable?

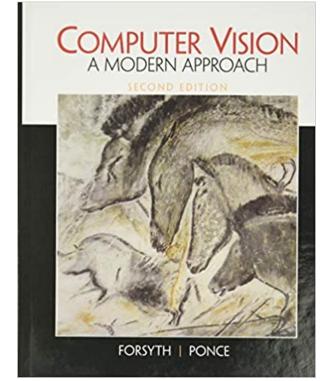


Calibration



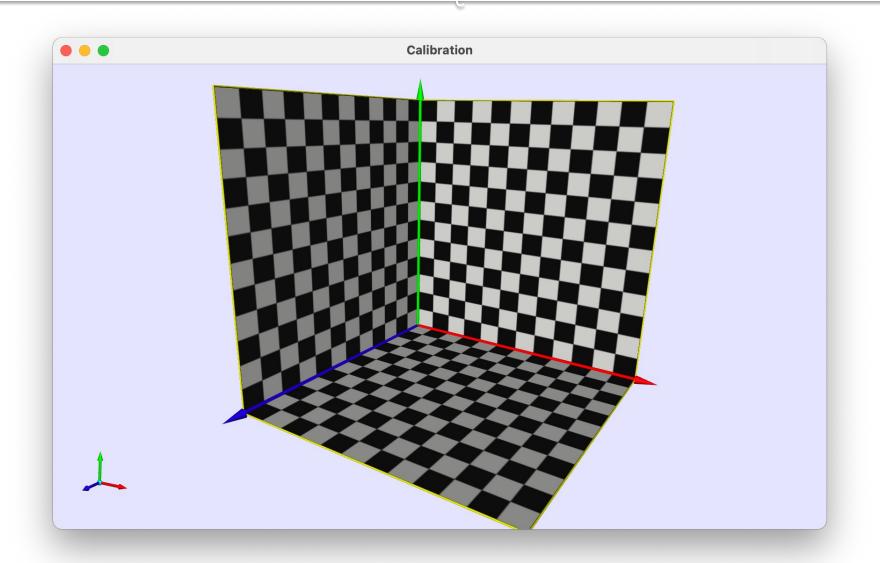
- Always solvable?
 - $-\{P_i\}$ cannot lie on the same plane
 - $-\{P_i\}$ cannot lie on the intersection curve of two quadric surfaces















Epipolar geometry

