

# Voxels and voxelisation

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GEO1004:  
3D modelling of the built environment

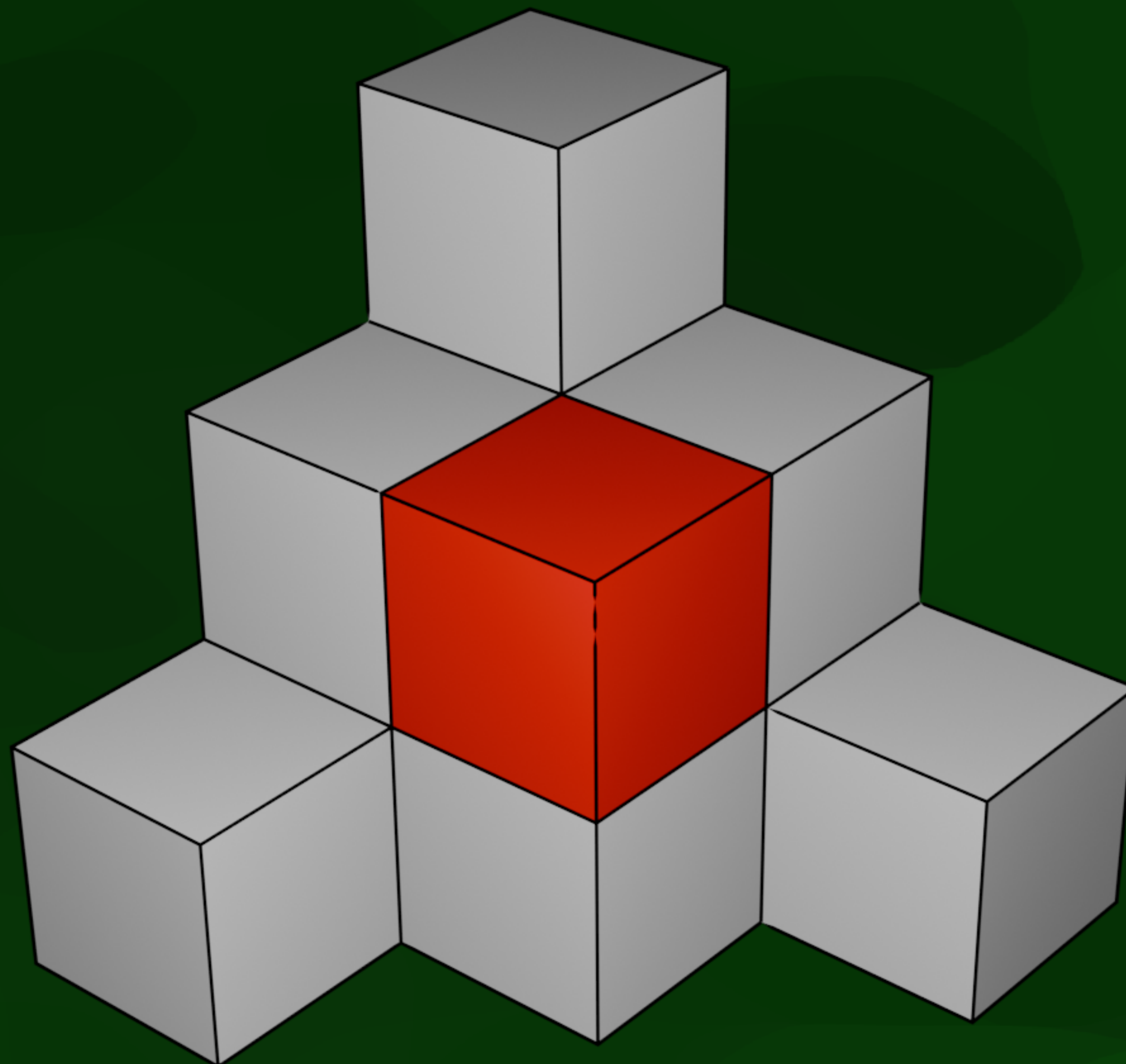
<https://3d.bk.tudelft.nl/courses/geo1004>



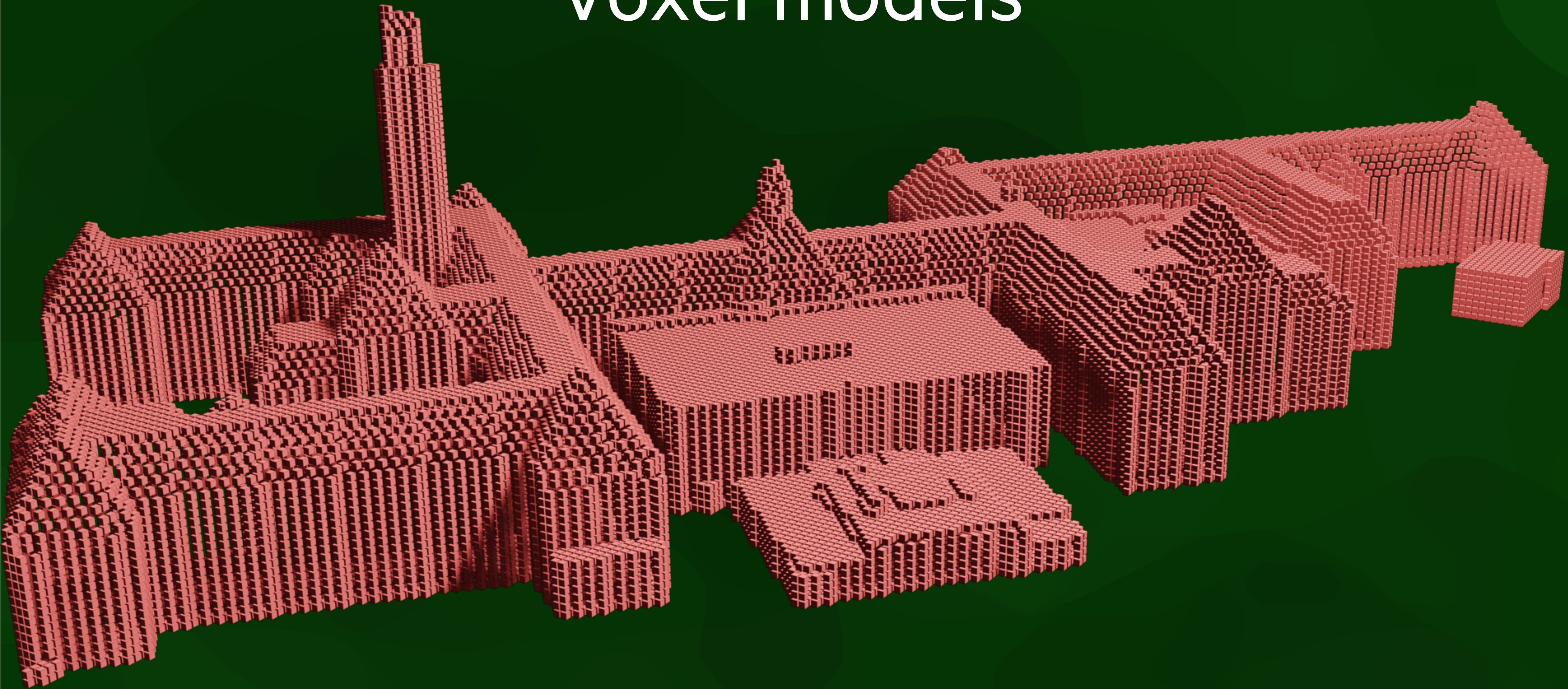
3D geoinformation

Department of Urbanism  
Faculty of Architecture and the Built Environment  
Delft University of Technology

# Voxels: 3D pixels



# Voxel models



# Why?

- **Simplicity:** simple storage, simple processing methods, simple to use in applications
- **Robustness:** many issues solved automatically or at least more easily, few degenerate cases
- **Speed:** easy to do parallel processing by processing voxels independently

# Nomenclature

- 2D:

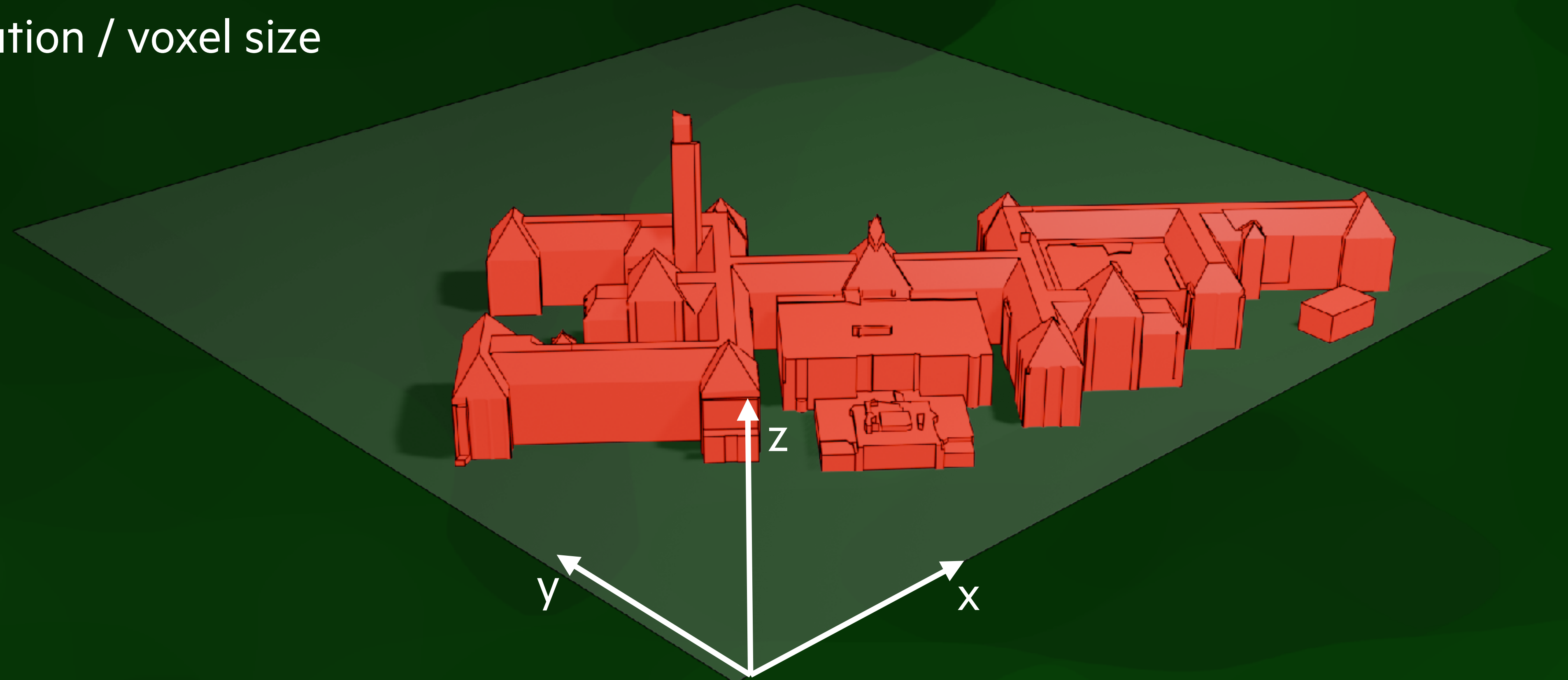
- pixel
- image / 2D raster
- (2D) rasterisation

- 3D:

- voxel
- voxel model / 3D raster
- voxelisation / 3D rasterisation

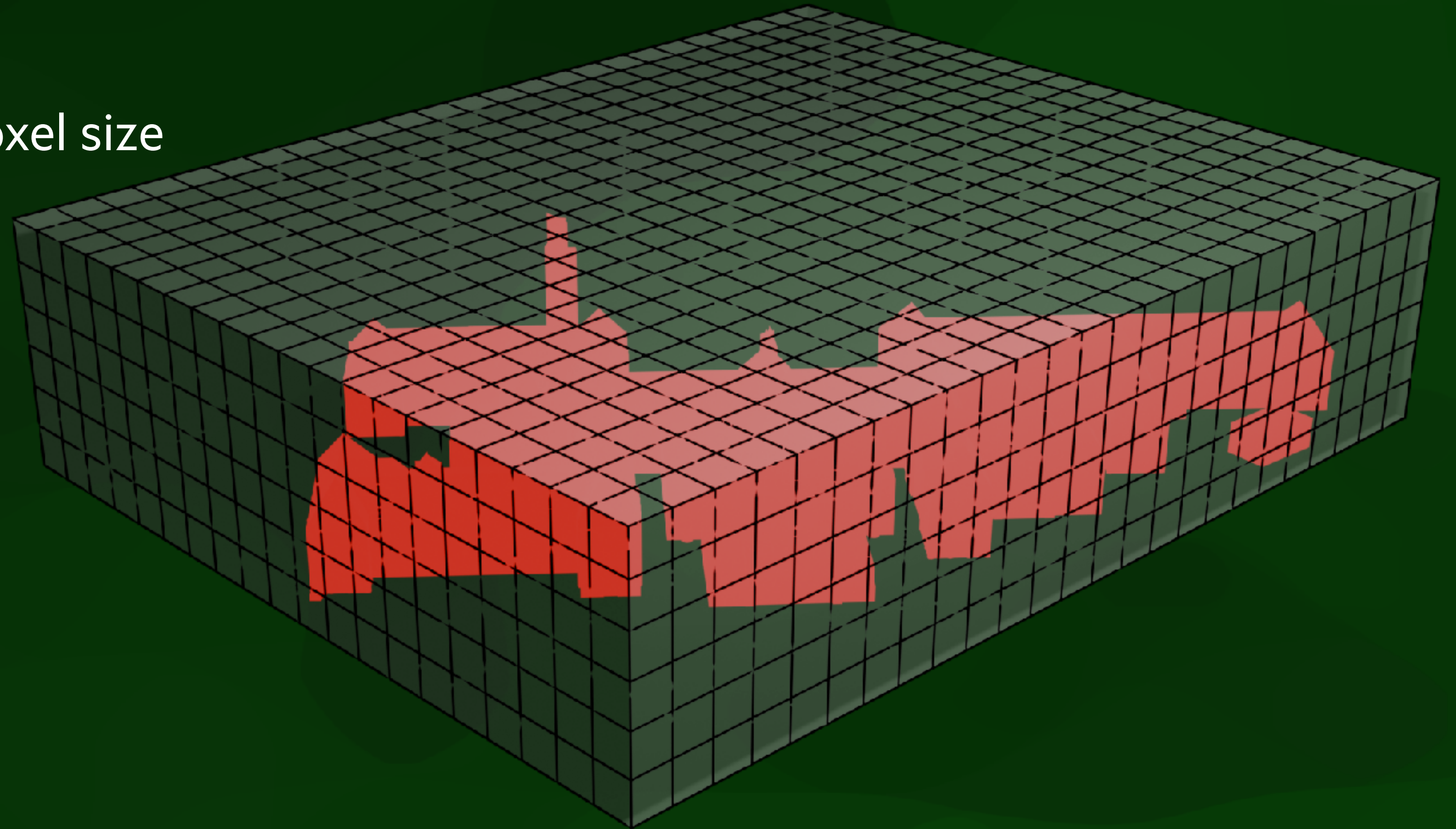
# Setup

1. Define domain (origin and orientation / axes)
2. Define resolution / voxel size



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# Usual (dense) encoding

1. Define order for storage / traversal (first  $x$   $0..i$ , then  $y$   $0..j$ , then  $z$   $0..k$ )
2. Following the order: specify what is in each voxel, e.g. occupied or not, object IDs, field values, etc.
  - [..., false, true, true, false, ...]
  - [..., 1, 1, 3, 3, 1, ...]
  - [..., 3.45, 3.56, 3.78, 3.99, ...]



# Sparse encoding

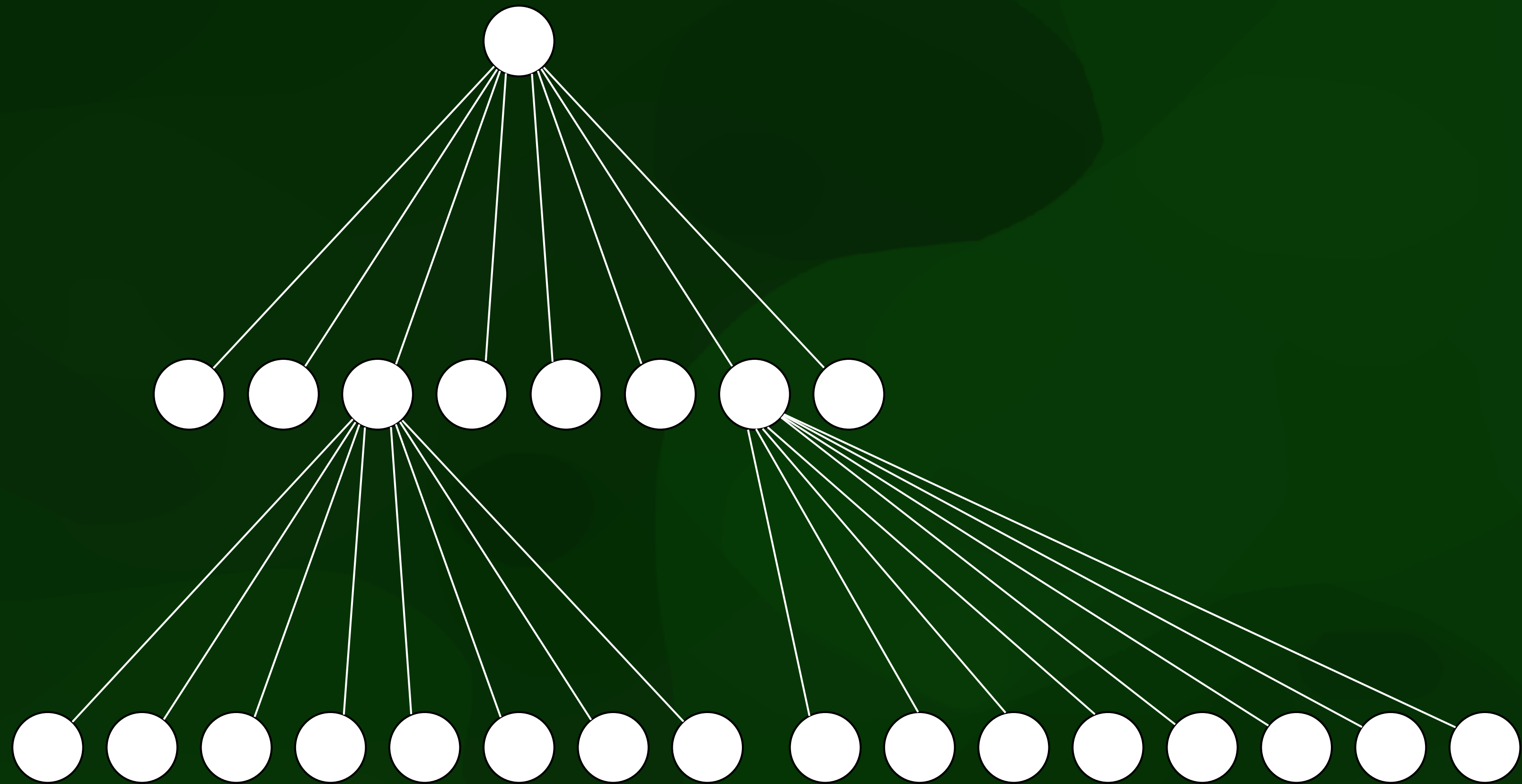
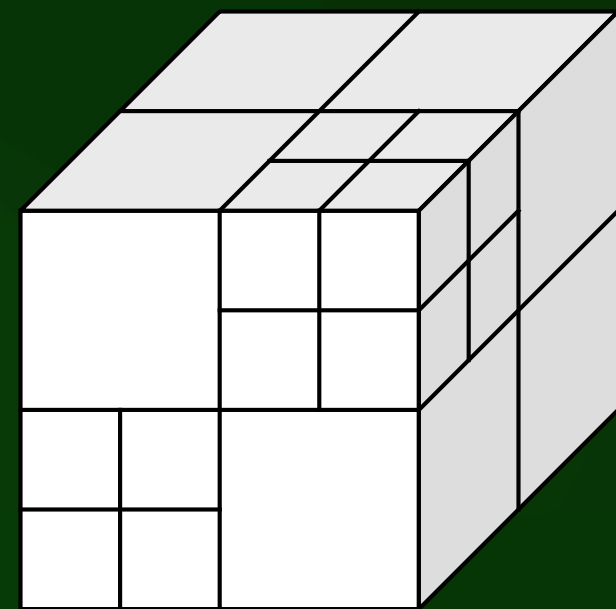
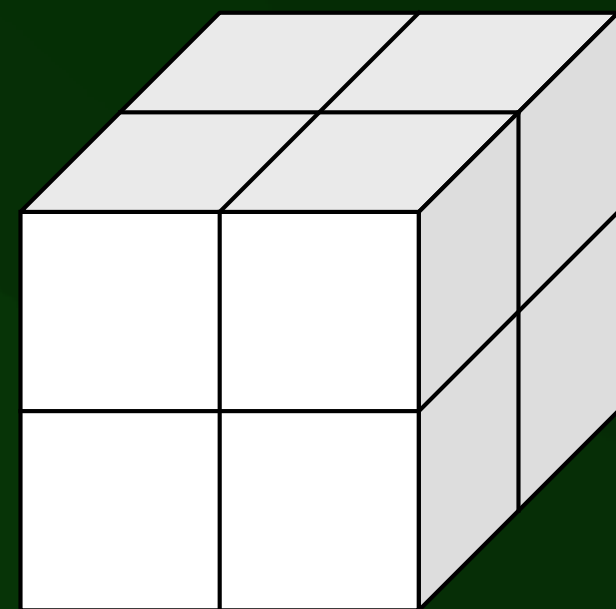
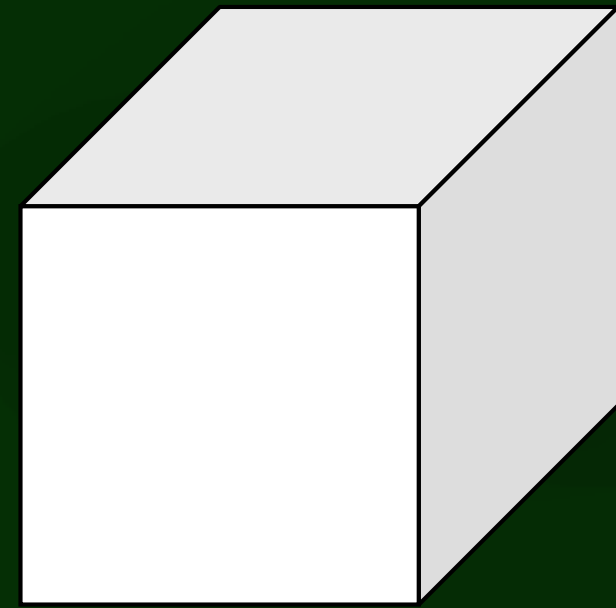
- List of entries containing for each voxel:
  - location (along x, y, z)
  - contents
- e.g.  $(x, y, z, ID) = \dots, [100, 105, 0, 3], [101, 105, 0, 3], \dots$

What encoding is better?

# Variations

- Varying sizes, e.g.
  - different size along z dimension
  - smaller size around an area of interest
- Differently shaped cells, e.g. octahedra

# Hierarchical subdivisions

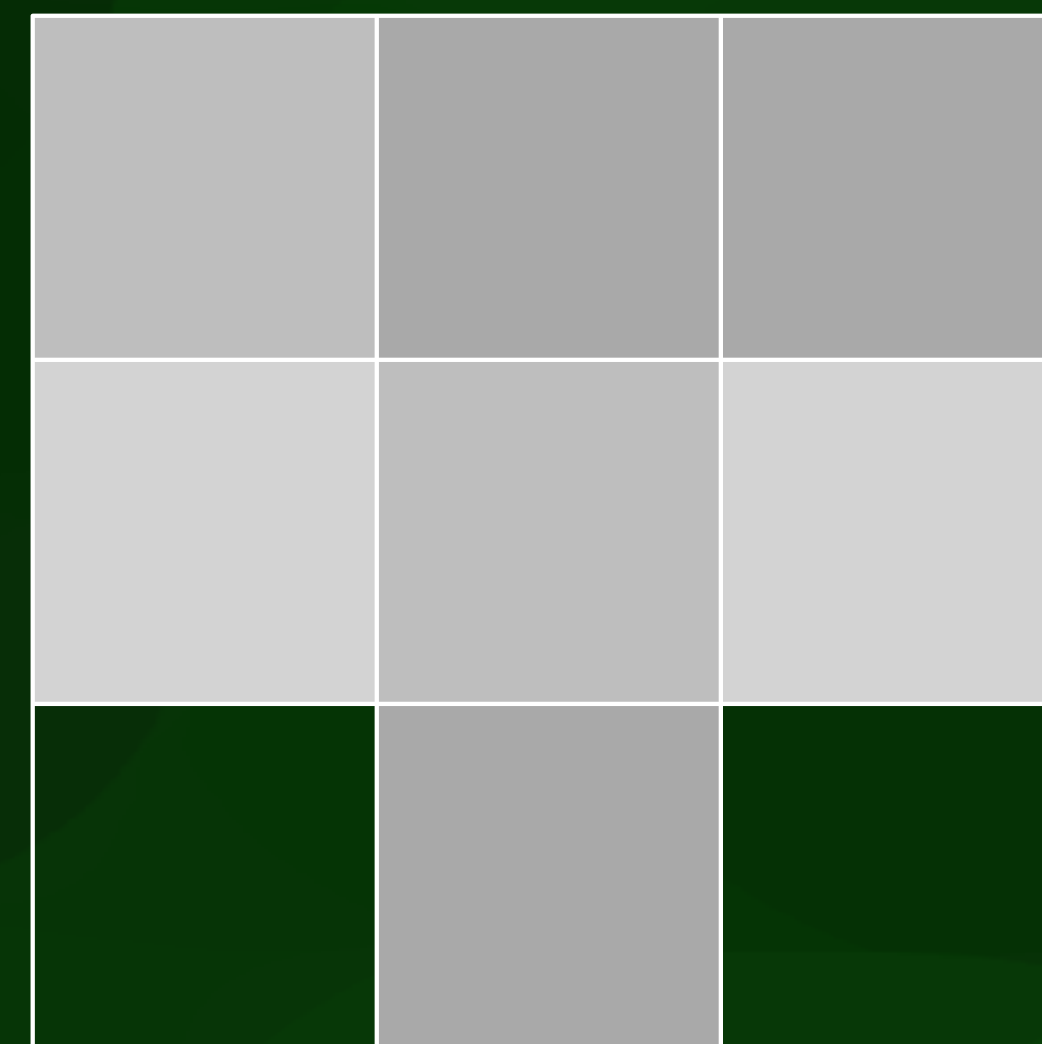
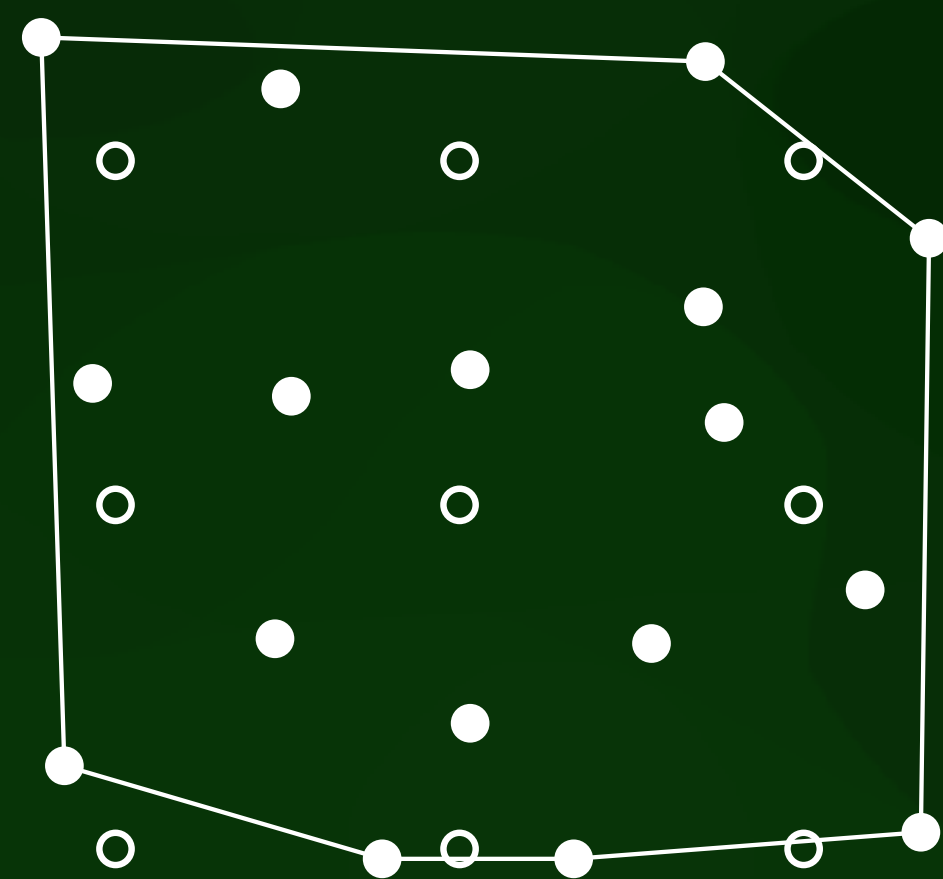


# Hierarchical subdivisions

- Octrees: evenly along every axis
- Bintrees: evenly along alternating axes
- k-d trees: using a value along alternating axes

# Voxelisation

# Voxelisation of fields

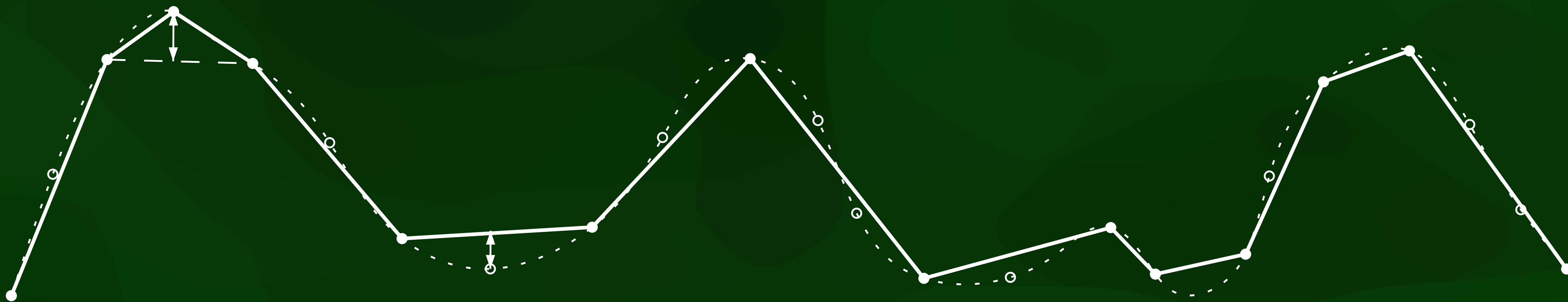
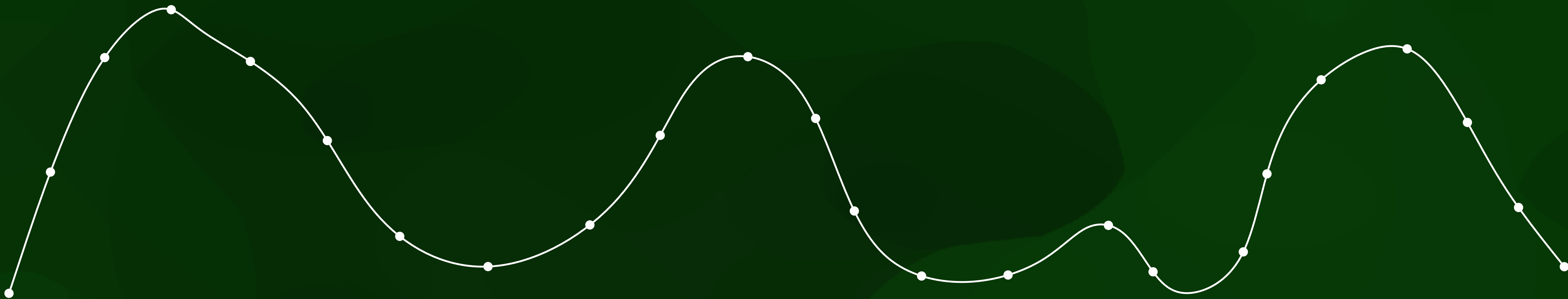


# Voxelisation of fields

- Nearest neighbour
- IDW
- Linear in tetrahedra
- Natural neighbour
- Kriging
- etc.



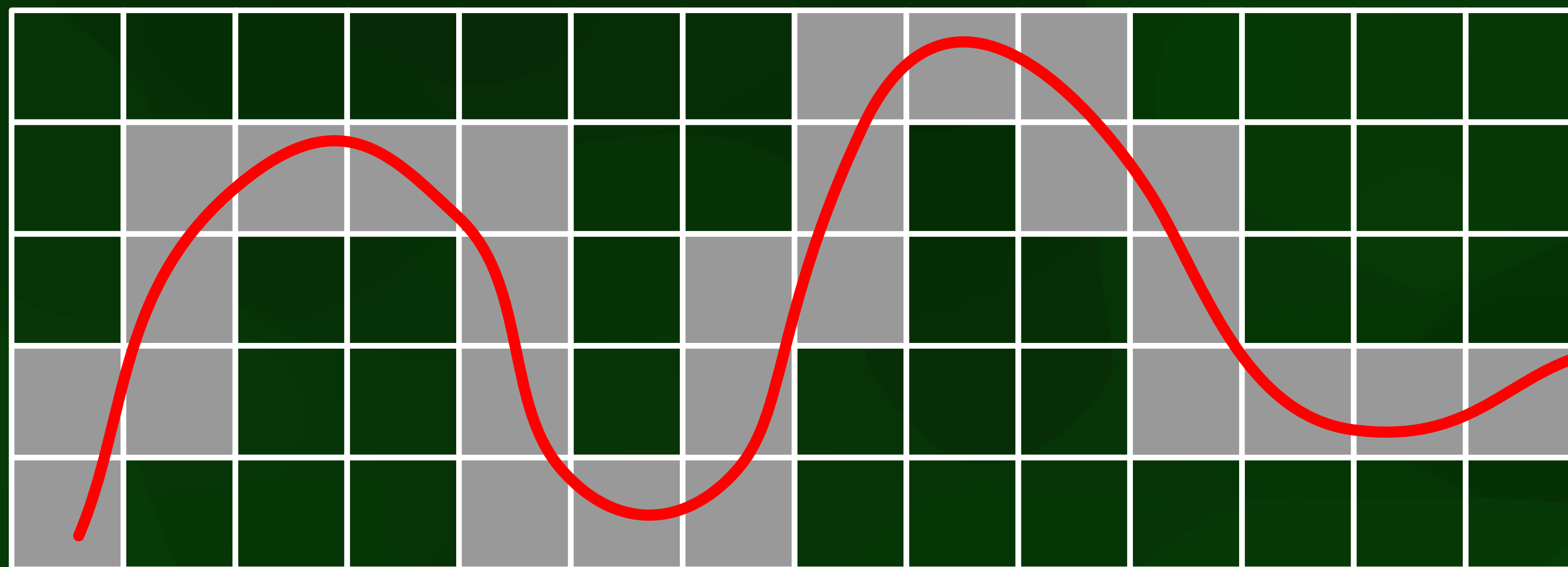
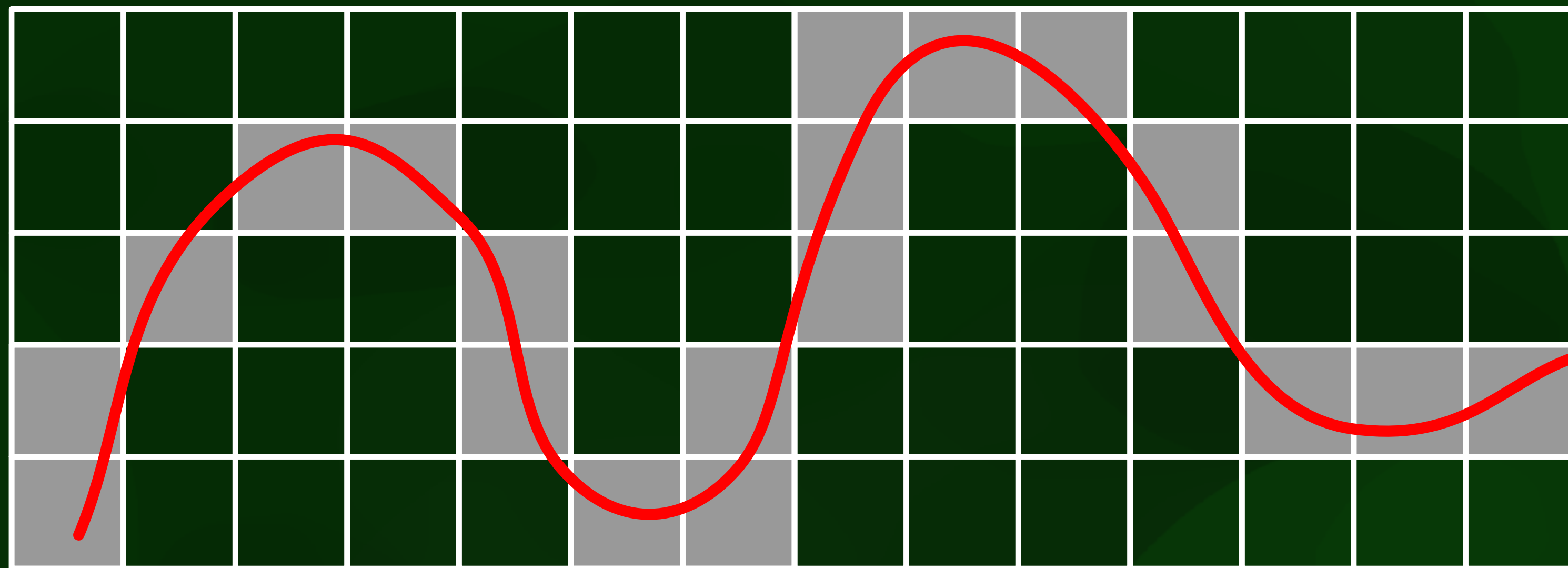
# Voxels to points



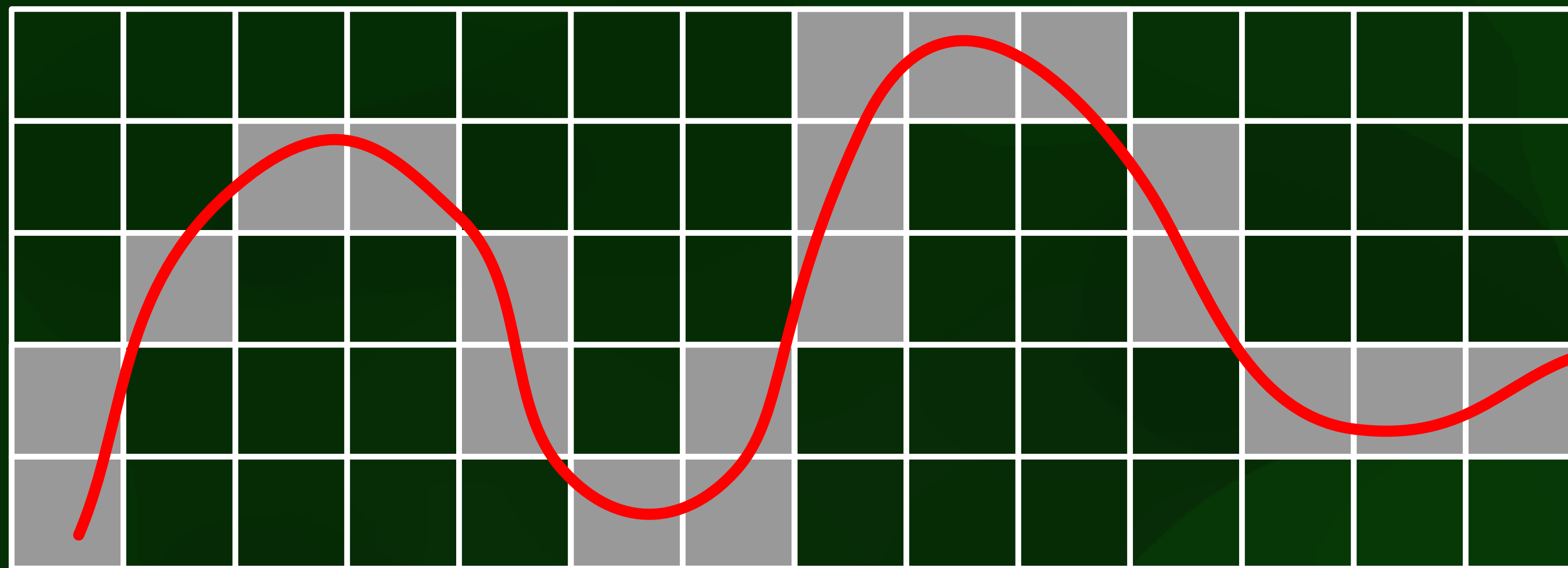
# Voxelisation of objects

Starting with 2D: rasterisation

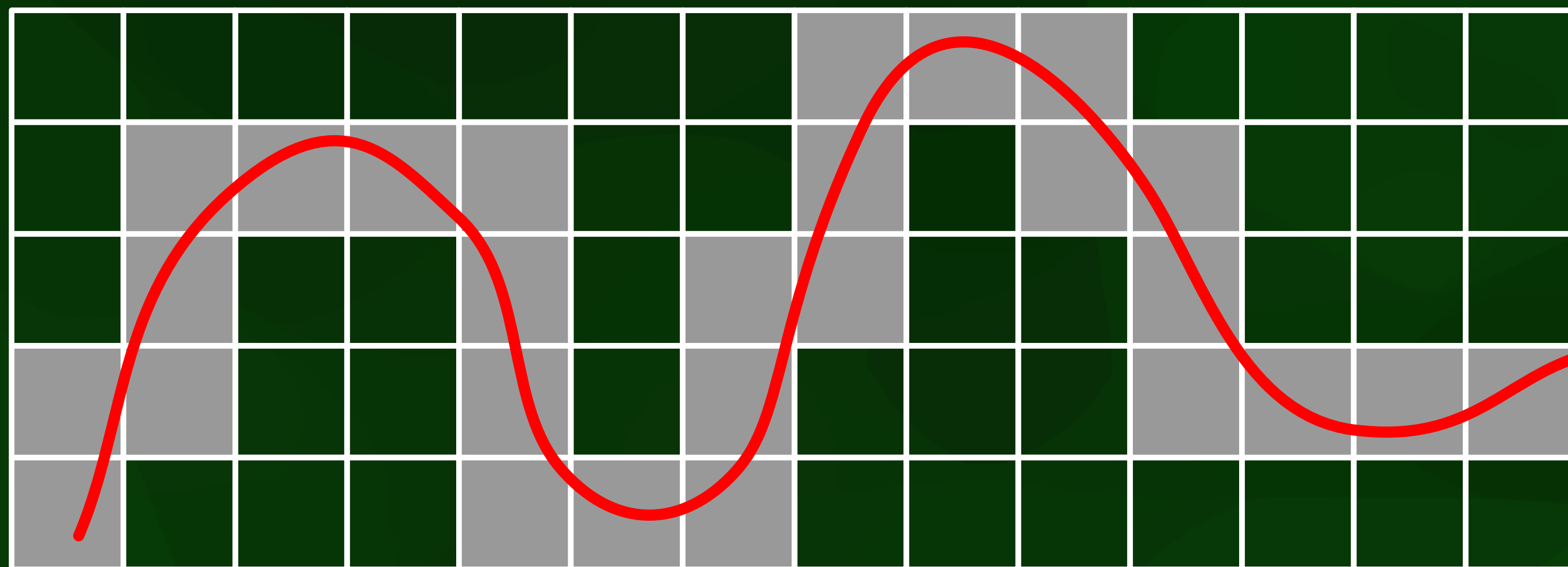
# In 2D: what is the difference?



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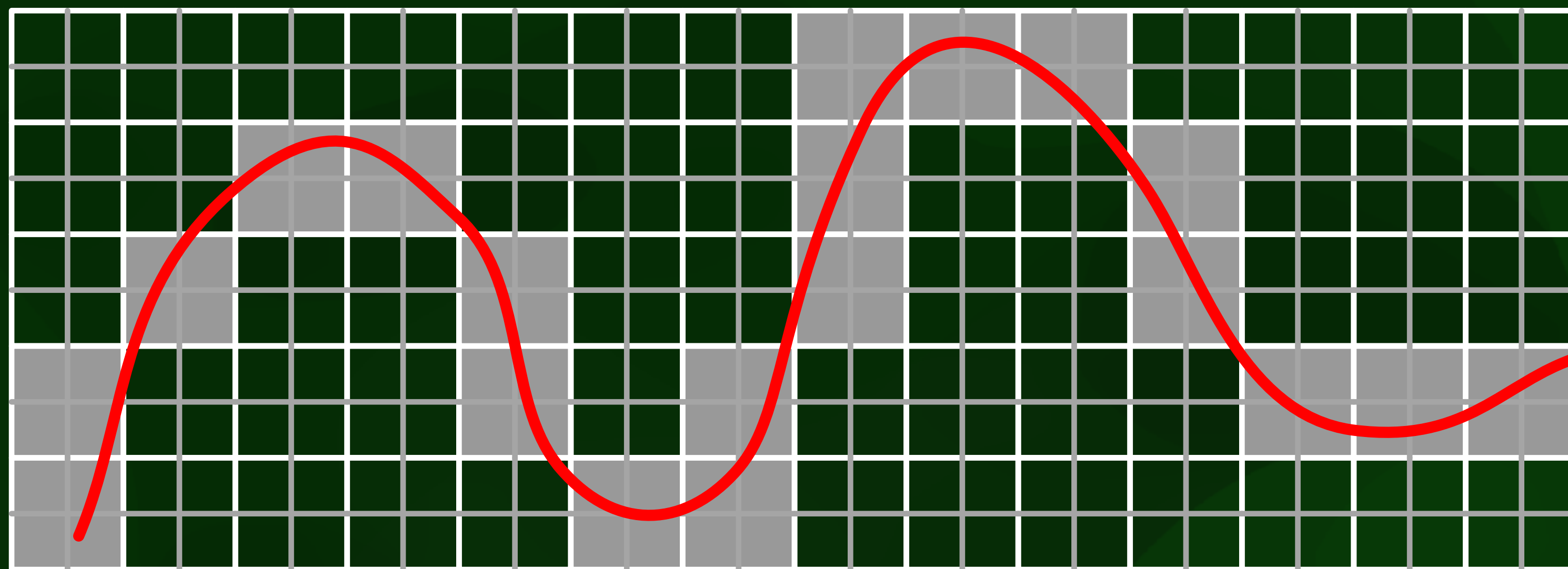


4-connected

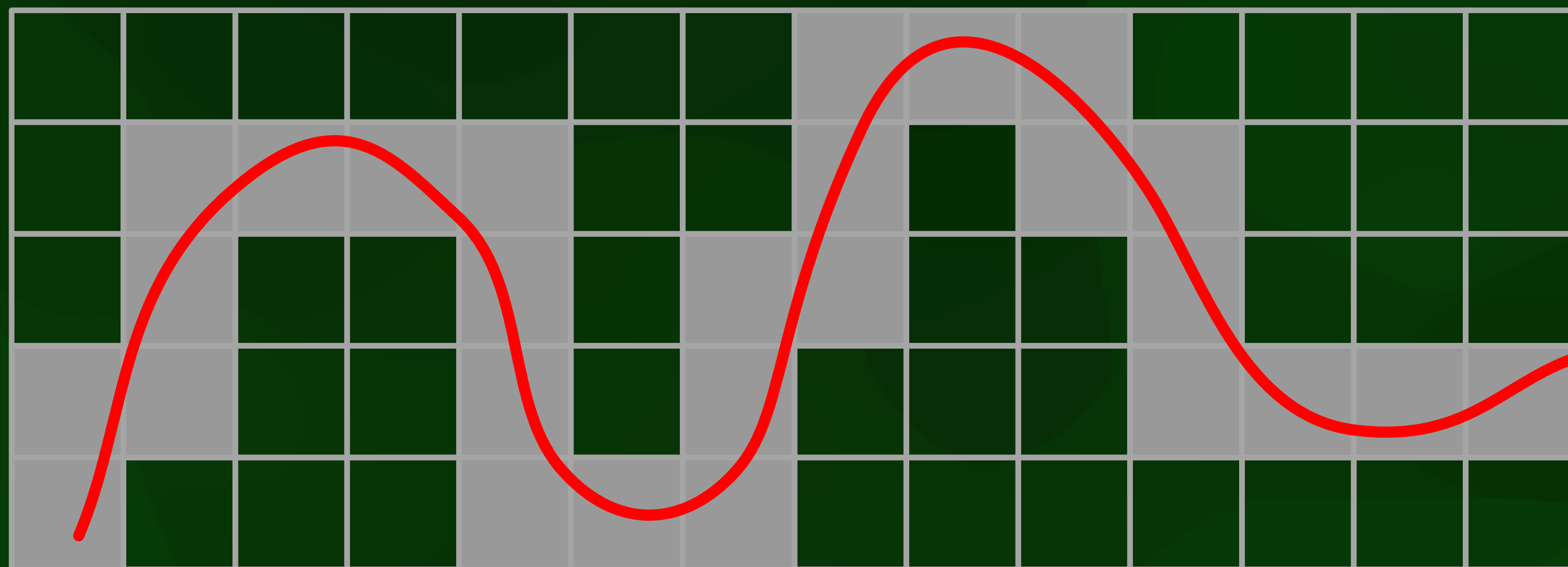


8-connected

# 2D targets

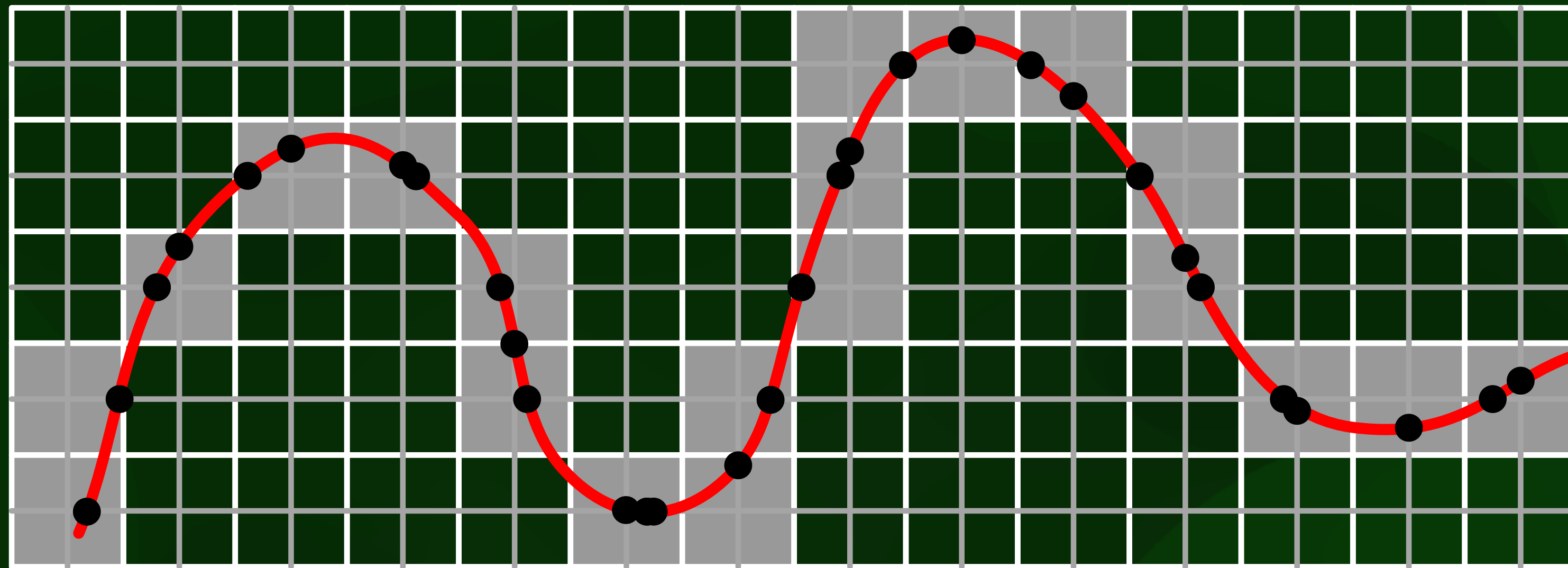


4-connectivity

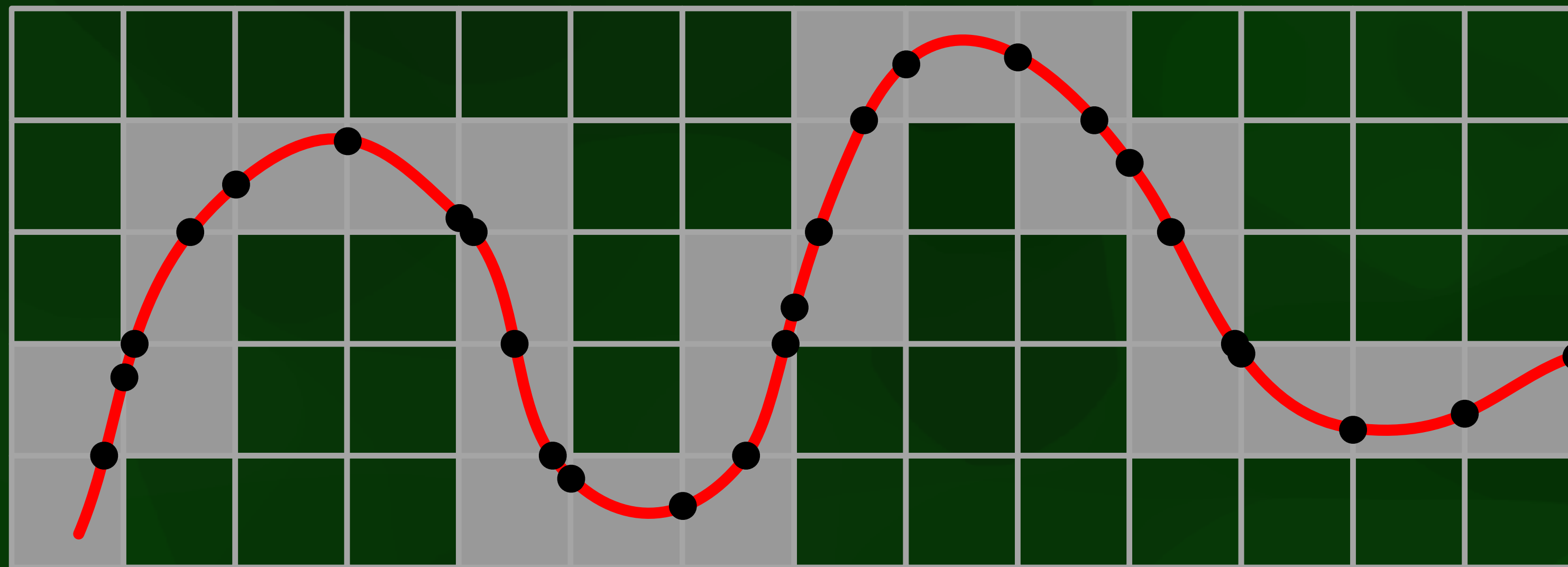


8-connectivity

# 2D targets



4-connectivity

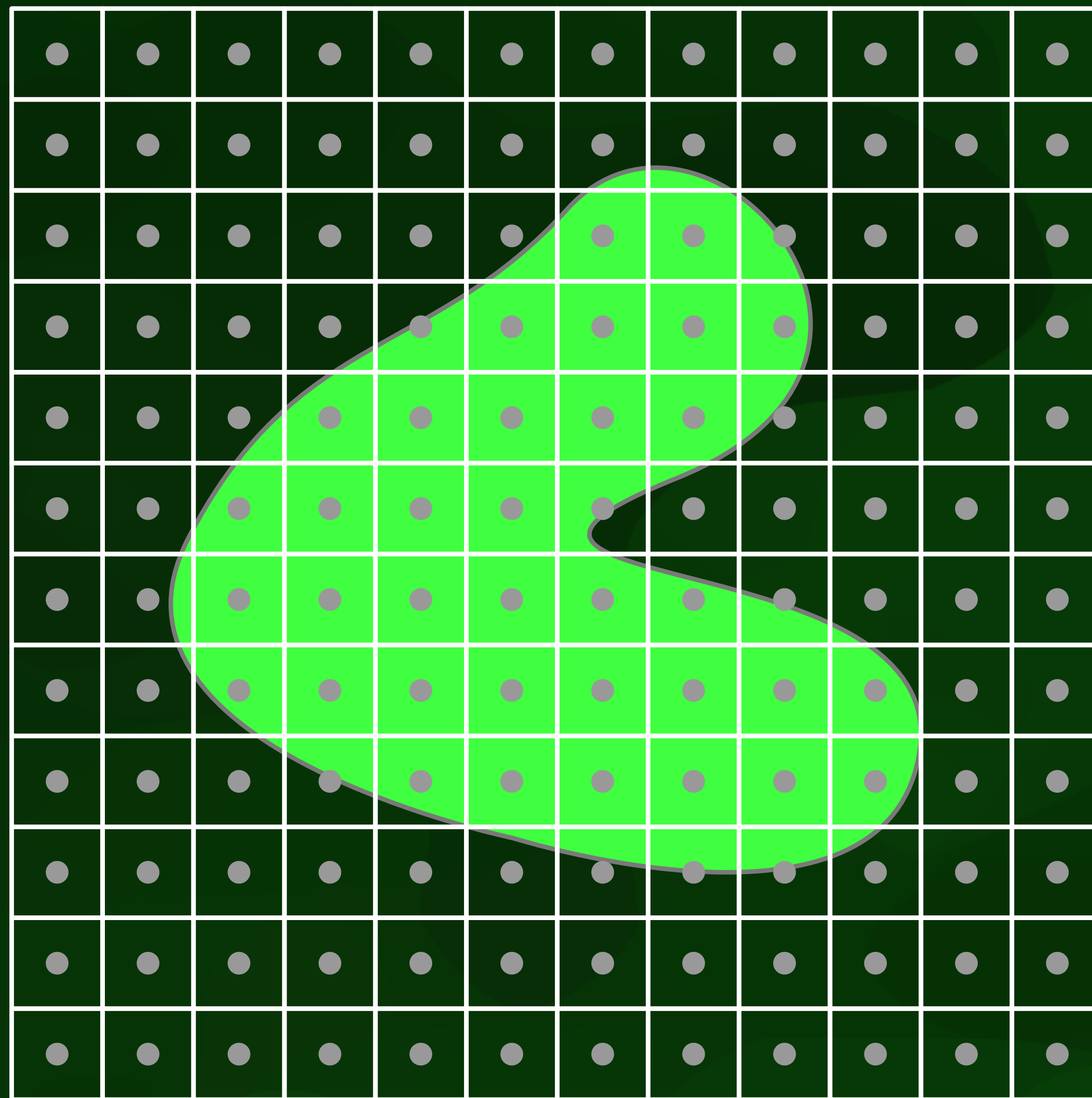


8-connectivity

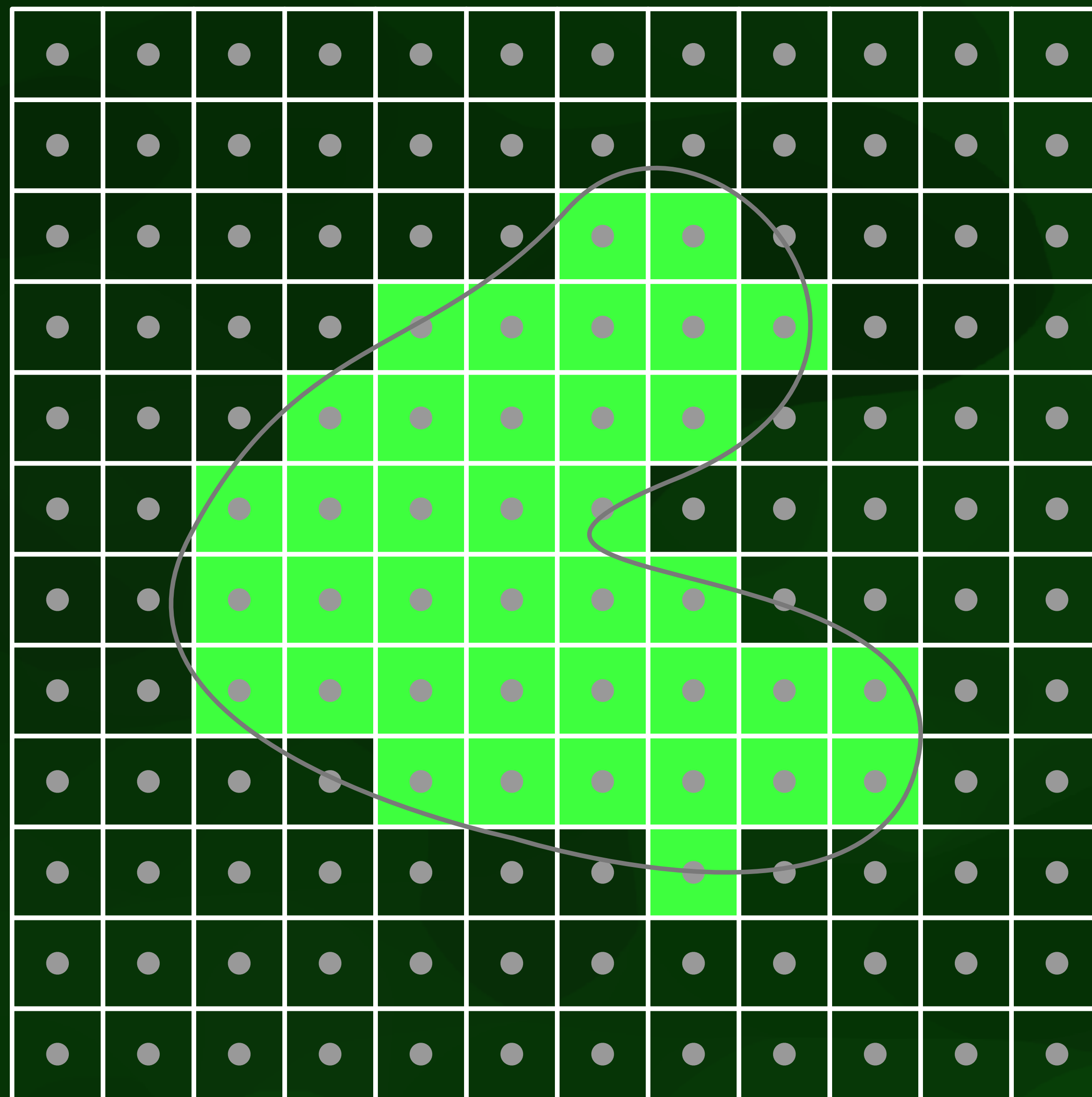




# Targets for areas



# Targets for areas



# Duality of targets in 2D

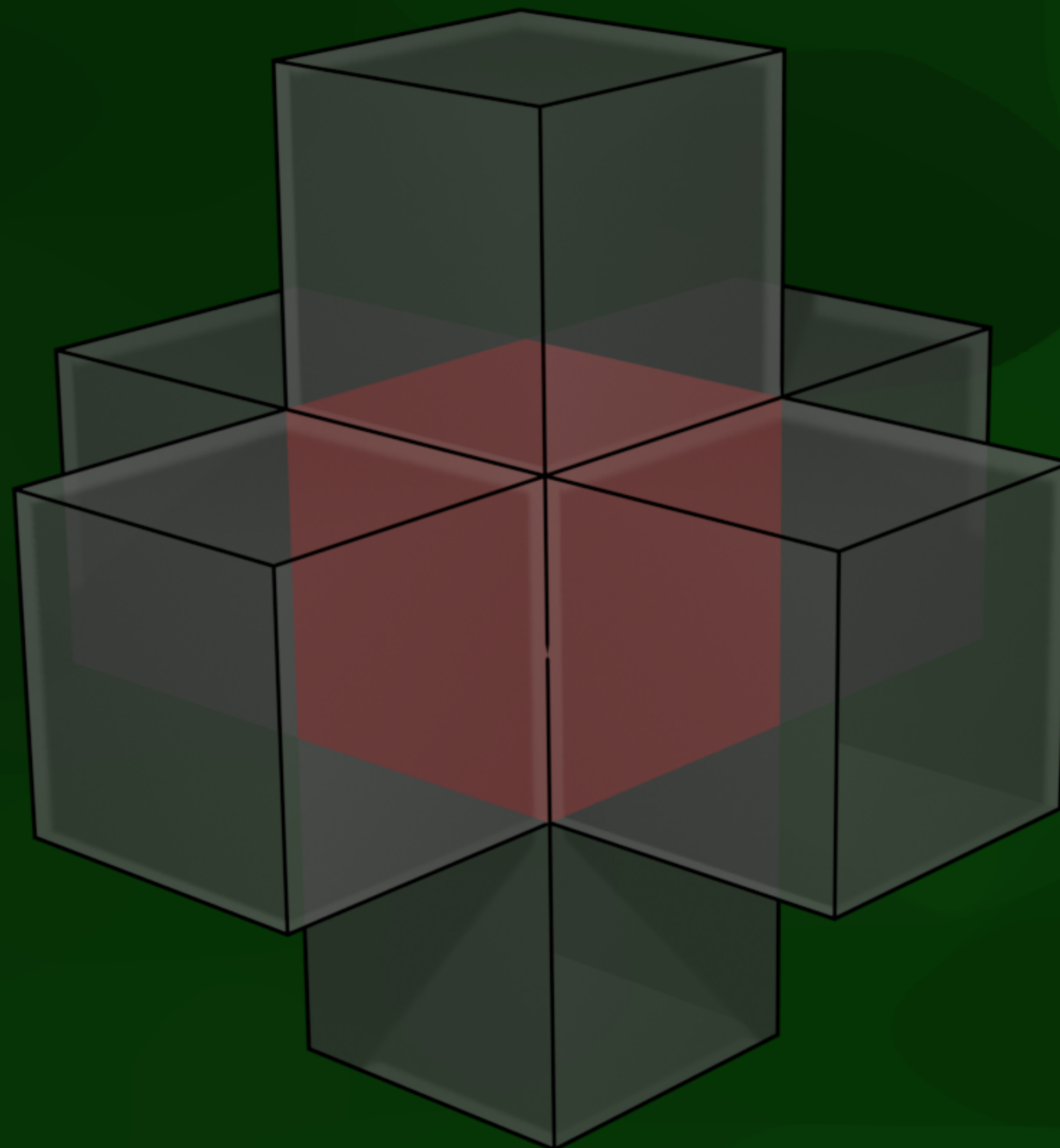
- To detect:
  - points (0D)  $\rightarrow$  squares (2D)
  - lines (1D)  $\rightarrow$  line segments (1D)
  - areas (2D)  $\rightarrow$  centre points (0D)

# Duality of targets in 3D

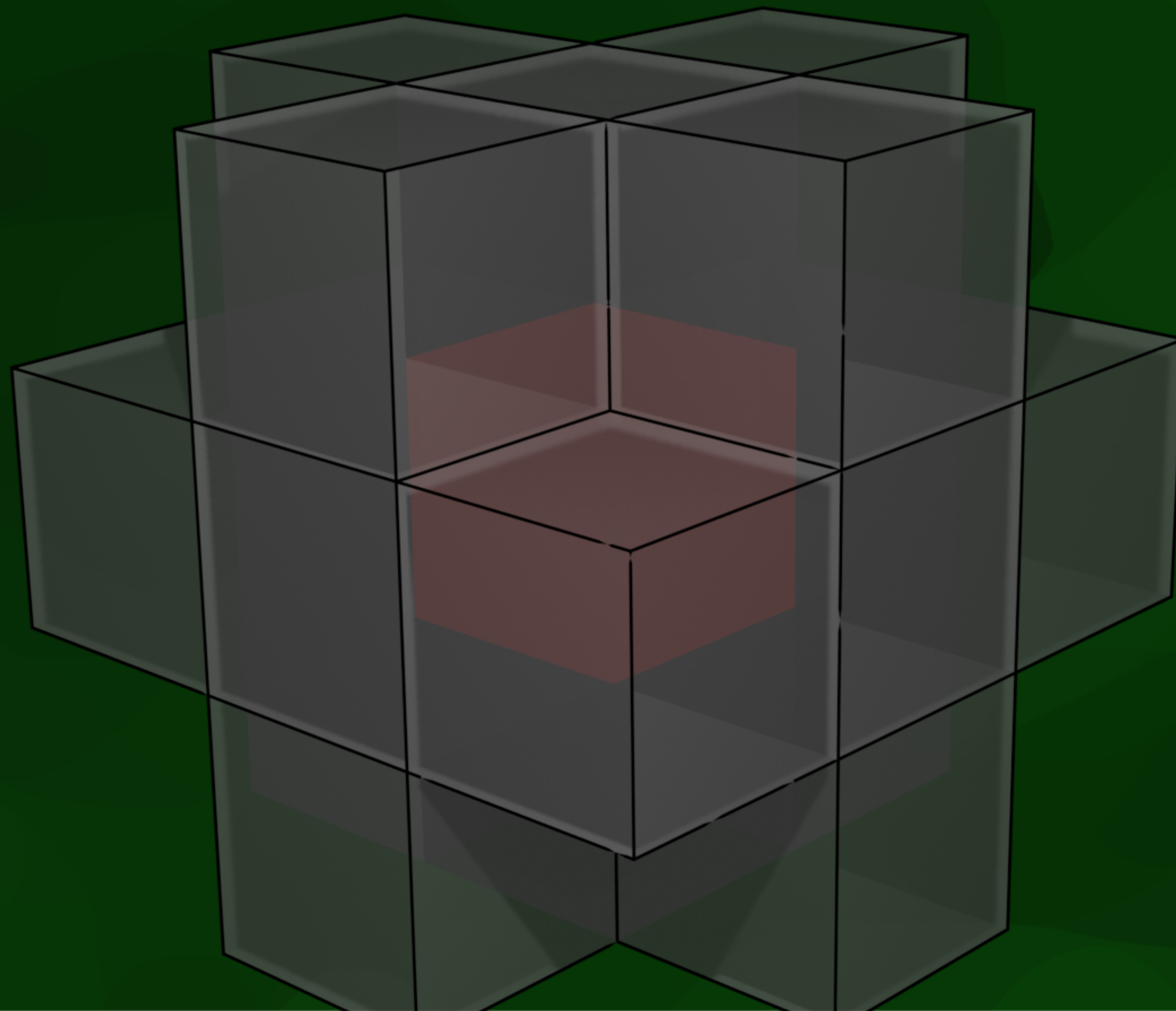
- To detect:
  - points (0D)  $\rightarrow$  cubes (3D)
  - lines (1D)  $\rightarrow$  surfaces (2D)
  - surfaces (2D)  $\rightarrow$  line segments (1D)
  - volumes (3D)  $\rightarrow$  centre points (0D)

# Connectivity in 3D

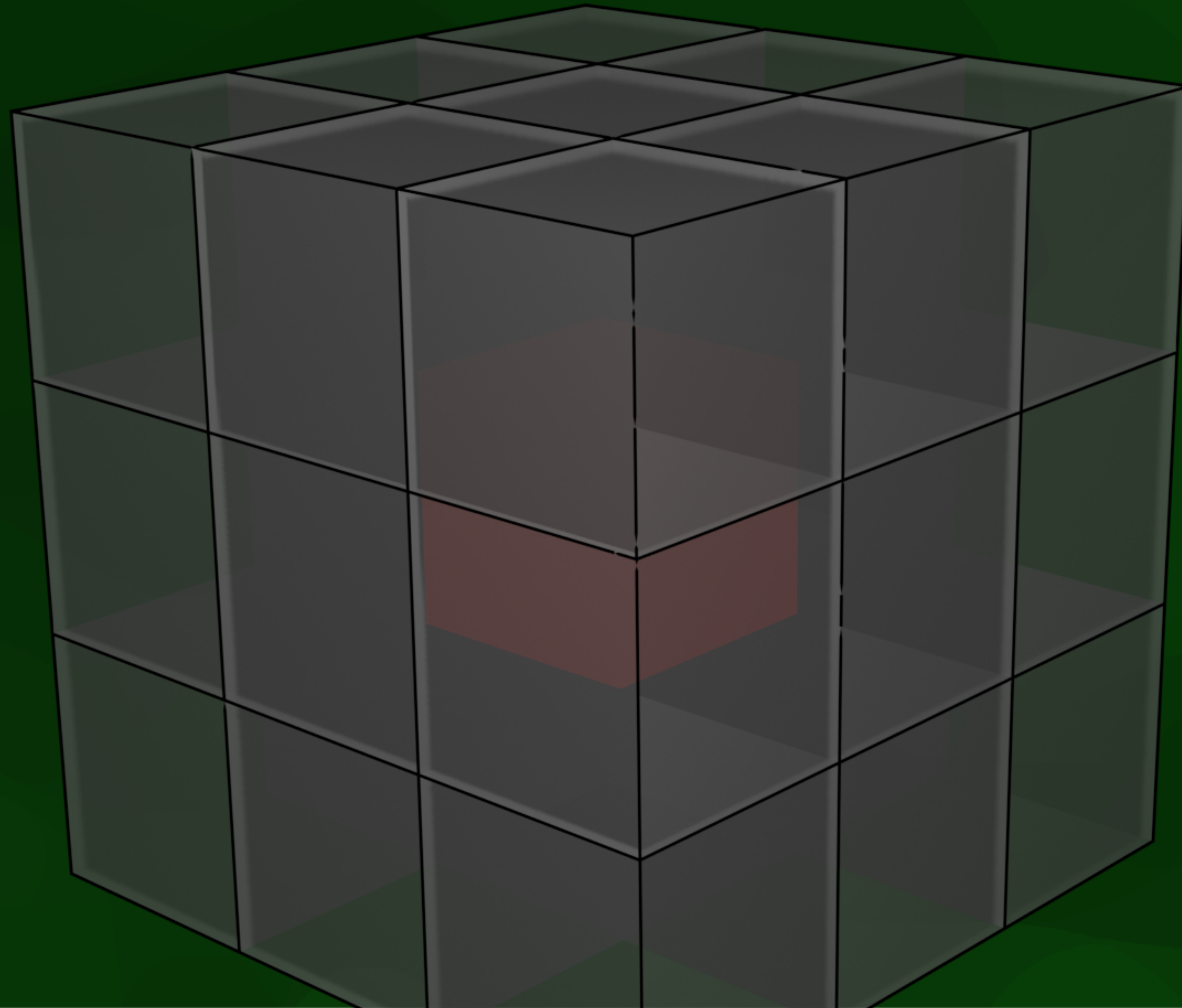
# 6-connectivity



# 18-connectivity

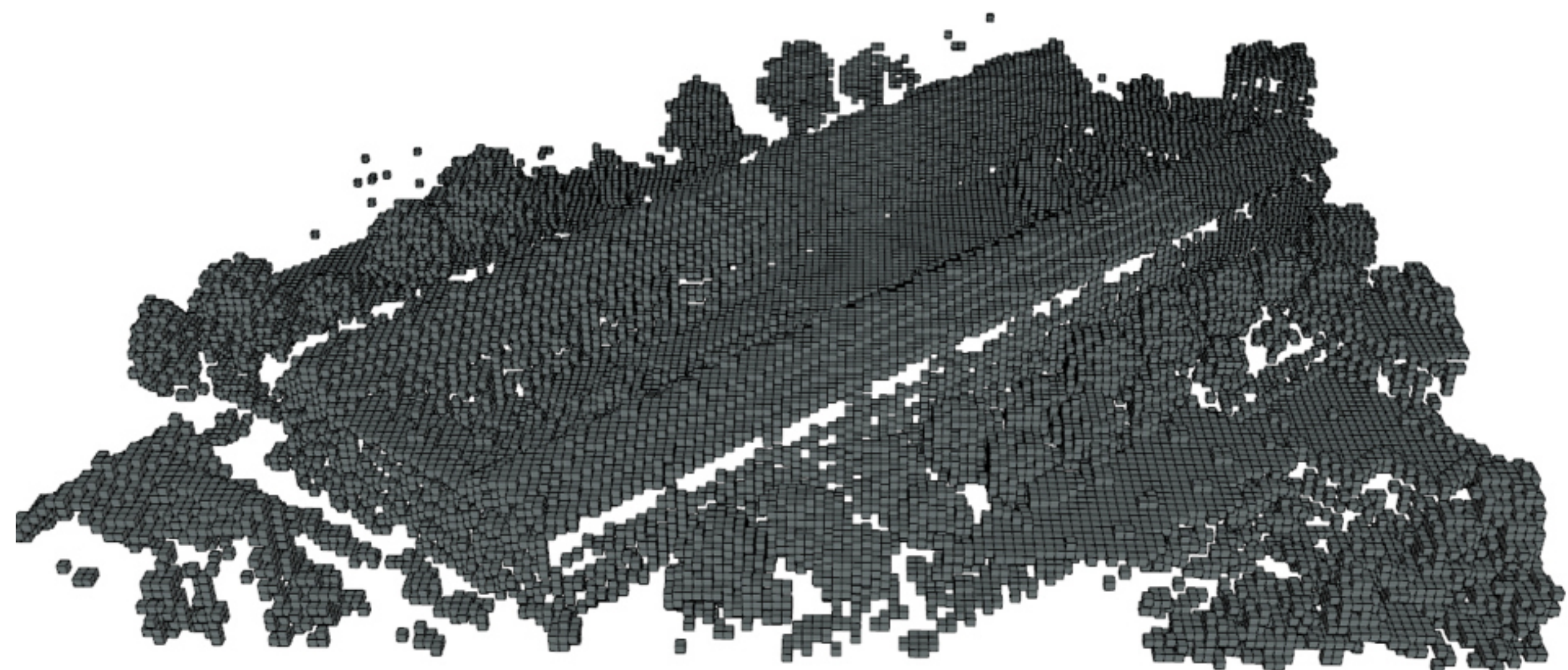
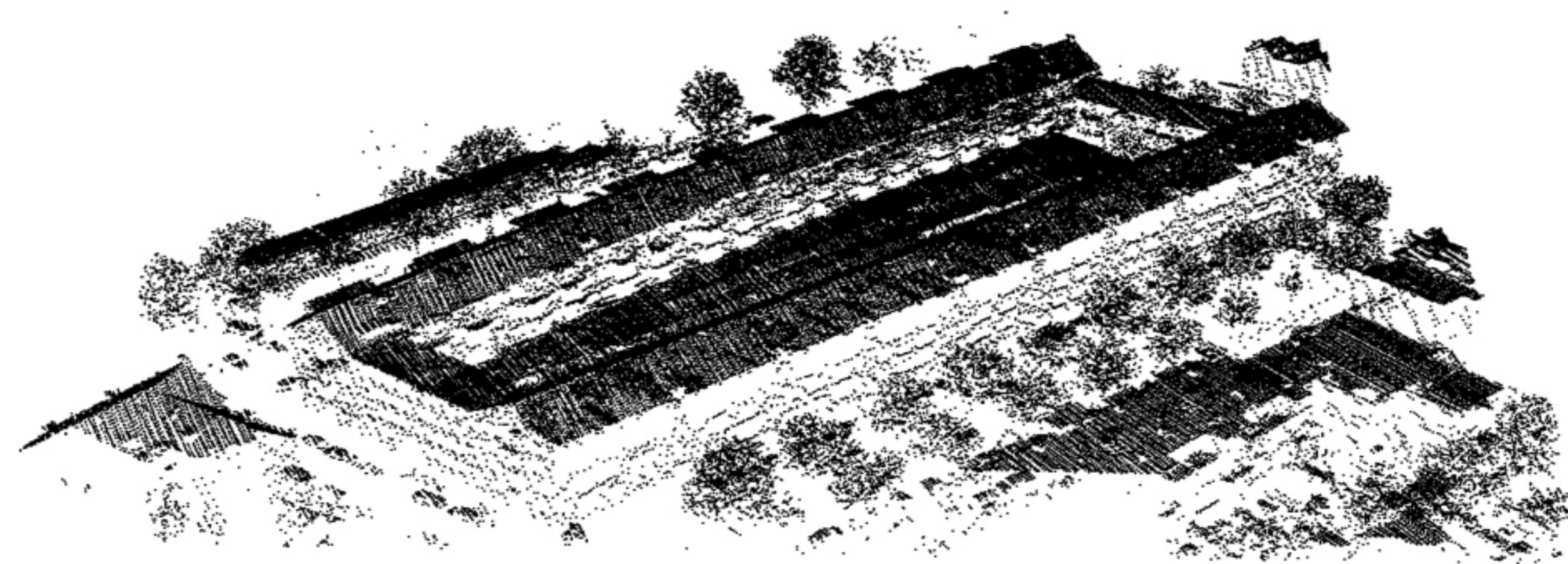


# 26-connectivity

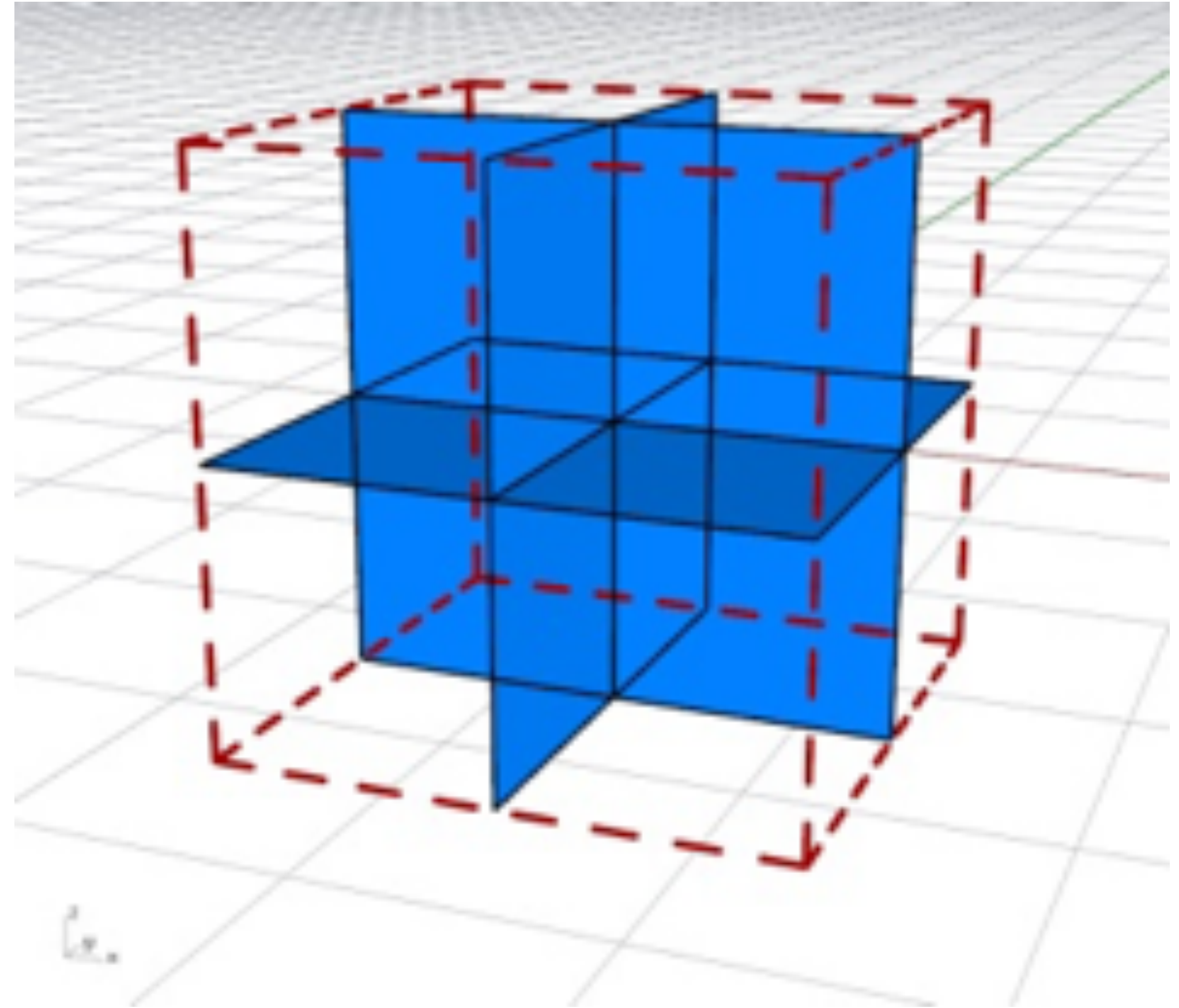
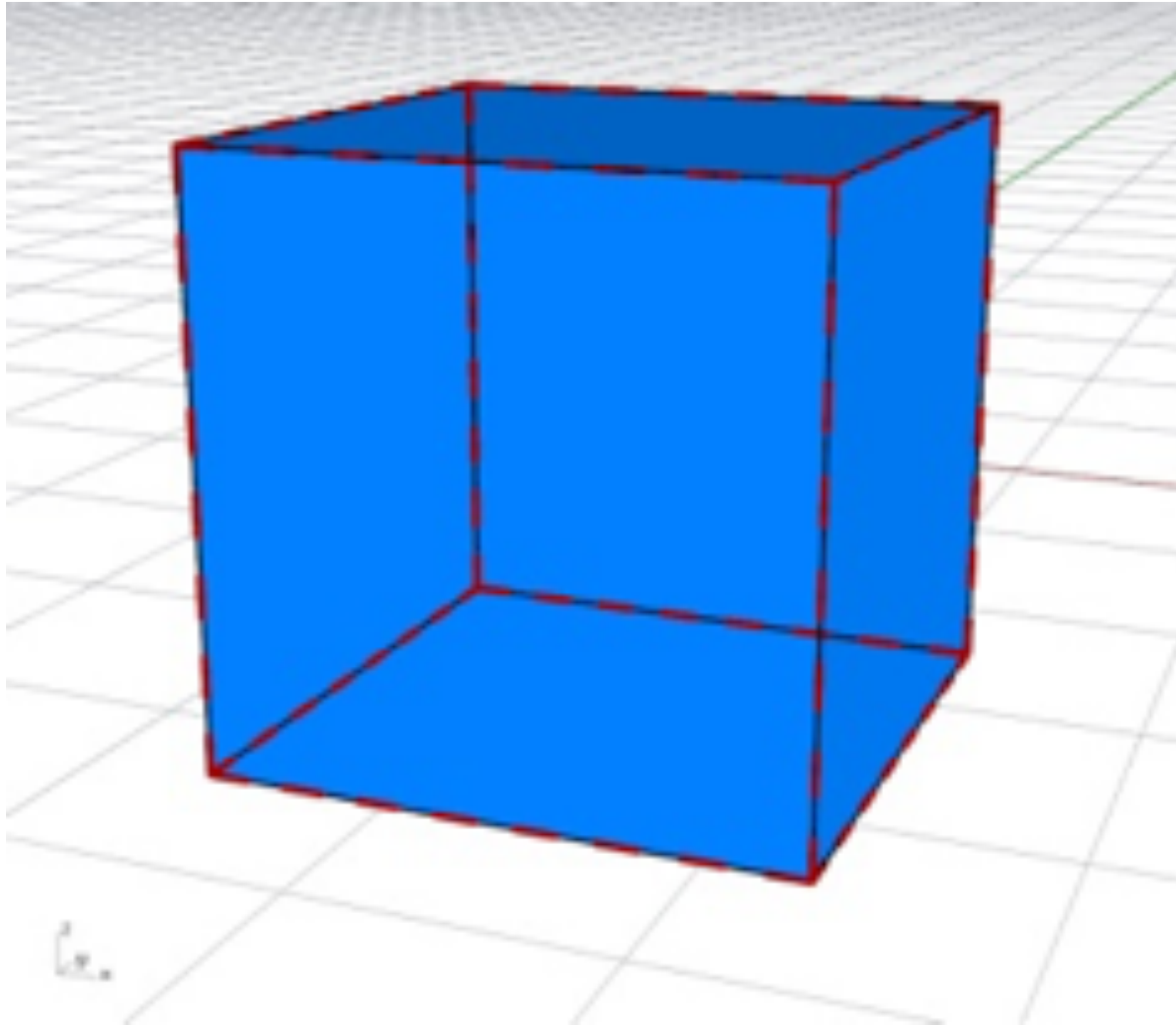




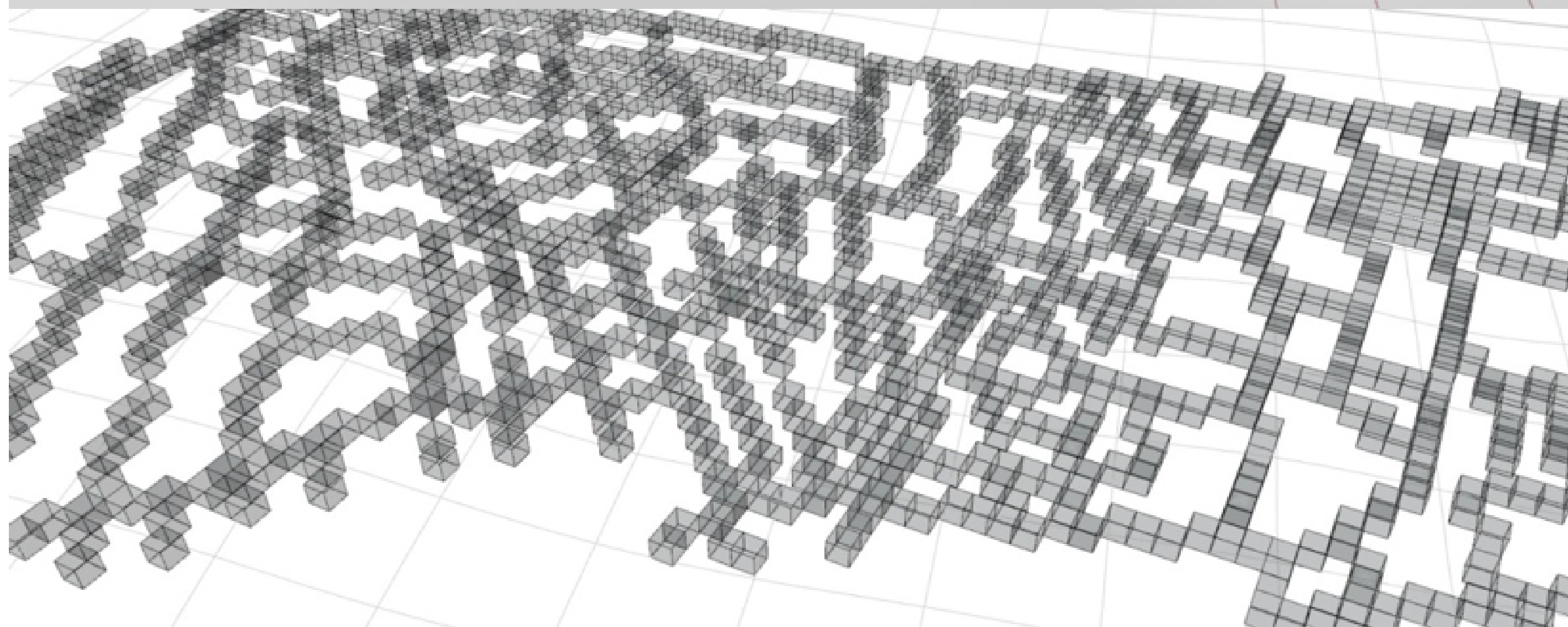
# Voxelising points



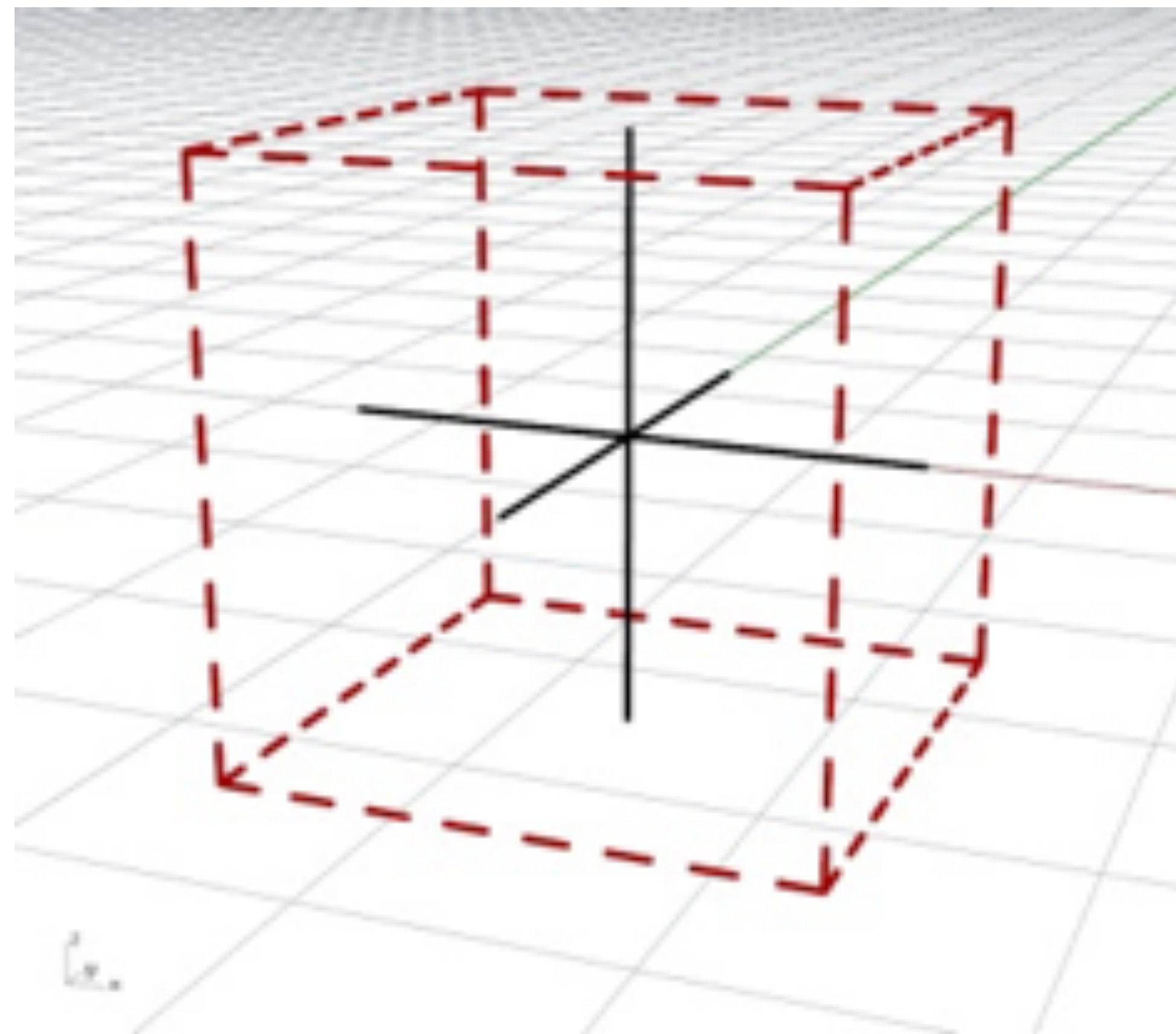
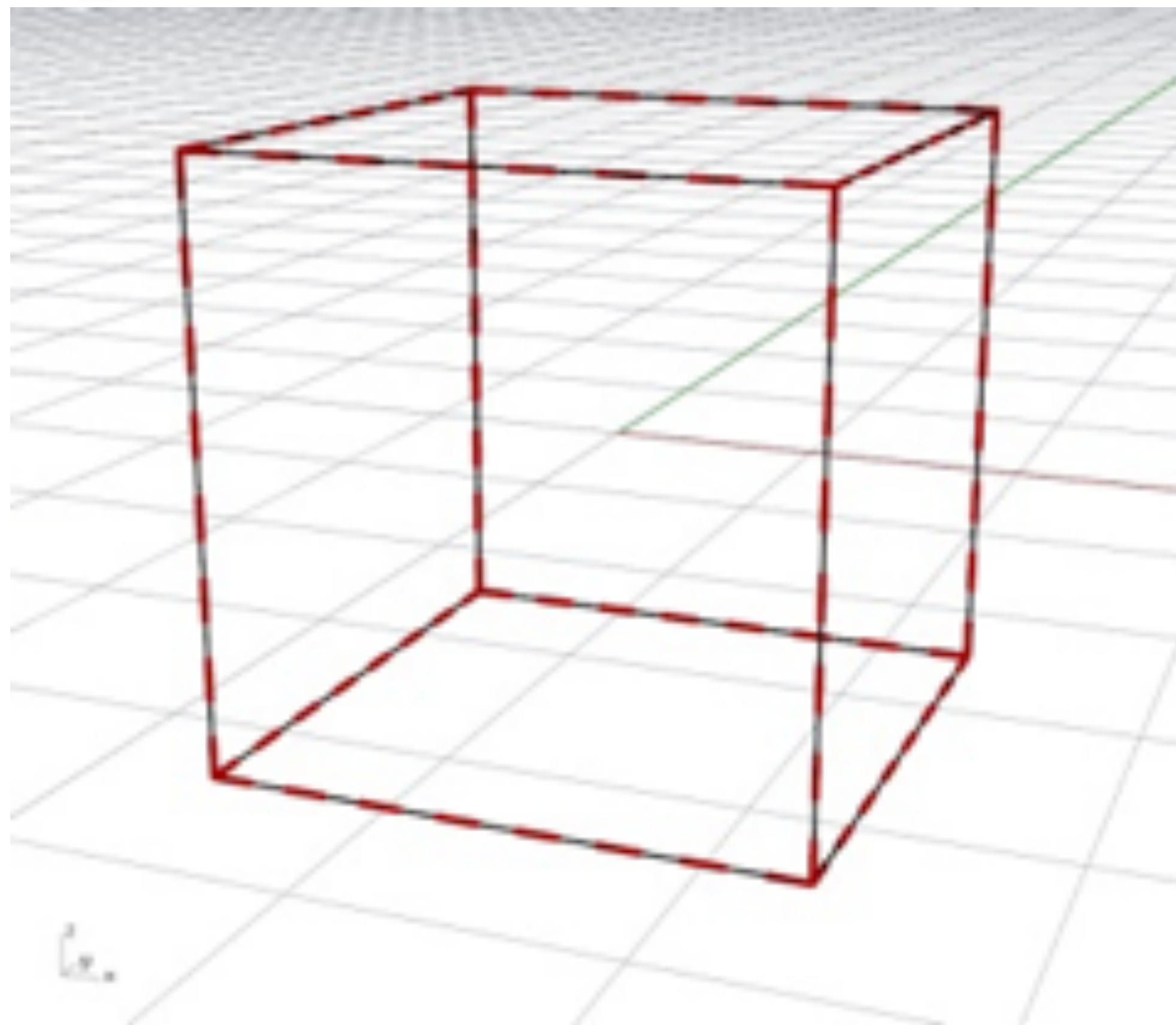
# Voxelising lines



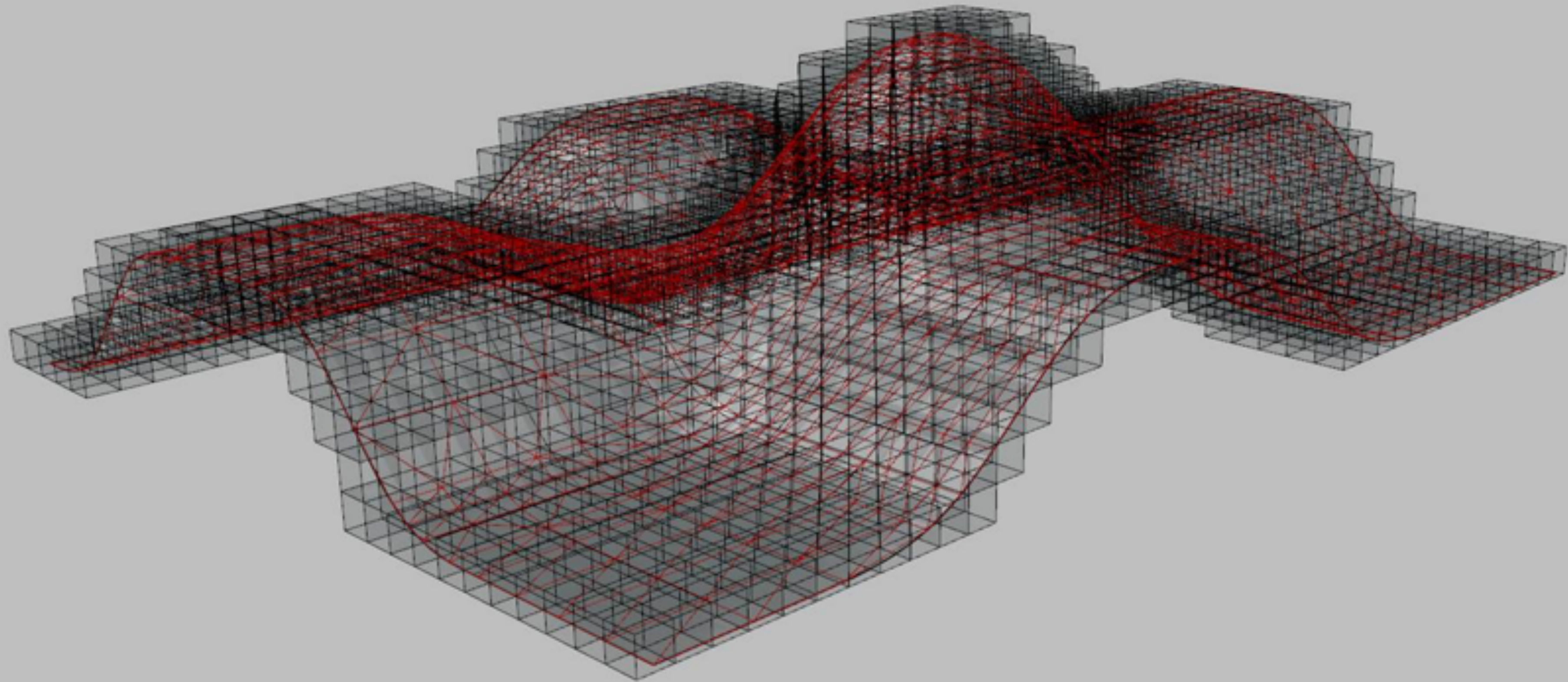
# Voxelising lines



# Voxelising surfaces



# Voxelising surfaces



Voxelising volumes?

# What to do next?

## 1. Today:

- Start with Homework 1 (triangulation of faces)
- Go to [geo1004](#) website and study today's lesson (3D book Chapter 4)
- If you have extra time: study Wednesday's lesson (3D book Chapter 3)

## 2. Wednesday: demo on 3D Voronoi and help with lessons or Hw 1

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