

GEO1016 Photogrammetry and 3D Computer Vision

#### Lecture Surface Reconstruction

Liangliang Nan



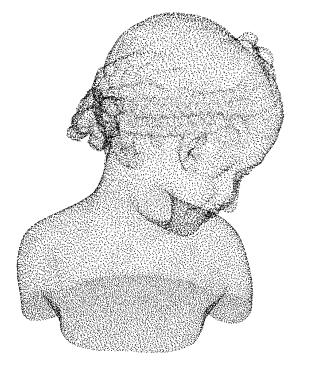
#### Outline

- Introduction
- Smooth object reconstruction
  - The pioneering work [Hoppe et al. 1992]
  - Poisson reconstruction [Kazhdan et al. 2006]
  - Piecewise smooth reconstruction
- Piecewise planar object reconstruction [Nan and Wonka. 2017]

• Data sources

Laser scanning with a turntable











- Data sources
  - Laser scanning with a hand-held scanner



- Data sources
  - Laser scanning with static laser scanner (range of 100, 200... meters)

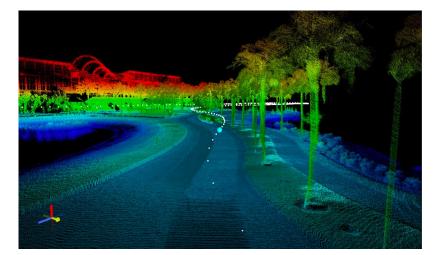


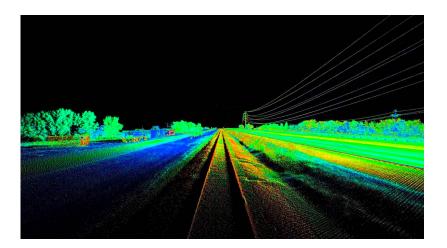




- Data sources
  - Laser scanning mobile scanners

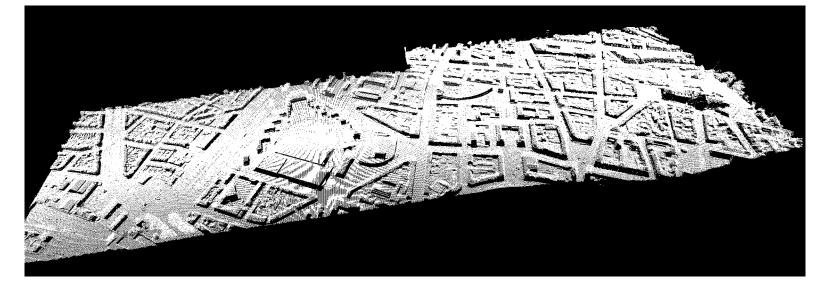


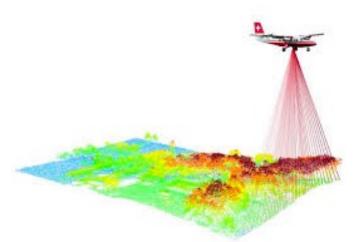






- Data sources
  - Laser scanning airborne LiDAR







- Data sources
  - Laser scanning
  - Structure from Motion (SfM) and Multi-view stereo (MVS)

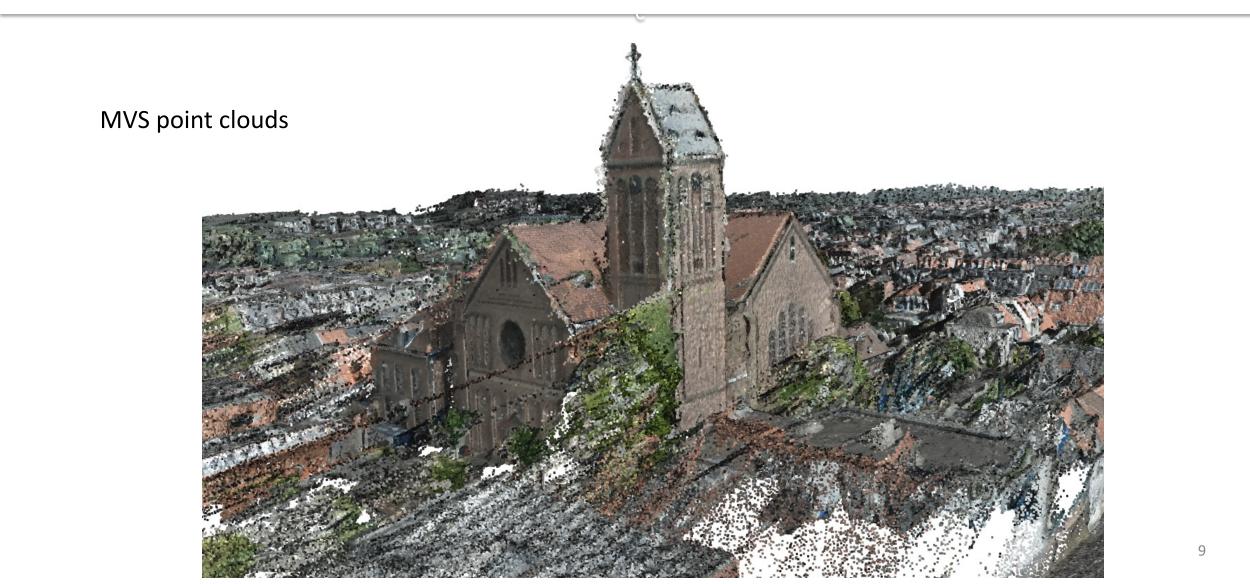






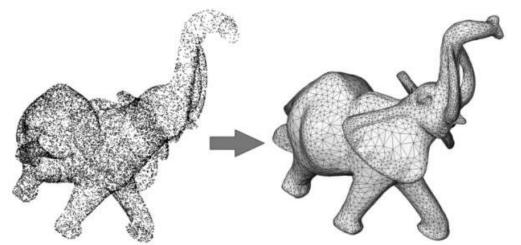




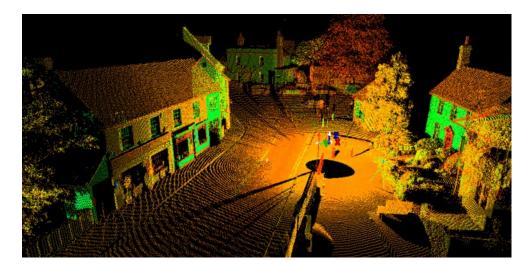




- Surface reconstruction
  - Input: point set P sampled over a surface S
    - Non-uniform sampling
    - With holes
    - With uncertainty (noise)
  - Output: surface approximating S in terms of topology and geometry
    - Desired
      - Watertight
      - Intersection free



- Challenges
  - The point samples may not be uniformly distributed
    - Oblique scanning angles
    - Laser energy attenuation

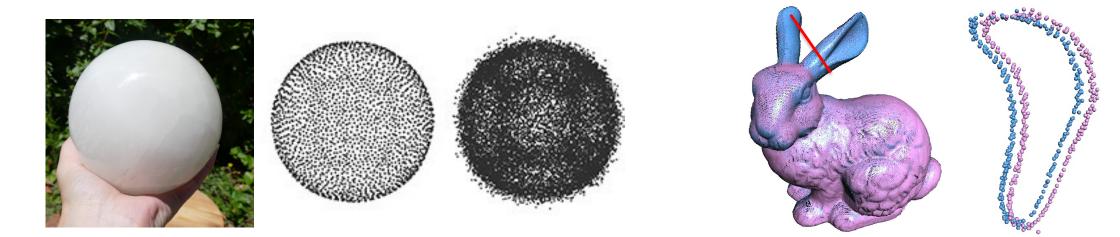








- Challenges
  - The point samples may not be uniformly distributed
  - The positions and normals are generally noisy
    - Sampling inaccuracy
    - Scan misregistration



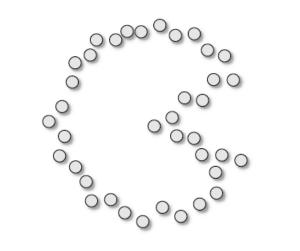


- Challenges
  - The point samples may not be uniformly distributed
  - The positions and normals are generally noisy
  - Missing data
    - Material properties, inaccessibility, occlusion, etc.



Many candidate surfaces for the reconstruction problem!

- Challenges
  - The point samples may not be uniformly distributed
  - The positions and normals are generally noisy
  - Missing data
  - Ill-posed problem





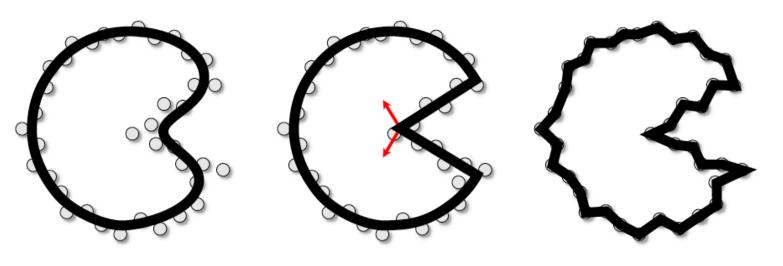


Many candidate surfaces for the reconstruction problem! 15

#### Introduction

- Challenges
  - The point samples may not be uniformly distributed
  - The positions and normals are generally noisy
  - Missing data
  - Ill-posed problem

, How to pick?





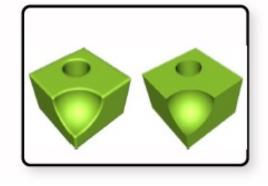
#### 16

#### **General Ideas**

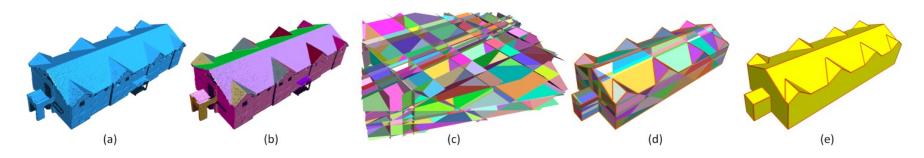
• Surface smoothness priors

- **Global Smoothness**

#### Piecewise Smoothness



• Domain-specific priors

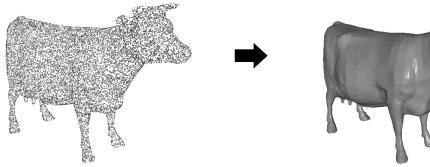


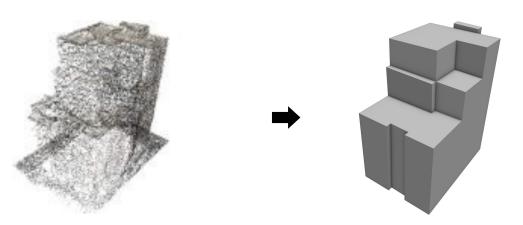
[Nan and Wonka 2017]



• Smooth surface reconstruction

• Piecewise-planar object reconstruction







#### Today's Agenda

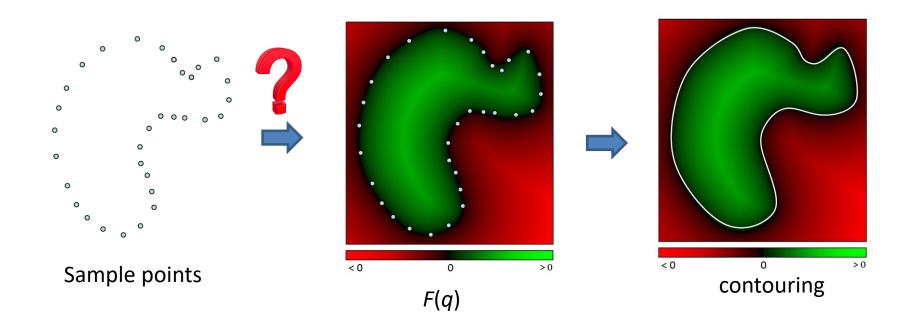
- Introduction
- Smooth object reconstruction
  - The pioneering work [Hoppe et al. 1992]
  - Poisson reconstruction [Kazhdan et al. 2006]
  - Piecewise smooth reconstruction
- Piecewise planar object reconstruction [Nan and Wonka. 2017]



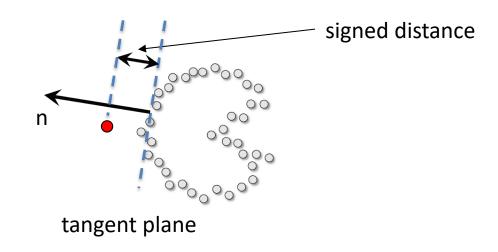




- Two main steps
  - Estimate signed geometric distance to the unknown surface
  - Extract the zero-set of the distance field using a contouring algorithm

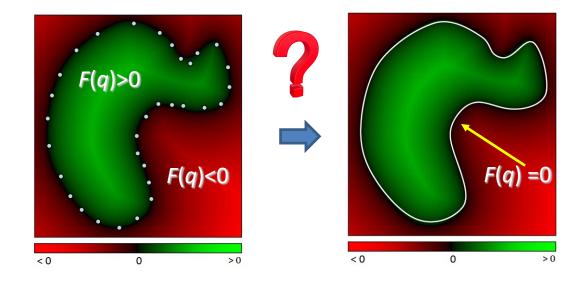


- Define a signed distance function (SDF)
  - Associate an oriented plane (tangent plane) with each of the data points
    - Tangent plane is a local linear approximation to the surface.
    - Used to define signed distance function to surface.



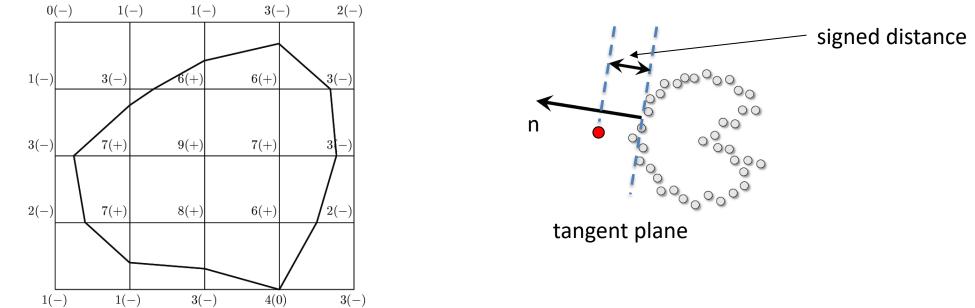


- Contour tracing
  - Extract 0-set iso-surface from the scalar field
    - Marching cubes





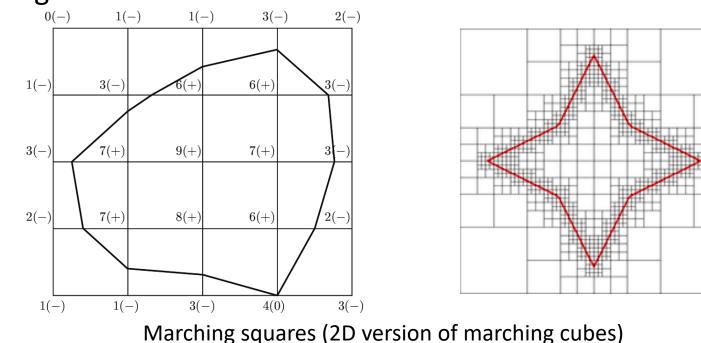
- Contour tracing
  - Extract 0-set iso-surface from the scalar field
    - Marching cubes



Marching squares (2D version of marching cubes)

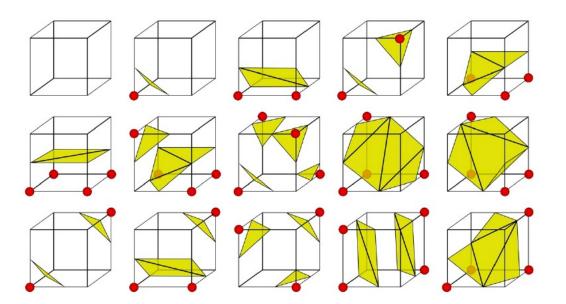


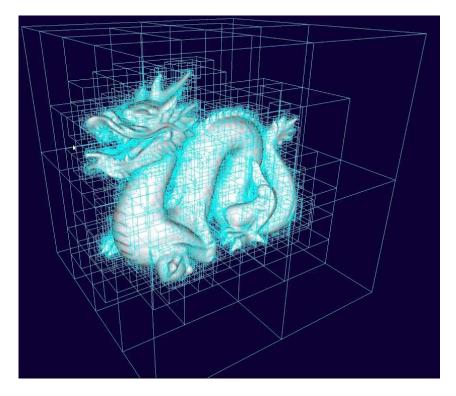
- Contour tracing
  - Extract 0-set iso-surface from the scalar field
    - Marching cubes
    - Irregular grid





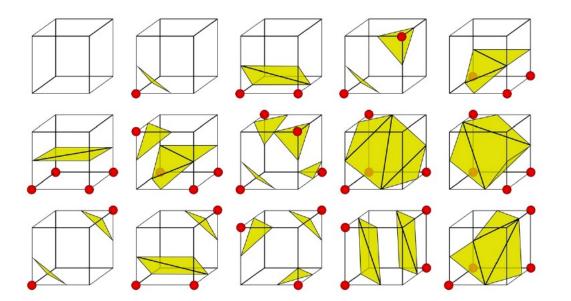
- Contour tracing
  - Extract O-set iso-surface from the scalar field
  - Marching cubes

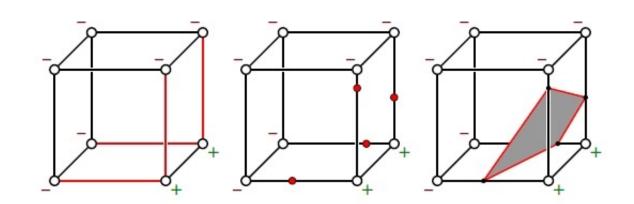






- Contour tracing
  - Extract 0-set iso-surface from the scalar field
  - Marching cubes

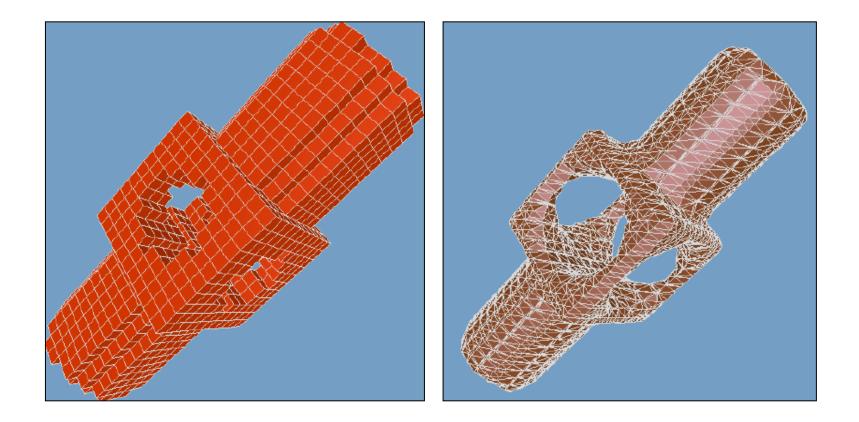




Marching cubes

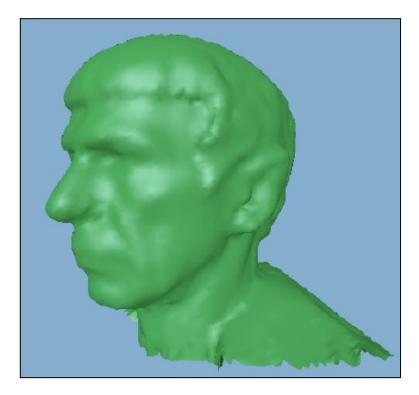


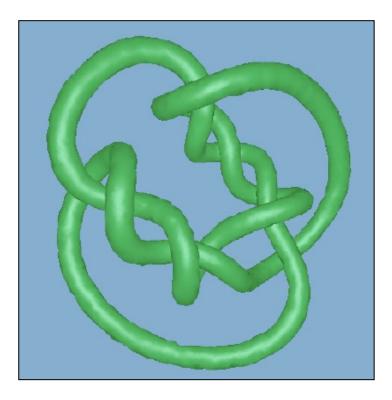
• Contour tracing





• Reconstruction results



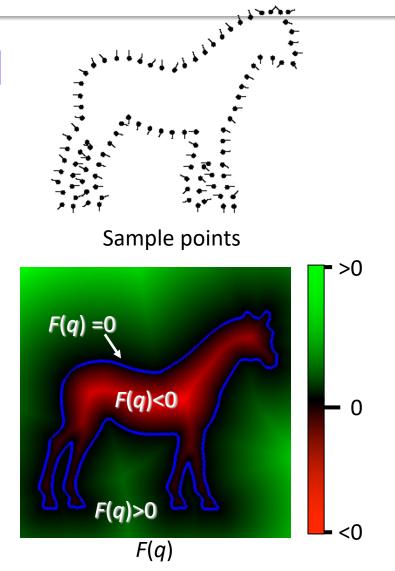




#### Outline

- Introduction
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  - Poisson reconstruction [Kazhdan et al. 2006]
  - Piecewise smooth reconstruction
- Piecewise planar object reconstruction [Nan and Wonka. 2017]

- Inherited idea from [Hoppe et al. 1992]
- Discrete SDF -> Implicit function fitting
  - Define a 3D scalar function
    - Zero values at the points
    - Positive values outside
    - Negative values inside
  - Extract the zero isosurface

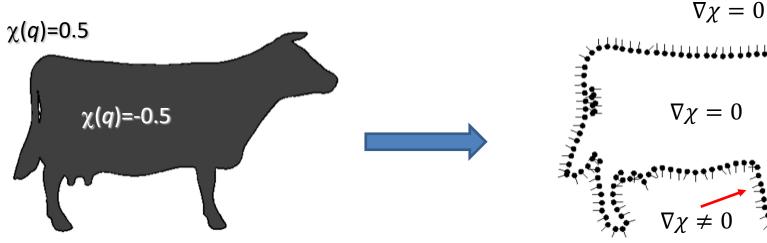


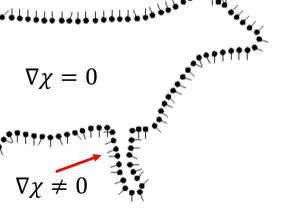


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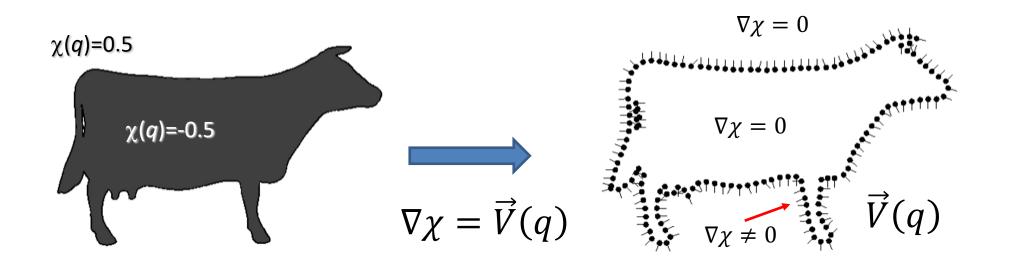
- The idea
  - The indicator function ( $\chi$ )
    - Interior: a constant negative value
    - Exterior: a constant positive value
  - The gradient of the indicator function  $(\nabla \chi)$ 
    - Zero everywhere except close to the boundary





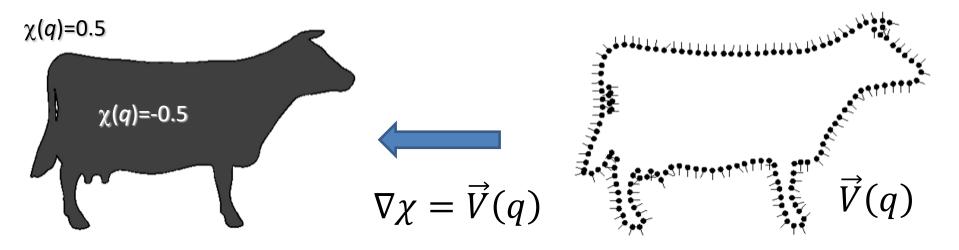


- The idea
  - The indicator function ( $\chi$ )
  - The gradient of the indicator function  $(\nabla \chi)$
  - Oriented points  $\vec{V}(q) \approx$  discretization of gradient of indicator function



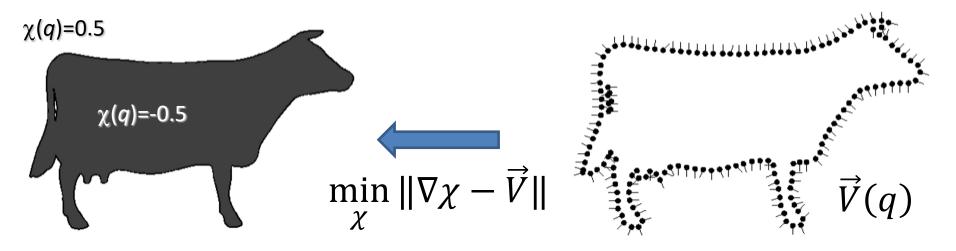


- The idea
  - The indicator function ( $\chi$ )
  - The gradient of the indicator function  $(\nabla \chi)$
  - Oriented points  $\vec{V}(q) \approx$  discretization of gradient of indicator function
  - Reconstruction

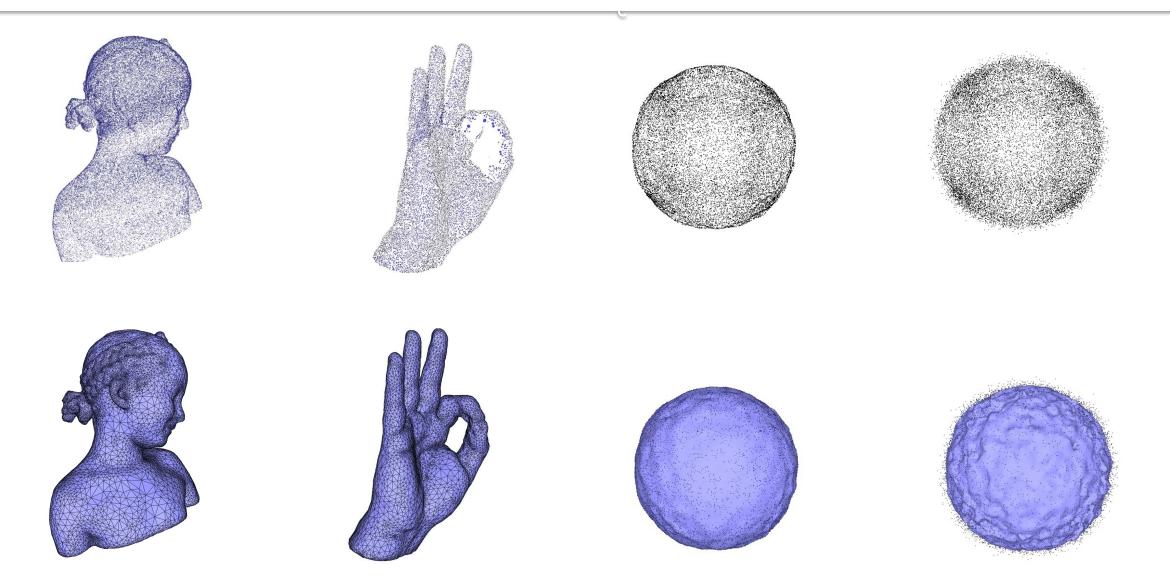




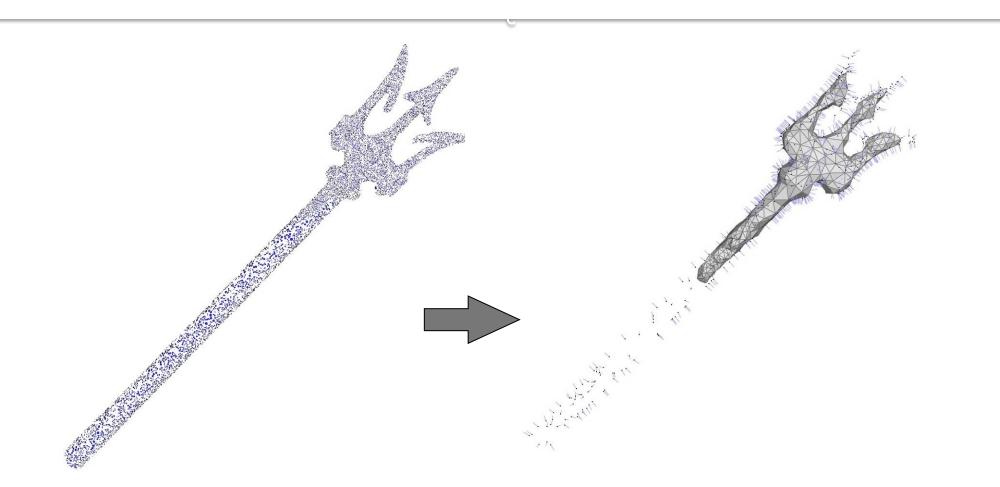
- The idea
  - The indicator function ( $\chi$ )
  - The gradient of the indicator function  $(\nabla \chi)$
  - Oriented points  $\vec{V}(q) \approx$  discretization of gradient of indicator function
  - Reconstruction: finding the indicator function + iso-surface extraction









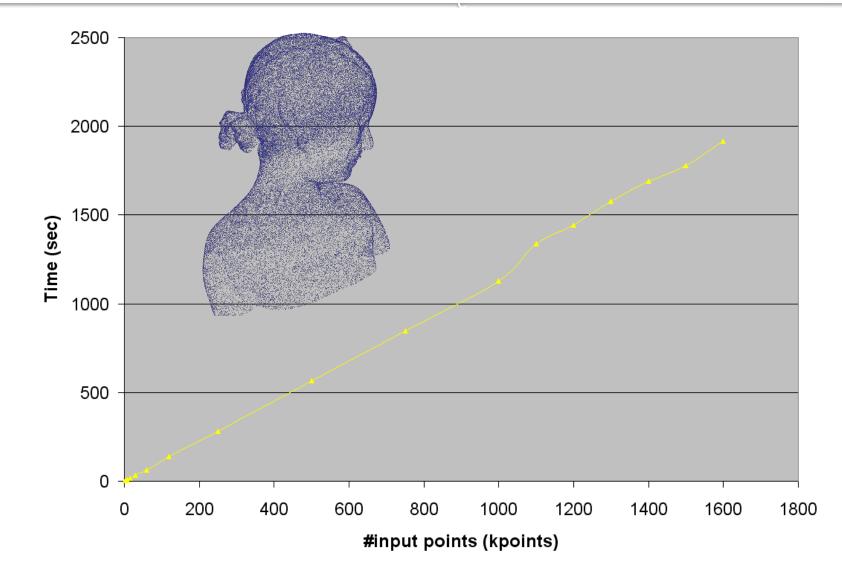


Left: 50K points sampled on Neptune trident

Right: point set simplified to 1K then reconstructed

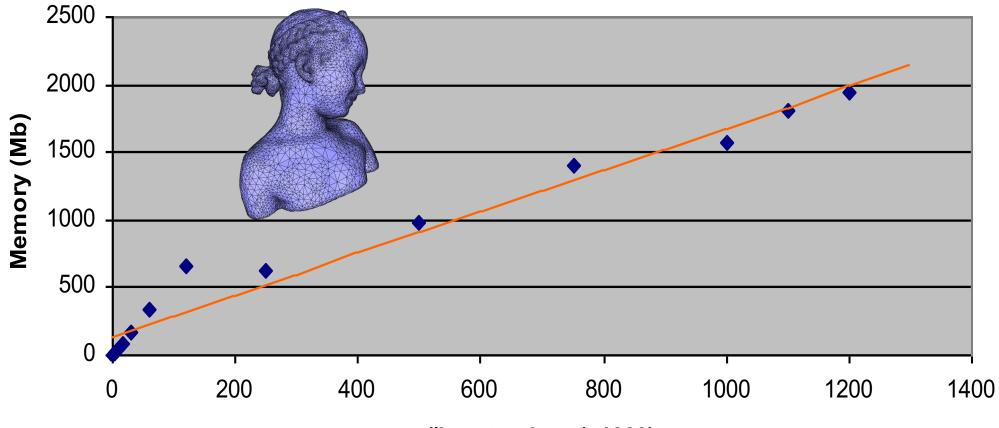


#### Poisson duration wrt #input points



#### Memory wrt #input points



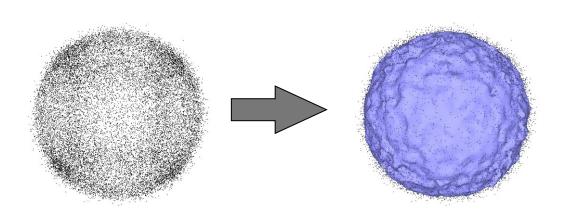


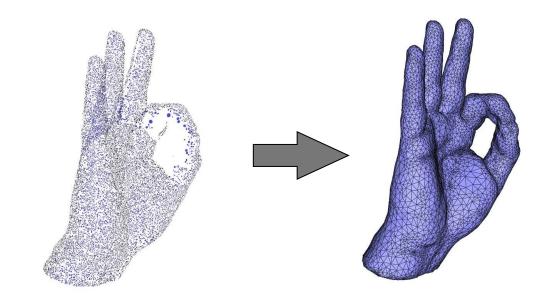
#input points (x1000)

#### **Poisson Reconstruction**



- Properties
  - ✓ Supports noisy, non-uniform data
  - ✓ Can fill reasonably large holes

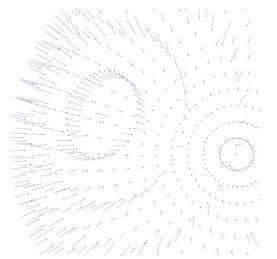


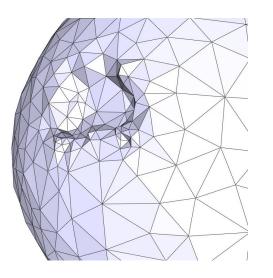


#### **Poisson Reconstruction**



- Properties
  - ✓ Supports noisy, non-uniform data
  - ✓ Can fill reasonably large holes
- Limitations
  - It requires good normal information

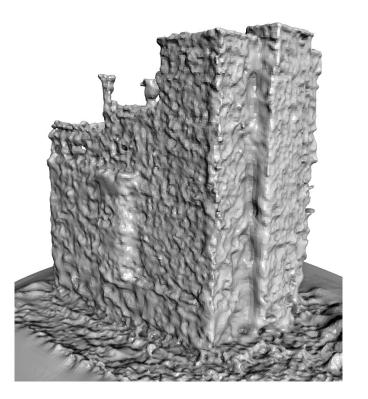




#### **Poisson Reconstruction**



- Properties
  - ✓ Supports noisy, non-uniform data
  - ✓ Can fill reasonably large holes
- Limitations
  - It requires good normal information
  - Sharp features are oversmoothed
    - Not good for piecewise planar objects





#### Outline

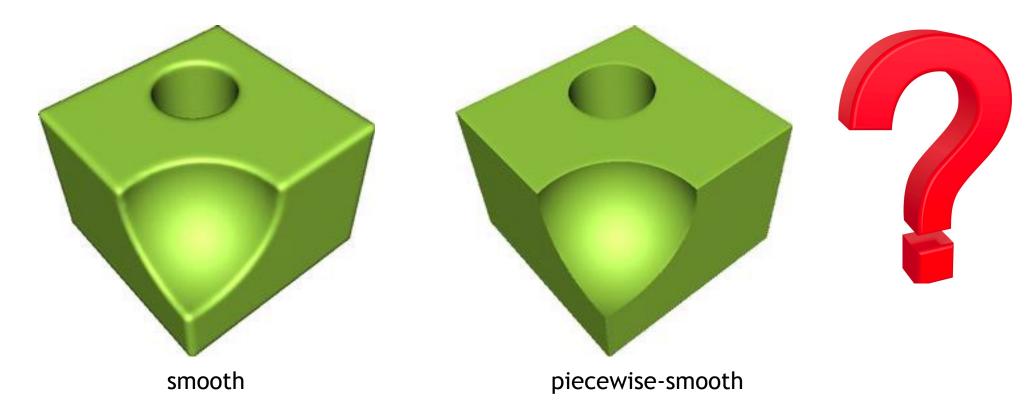
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- Smooth object reconstruction
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  - Poisson reconstruction [Kazhdan et al. 2006]
  - Piecewise smooth reconstruction





#### **Piecewise Smooth Reconstruction**

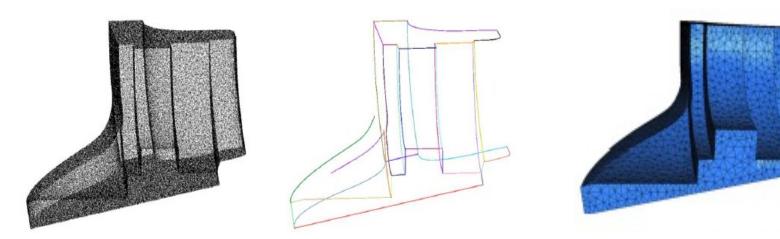
• Piecewise-smooth





### **Piecewise Smooth Reconstruction**

- Feature detection
  - Extract a set of sharp features
  - Decompose the point cloud into smooth patches
- Smooth reconstruction patch by patch
- Stitch the patches





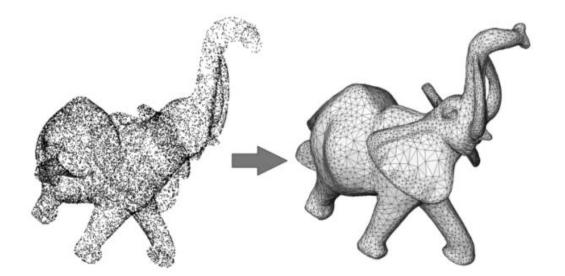
### Outline

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  - Poisson reconstruction [Kazhdan et al. 2006]
  - Piecewise smooth reconstruction
- Piecewise planar object reconstruction





- Surface Reconstruction Methods
  - Smooth surfaces
    - Fit noisy data; robust to non-uniform distribution; fill (small) holes



Poisson Surface Reconstruction [Kazhdan et al. 06]

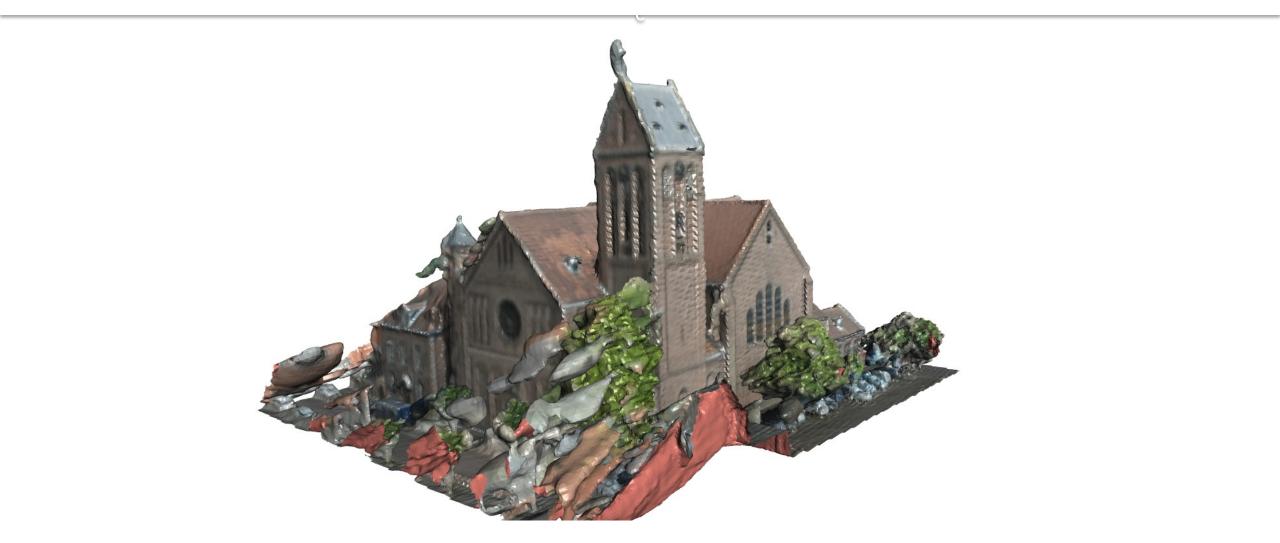


- Surface Reconstruction Methods
  - Smooth surfaces
  - Piecewise planar objects



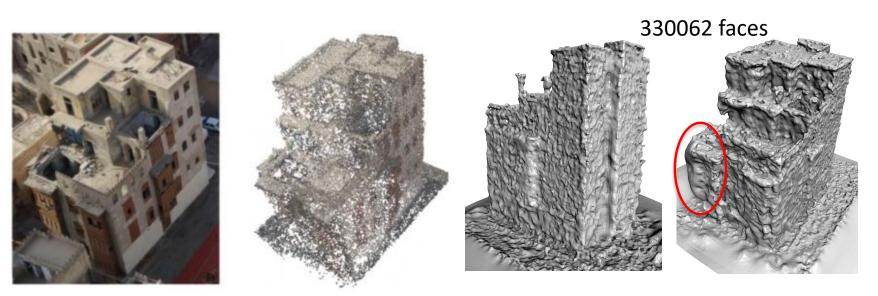








- Surface Reconstruction Methods
  - Smooth surfaces
  - Piecewise planar objects



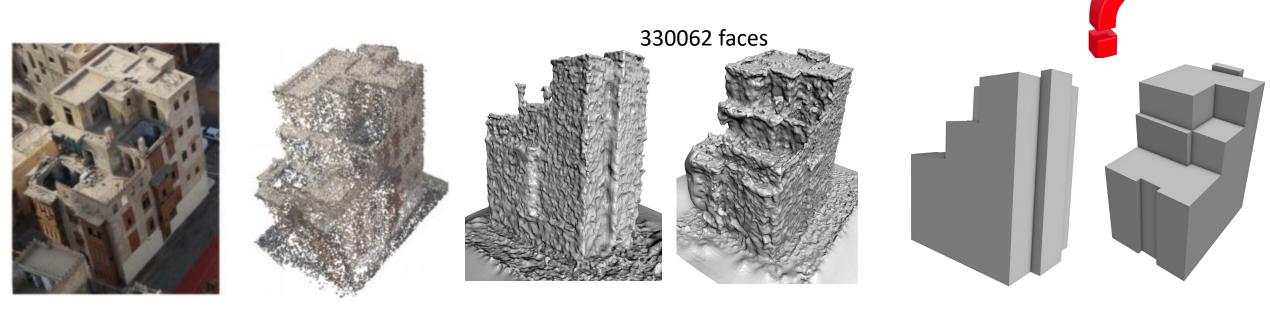
Unsatisfied results

- Bumpy
- Large number of faces
- Unacceptable hole filling
- Rare direct applications
  - Post-processing required
    - Topologically correct
    - Simplified

Result of [Kazhdan et al. 06]



- Surface Reconstruction Methods
  - Smooth surfaces
  - Piecewise planar objects

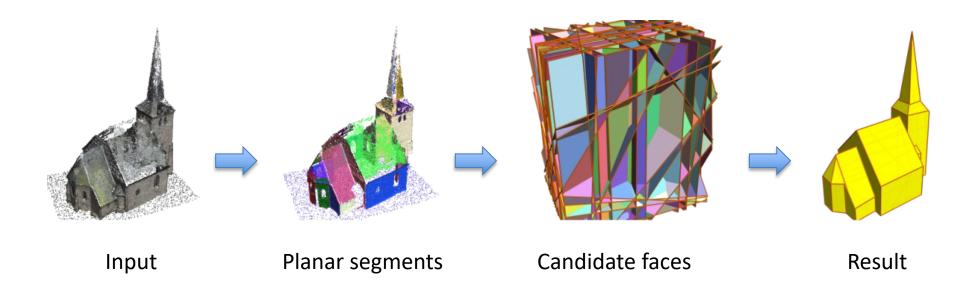


Result of [Kazhdan et al. 06]

[Nan and Wonka 17]

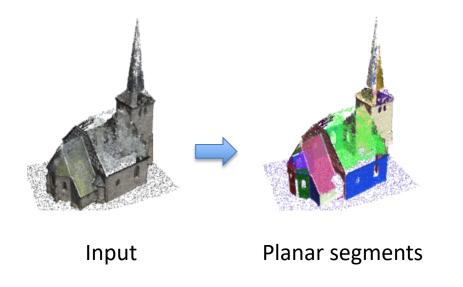


• Overview





• Plane extraction

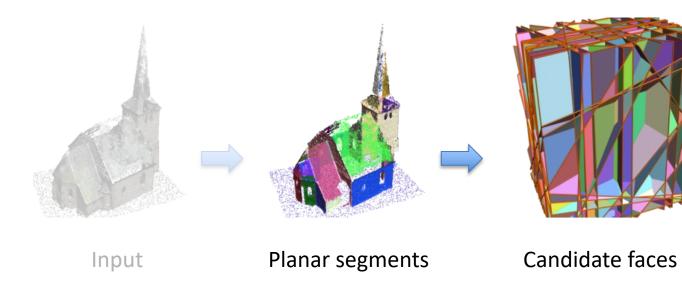


#### **RANSAC** algorithm

- Random 3 points -> plane
- Scoring, accept or reject
- Repeat
  - Plane from the remaining points
  - Stop if no plane can be extracted

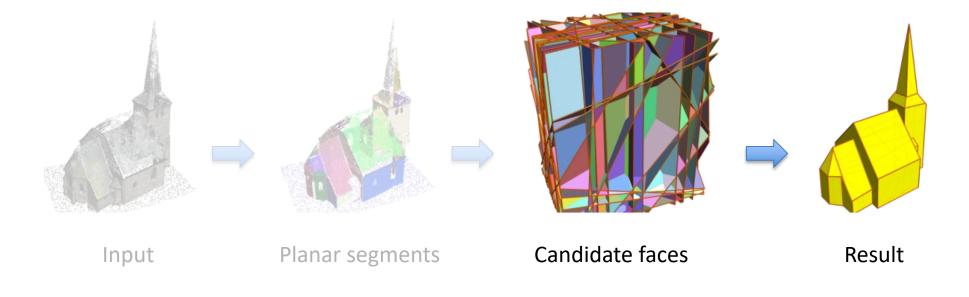


- Candidate generation
  - Supporting plane clipping
  - Pairwise intersection



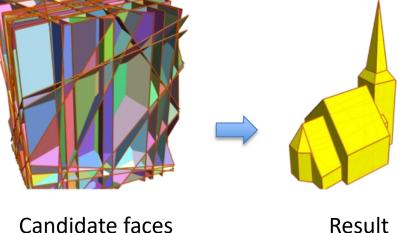


• Face selection





- Face selection
  - Labeling problem
  - Linear integer program



*N* candidate faces  $F = \{f_i | 1 \le i \le N\}$ Variables:  $x_i = \begin{cases} 1, & \text{face } f_i \text{ will be chosen} \\ 0, & \text{face } f_i \text{ will } \mathbf{not} \text{ be chosen} \end{cases}$ 

Result



- Objective function
  - Data fitting
    - Favors selecting faces with more support
    - Percentage of unused points

$$E_f = 1 - \frac{1}{|P|} \sum_{i=1}^{N} x_i \cdot support(f_i)$$



- Objective function
  - Data fitting
    - Favors selecting faces with more support
    - Percentage of unused points

$$E_f = 1 - \frac{1}{|P|} \sum_{i=1}^{N} x_i \cdot support(f_i)$$

 $\begin{array}{ll} \text{Confidence weighted} & support(f) = \sum_{p,f \mid dist(p,f) < \varepsilon} (1 - \frac{dist(p,f)}{\varepsilon}) \cdot conf(p) \end{array}$ 



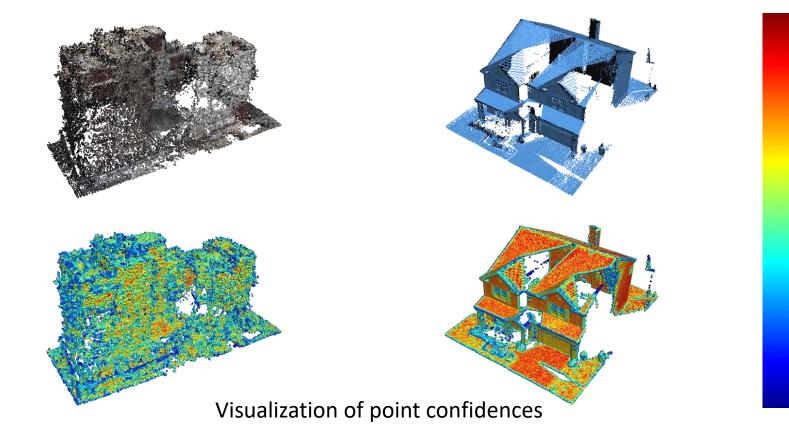
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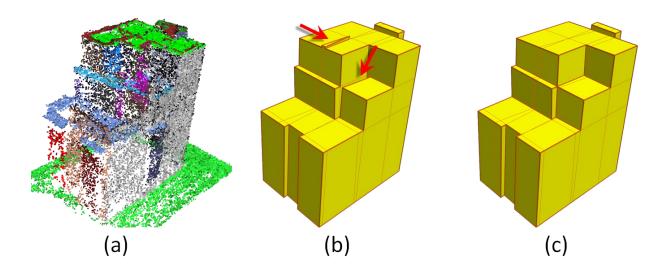


- Objective function
  - Data fitting



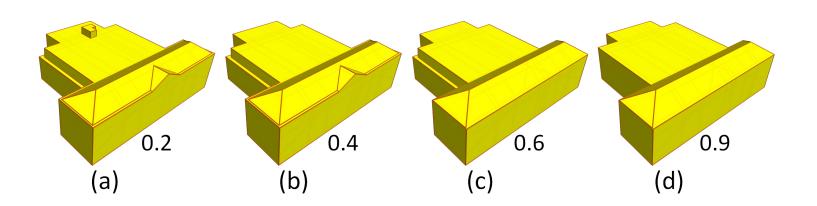


- Objective function
  - Data fitting
  - Model complexity
    - Penalize sharp corners





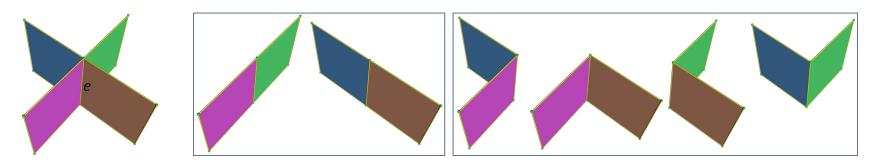
- Objective function
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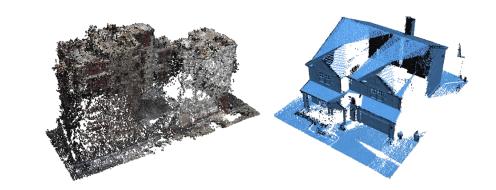
- Objective function
  - Data fitting
  - Model complexity
    - Penalize sharp corners

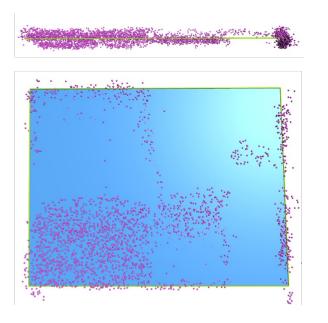
$$E_m = \frac{1}{|E|} \sum_{i=1}^{|E|} corner(e_i)$$





- Objective function
  - Data fitting
  - Model complexity
  - Point coverage









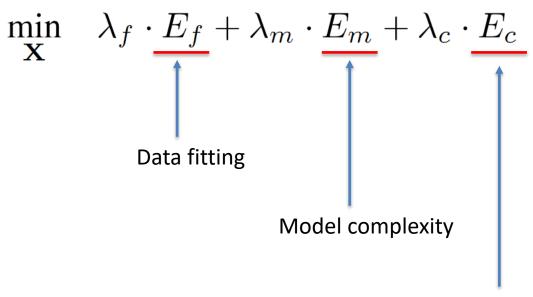
- Objective function
  - Data fitting
  - Model complexity
  - Point coverage

$$E_{c} = \frac{1}{area(M)} \sum_{i=1}^{N} x_{i} \cdot (area(f_{i}) - area(M_{i}^{\alpha})),$$

$$\bigcup_{0.93} \bigcup_{0.65} \bigcup_{0.$$

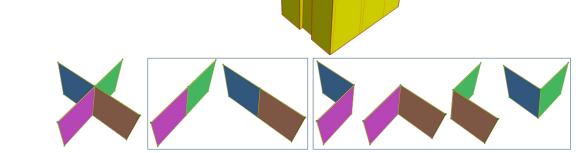


- Face selection
  - Linear integer program





- Face selection
  - Linear integer program
    - Constraints
      - Watertight
      - Manifold



 $\min_{\mathbf{X}} \quad \lambda_f \cdot E_f + \lambda_m \cdot E_m + \lambda_c \cdot E_c$ 

s.t. 
$$\begin{cases} \sum_{j \in \mathcal{N}(e_i)} x_j = 2 \text{ or } 0, & 1 \le i \le |E| \\ x_i \in \{0, 1\}, & 1 \le i \le N \end{cases}$$

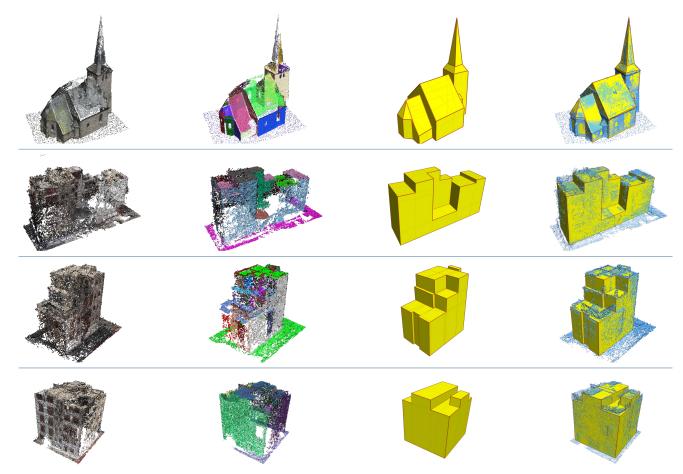


- Face selection
  - Linear integer program
    - Constraints
    - Solvers (SCIP, CBC, GLPK, Gurobi...)

$$\begin{split} \min_{\mathbf{X}} \quad \lambda_f \cdot E_f + \lambda_m \cdot E_m + \lambda_c \cdot E_c \\ \text{s.t.} \quad \begin{cases} \sum_{j \in \mathcal{N}(e_i)} x_j = 2 \quad \text{or} \quad 0, \quad 1 \leq i \leq |E| \\ x_i \in \{0, 1\}, \quad 1 \leq i \leq N \end{cases} \end{split}$$

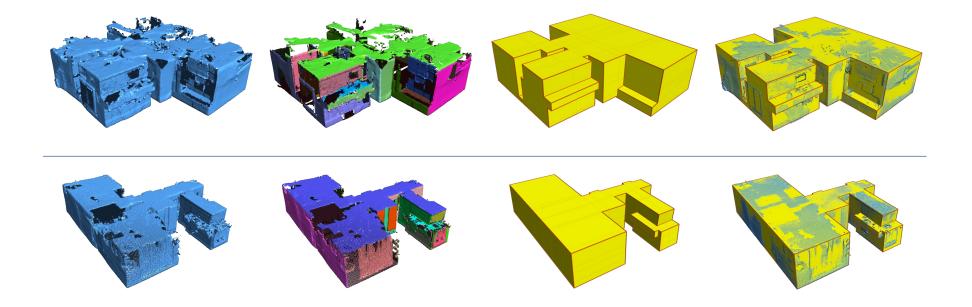


• Reconstruction results





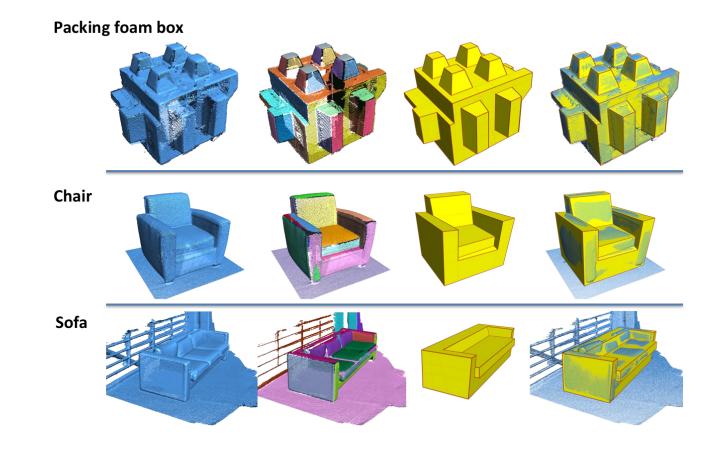
• Reconstruction results



#### Dn **fu**Delft 3Dgeoinfo

#### **Piecewise Planar Reconstruction**

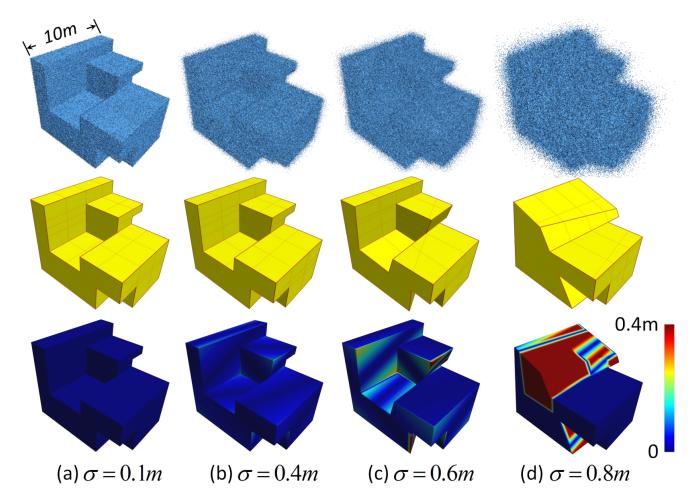
• Reconstruction results





#### **Piecewise Planar Reconstruction**

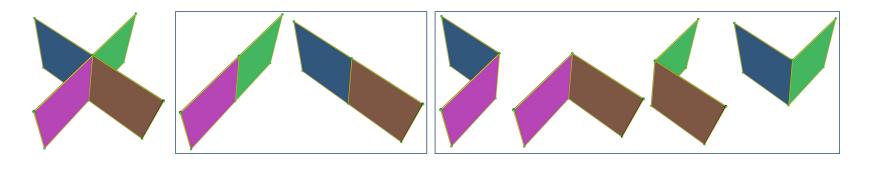
• Robustness to noise



#### Limitations



• Open surfaces

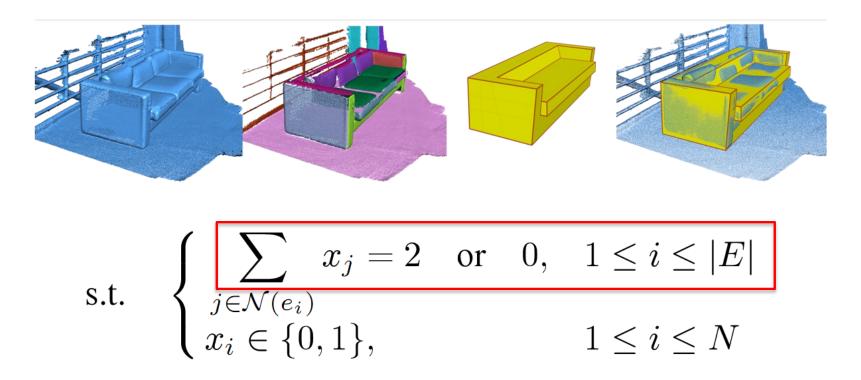


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#### **TUDelft** 3Dgeoinfo

#### Limitations

• Open surfaces



#### Limitations

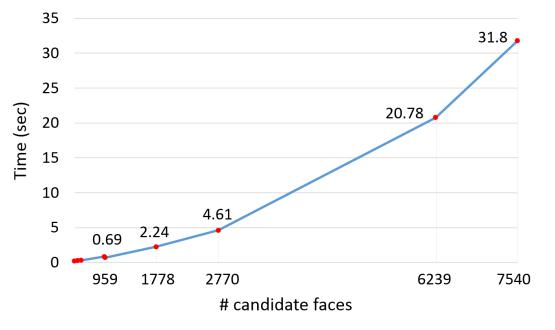


- Open surfaces
- Finer surface details
  - Fence
  - Façade decorations
  - Door handle



#### Limitations

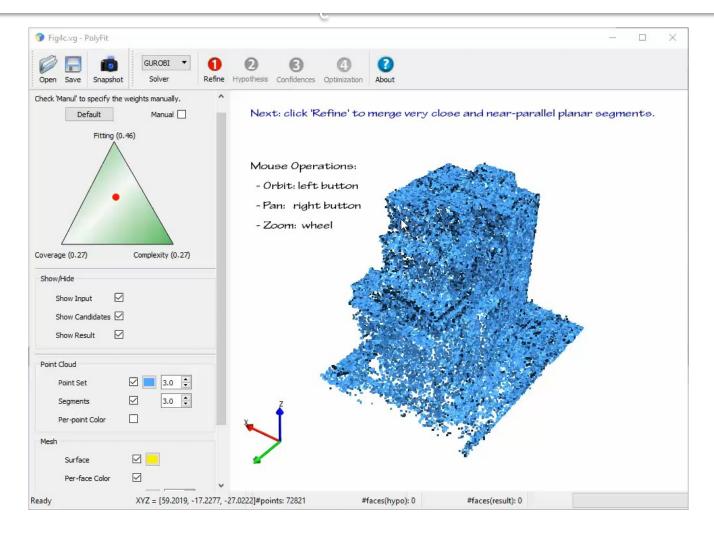
- Open surfaces
- Finer surface details
- Complexity of the algorithm







• Demo



Source Code (in C++) <a href="https://github.com/LiangliangNan/PolyFit">https://github.com/LiangliangNan/PolyFit</a>



#### Next

- Feedback on the assignments
- Example questions (for the final exam)