

Learning Stereo

Nail Ibrahimli

What are these characters having in common?



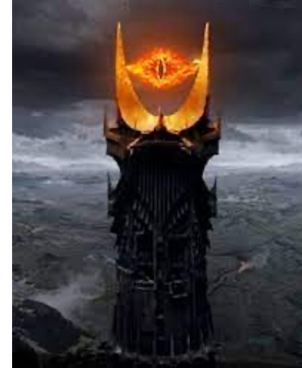
Cyclope
(Greek)



Hitotsume-kozō
(Japanese)



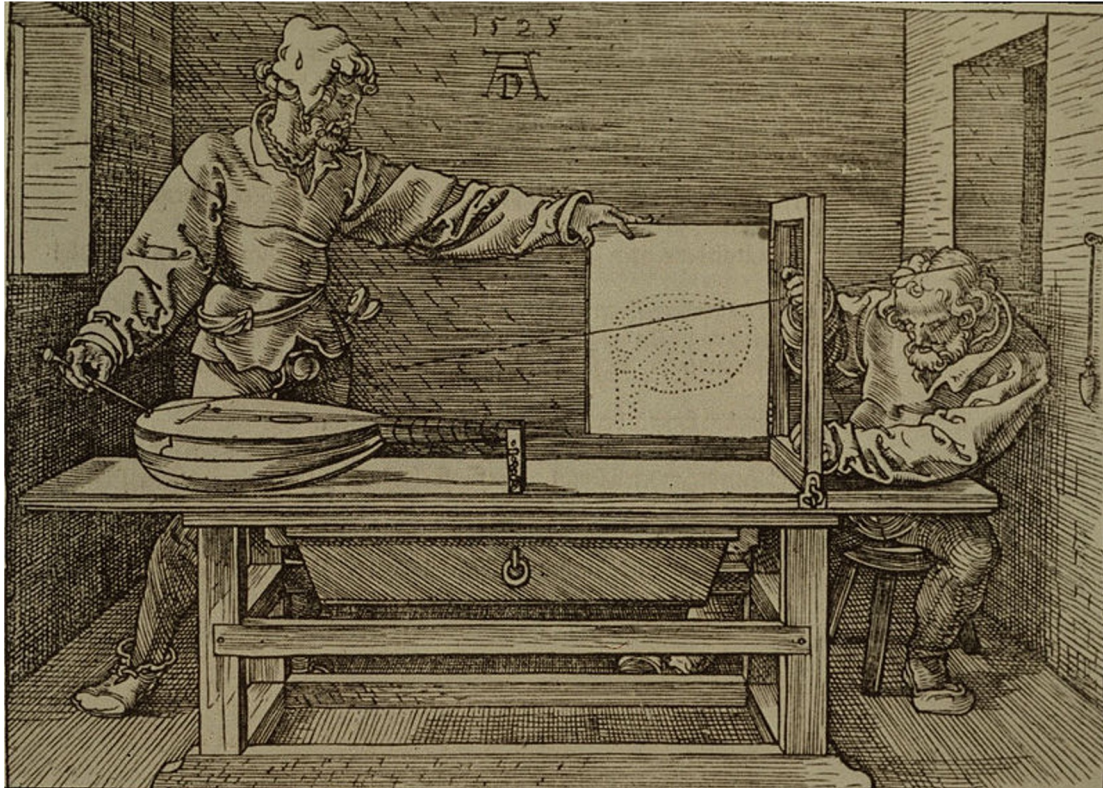
Tepegöz
(Turkic)



Eye of Sauron
(LOTR)



Imaging geometry of single eye (camera)



Albrecht Durer (Pinhole)

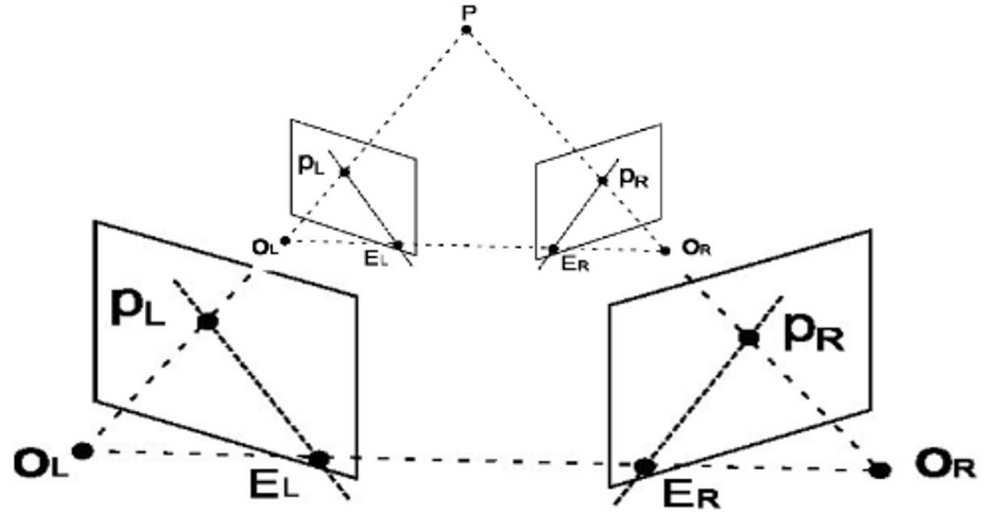


M.C. Escher (Omni-directional)

Limitations of single eye



Limitations of single eye



Limitations of single eye



M.C. Escher



Internet

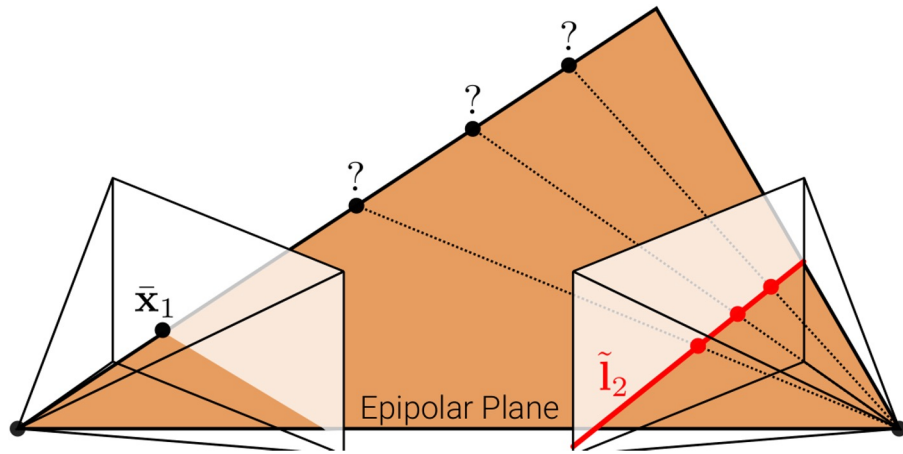
Why do we have two eyes?



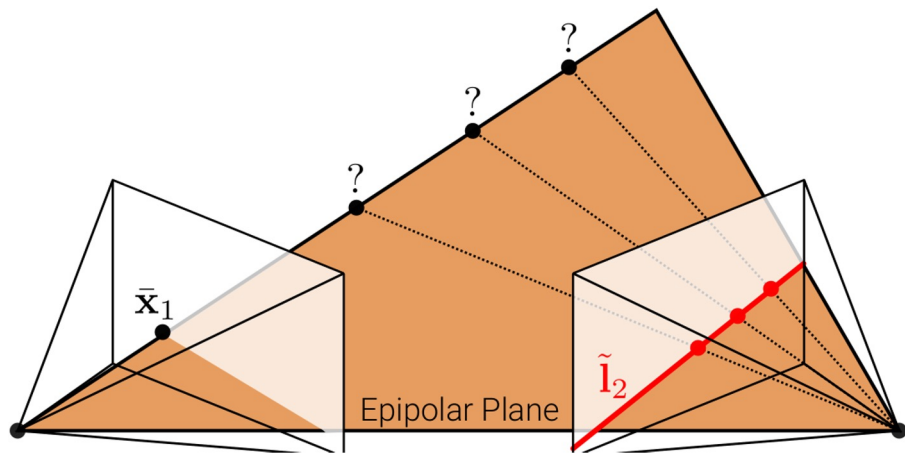
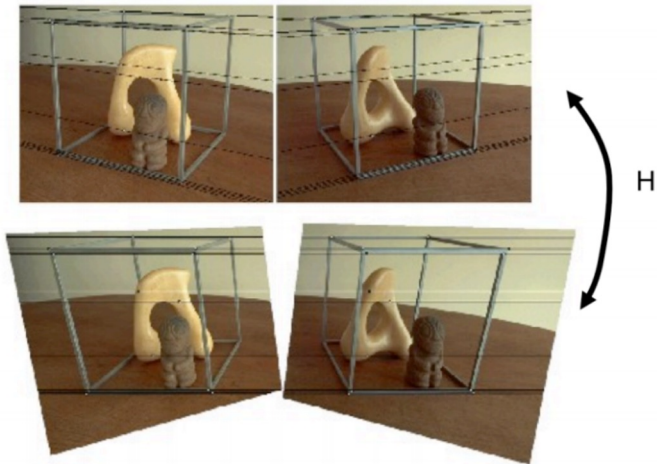
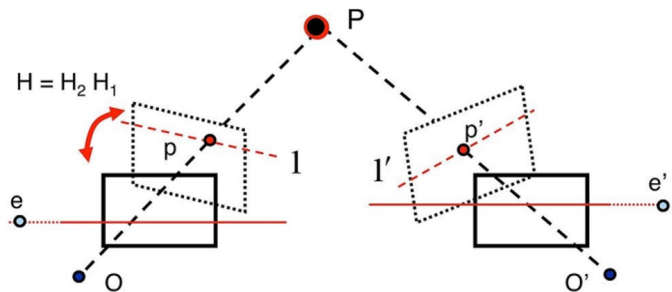
Pan's Labyrinth



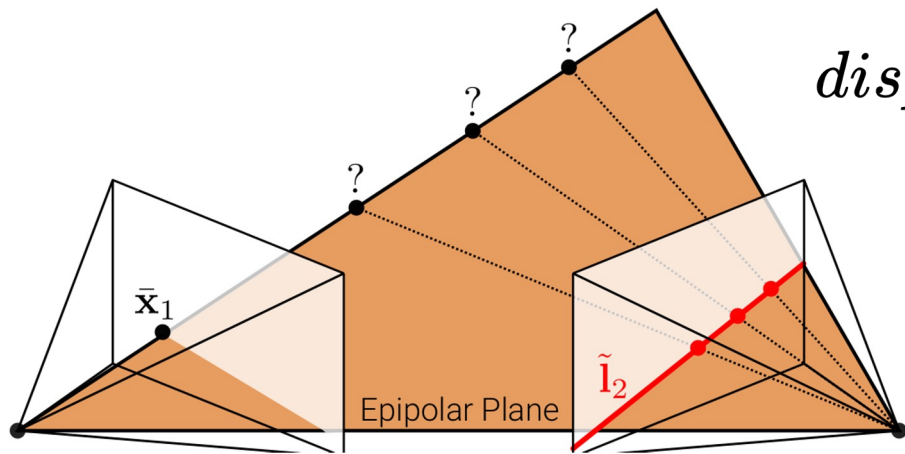
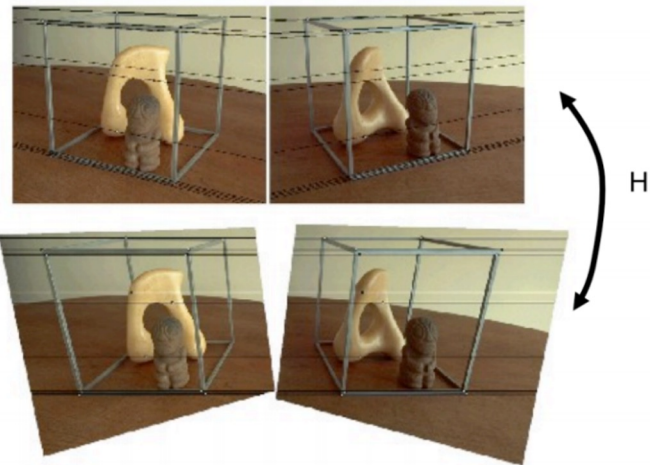
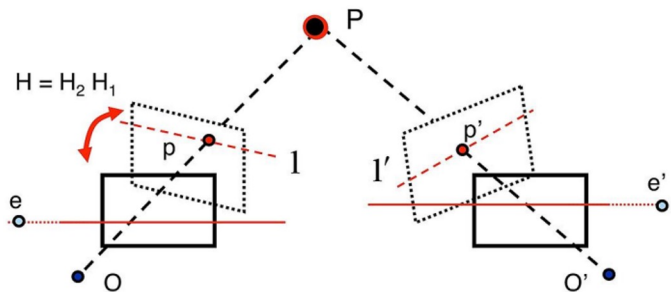
Why do we have two eyes?



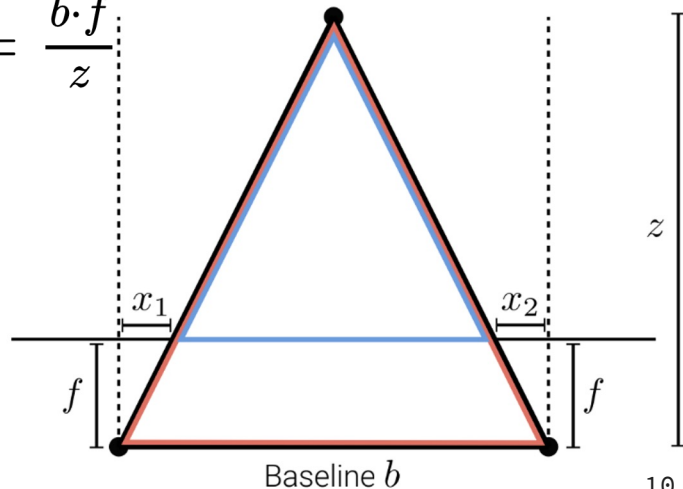
Why do we have two eyes?



Why do we have two eyes?



$$\text{disparity} = \frac{b \cdot f}{z}$$



Triangulation

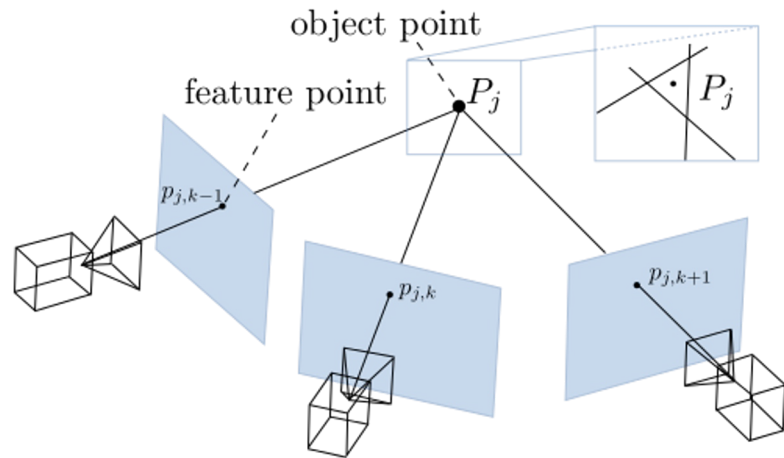
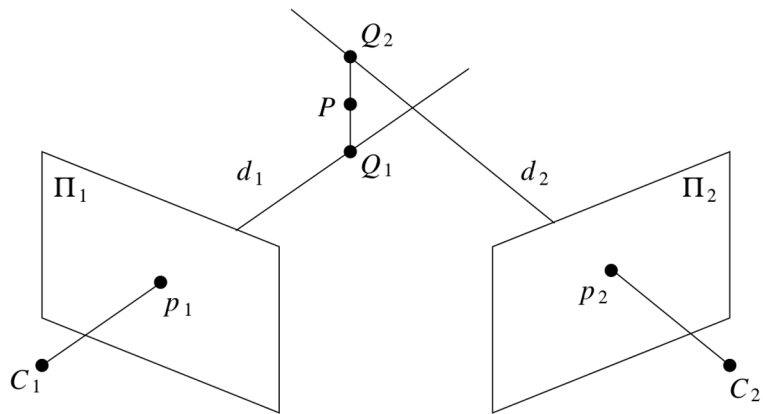
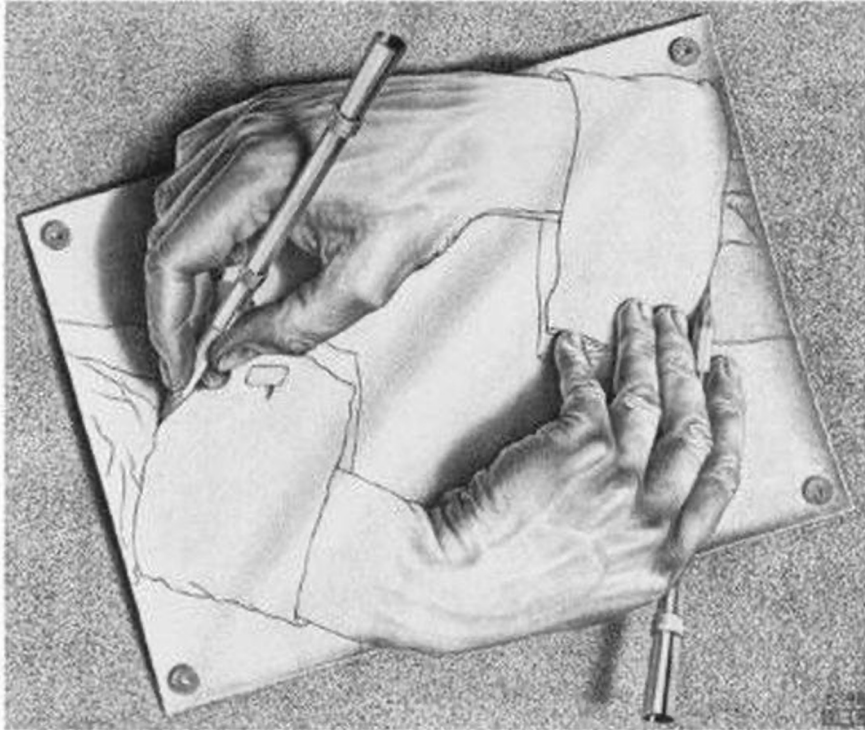


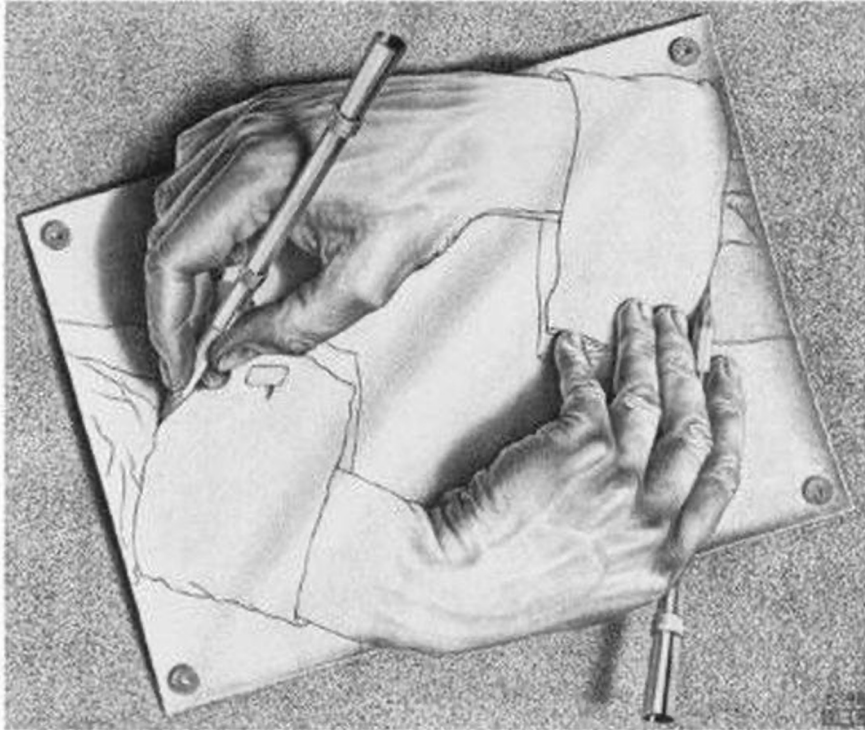
Image credit: OpenMVG

Visual cues for 3D: Shading



M.C. Escher

Visual cues for 3D: Shading

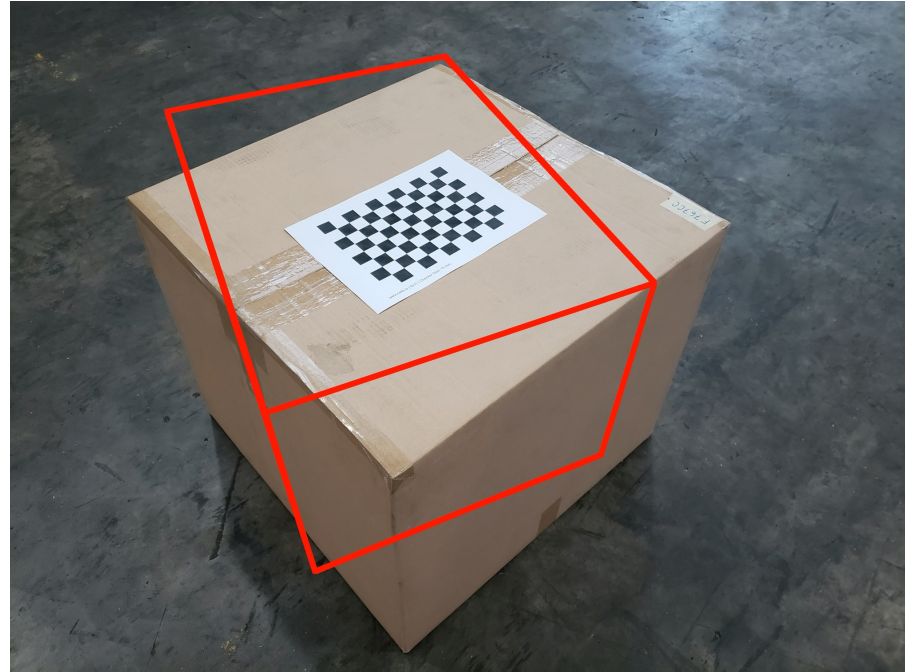
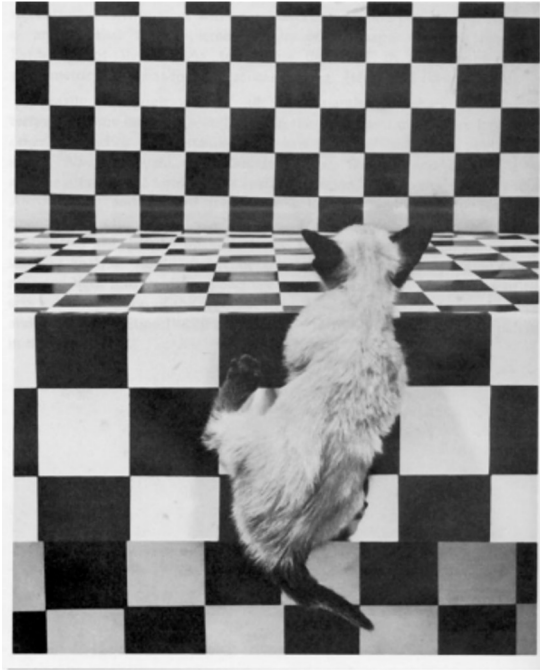


M.C. Escher



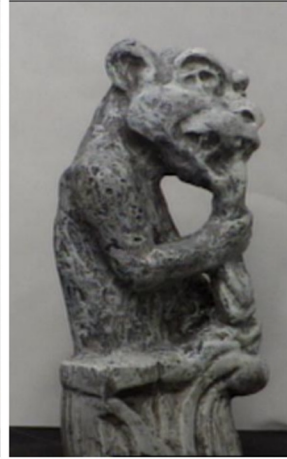
Merle Norman Cosmetics

Visual cues for 3D: Texture



The Visual Cliff by William Vandivert

Visual cues for 3D: Focus, Motion

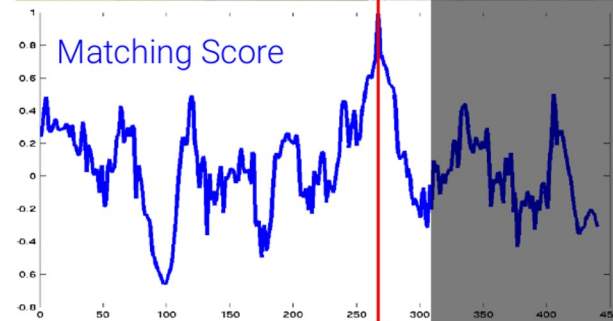
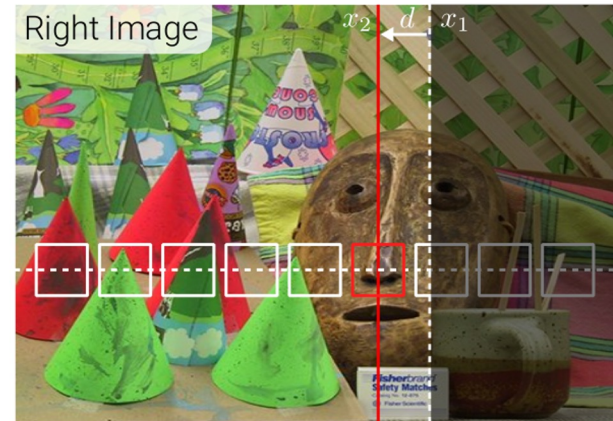
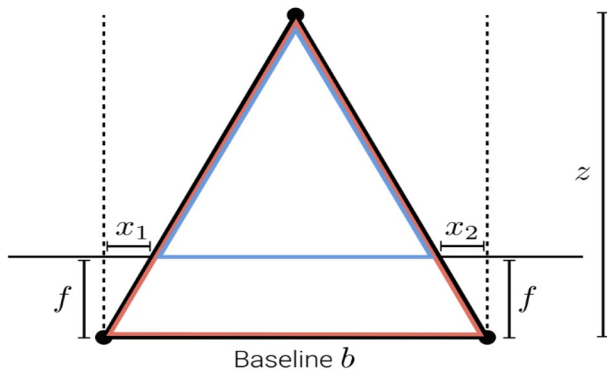


From Art of the Photography

Slide credit: James Hays

Stereo matching

$$\text{disparity} = \frac{b \cdot f}{z}$$



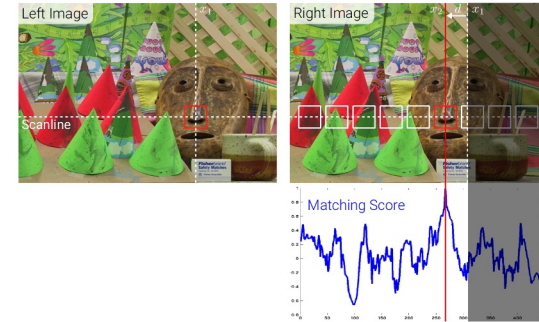
Block matching

$$\text{SSD} = \sum \sum (I_{\text{left}} - I_{\text{right}})^2 \quad \text{Sum of squares difference}$$

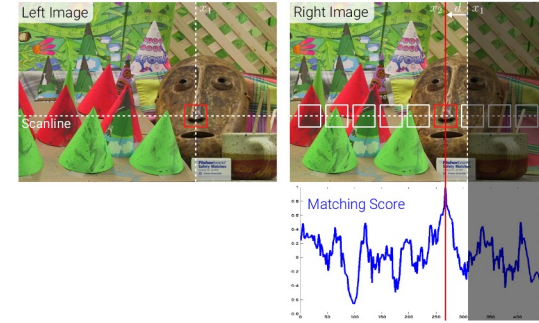
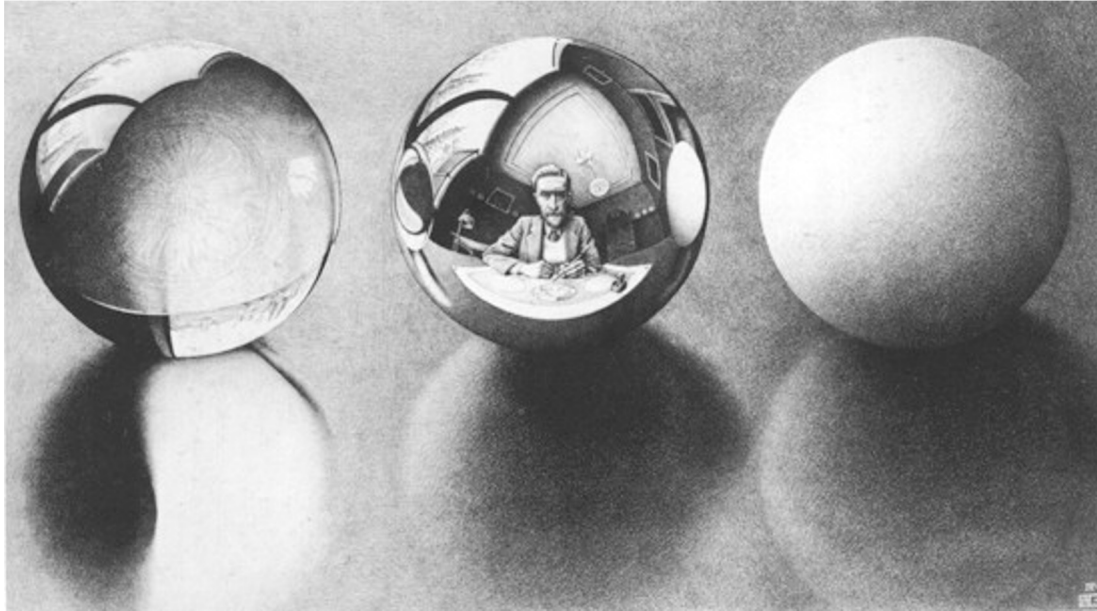
$$\text{AD} = \sum \sum |I_{\text{left}} - I_{\text{right}}| \quad \text{Absolute difference}$$

$$\text{CC} = \sum \sum I_{\text{left}} I_{\text{right}} \quad \text{Cross correlation}$$

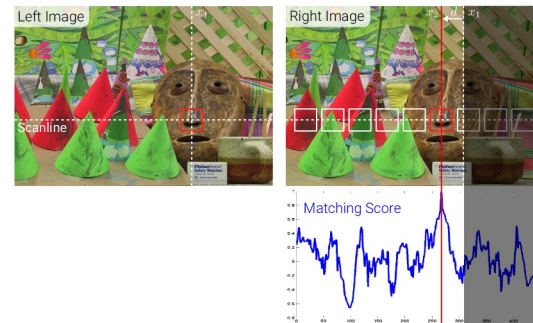
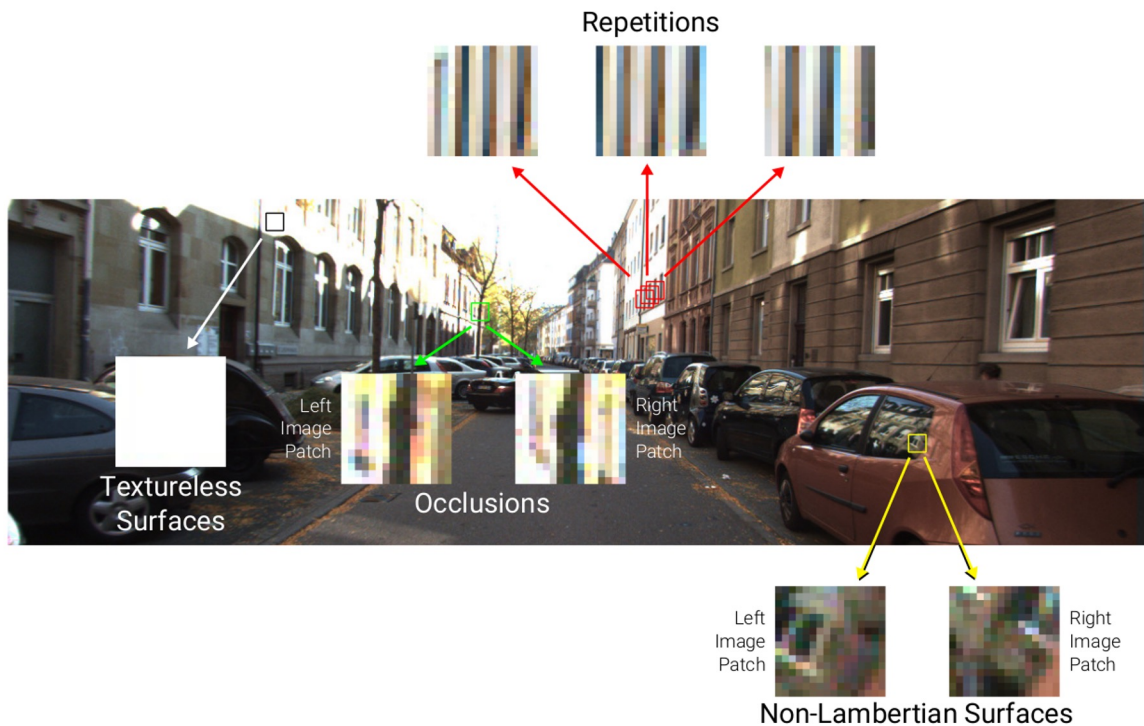
$$\text{NC} = \frac{\sum \sum (I_{\text{left}} \cdot I_{\text{right}})}{\sqrt{\sum \sum I_{\text{left}} \cdot I_{\text{right}}}} \quad \text{Normalized Correlation}$$



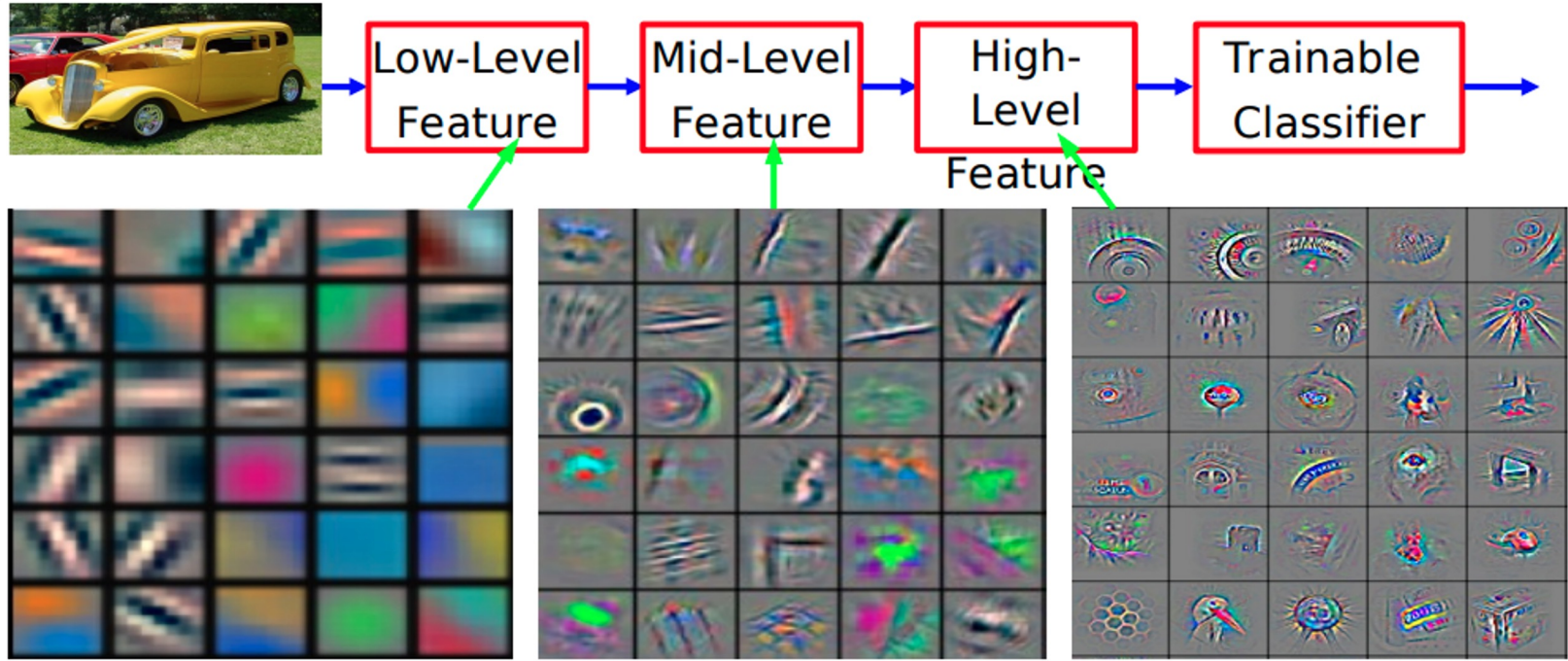
Block matching (Failure cases)



Block matching (Failure cases)



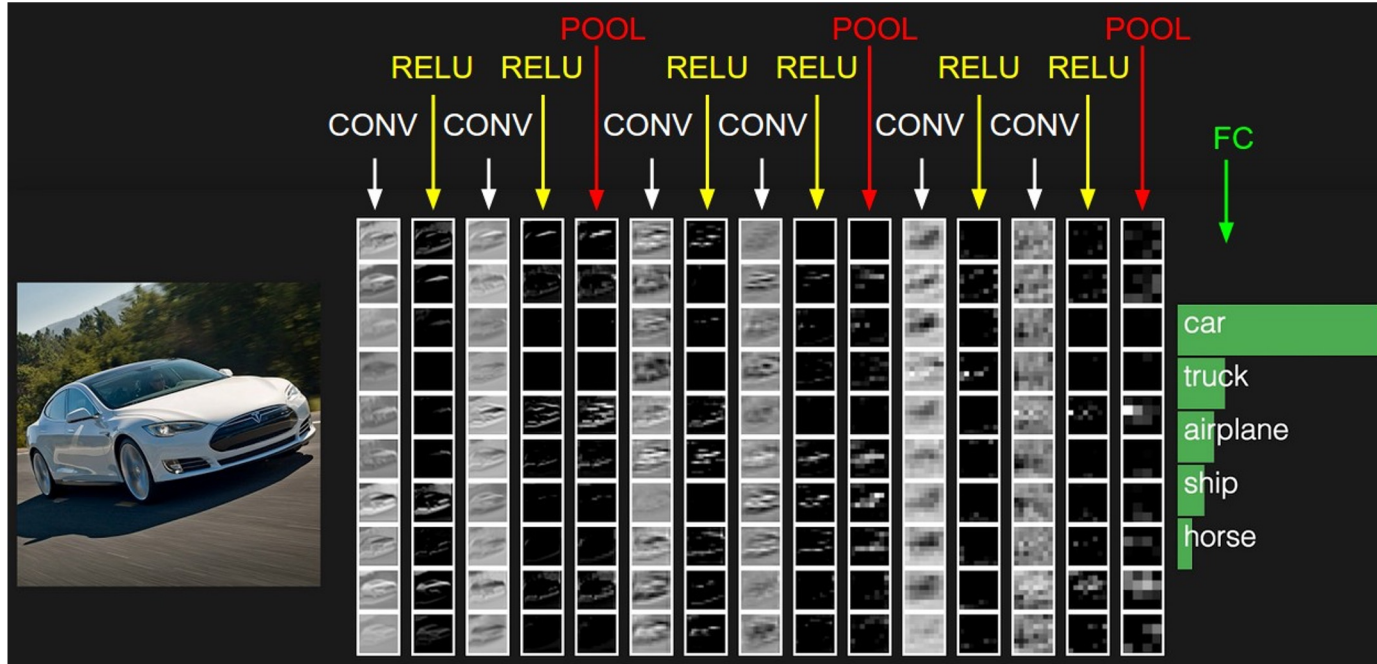
Convolutional features



Slide credit: Yann Lecun

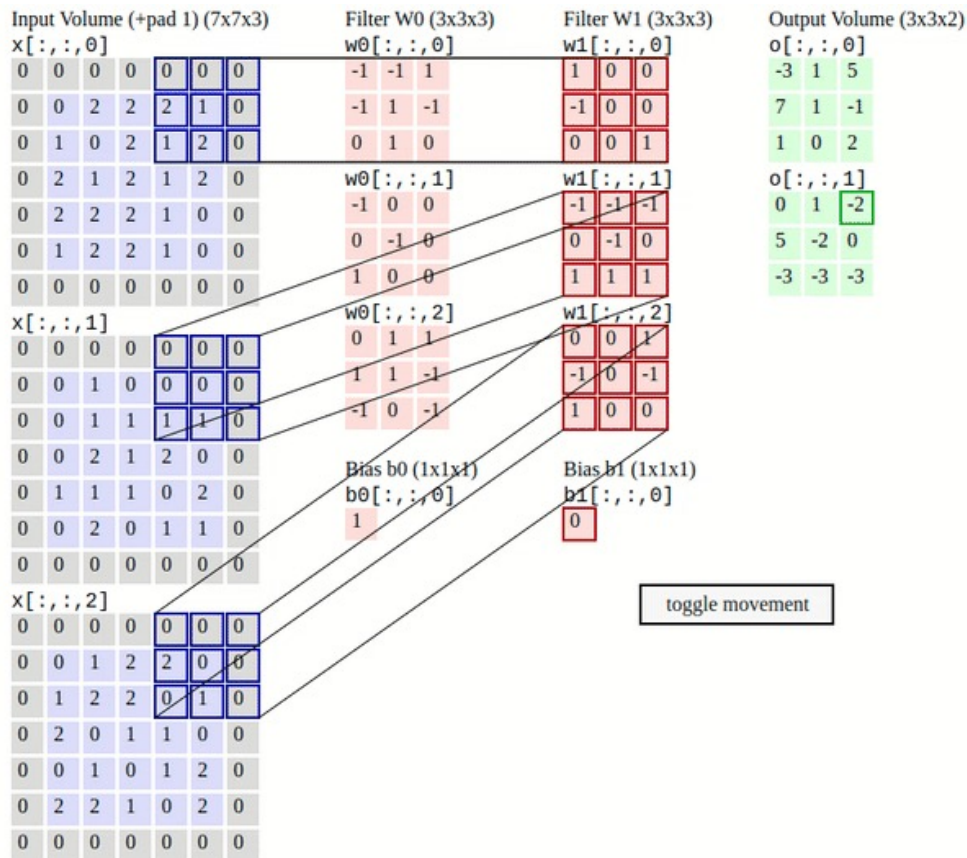
Image credit: Visualizing and Understanding Convolutional Networks (Zeiler & Fergus, 2013)

Convolutional features

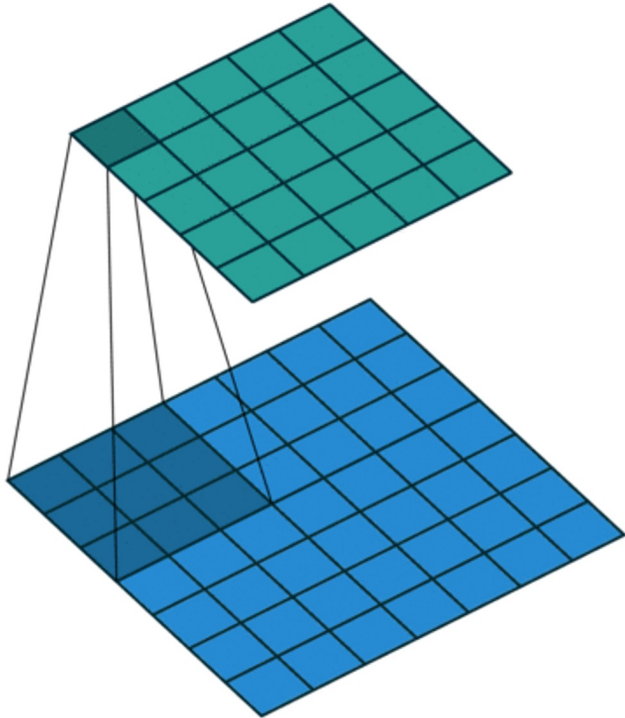


Slide credit: Andrej Karpathy

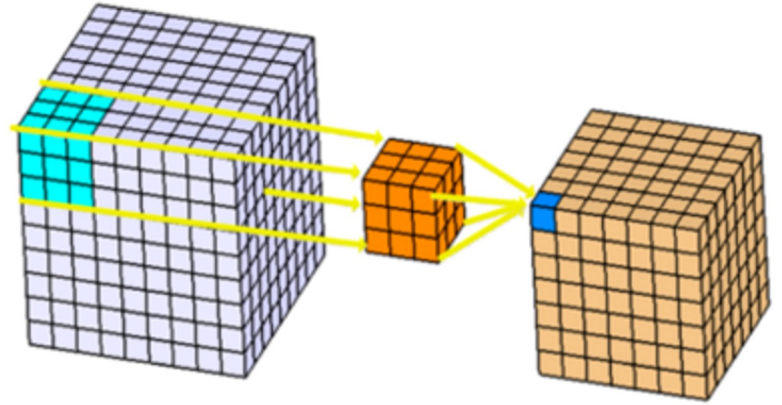
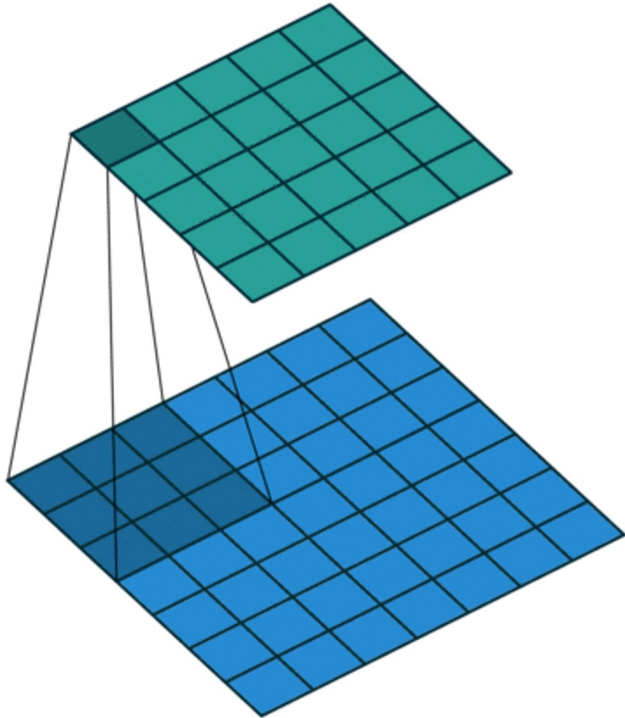
Image convolution



2D and 3D convolutions



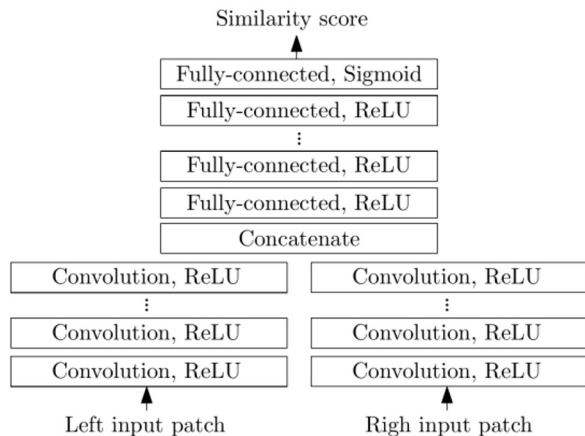
2D and 3D convolutions



Block matching

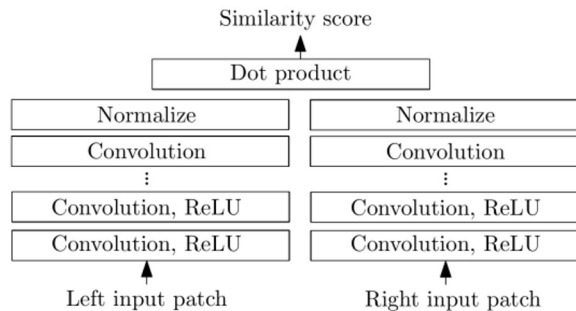
Learned Similarity:

- ▶ Learn features & sim. metric
- ▶ Potentially more expressive
- ▶ Slow (WxHxD MLP evaluations)



Cosine Similarity:

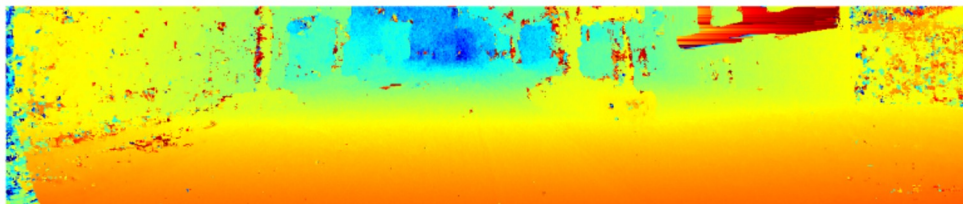
- ▶ Learn features & apply dot-product
- ▶ Features must do the heavy lifting
- ▶ Fast matching (no network eval.)



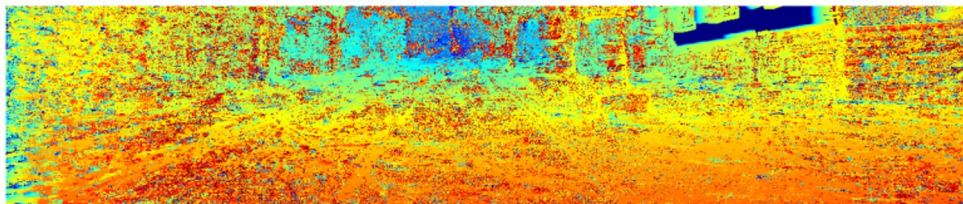
Block matching



Left Input Image

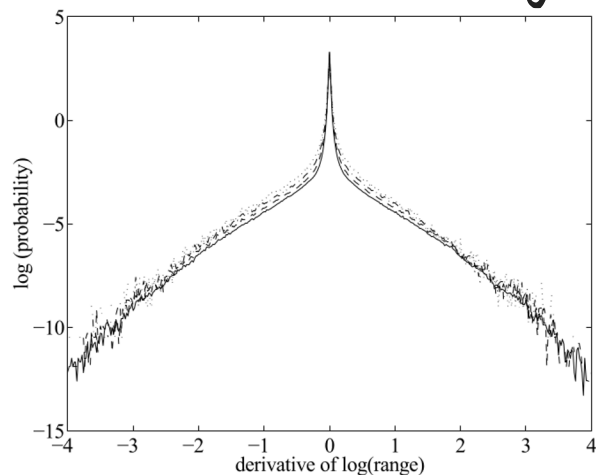


Siamese Network



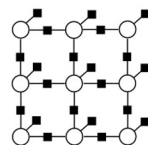
Standard Block Matching

Block matching



Huang, Lee and Mumford: Statistics of Range Images. CVPR, 2000.

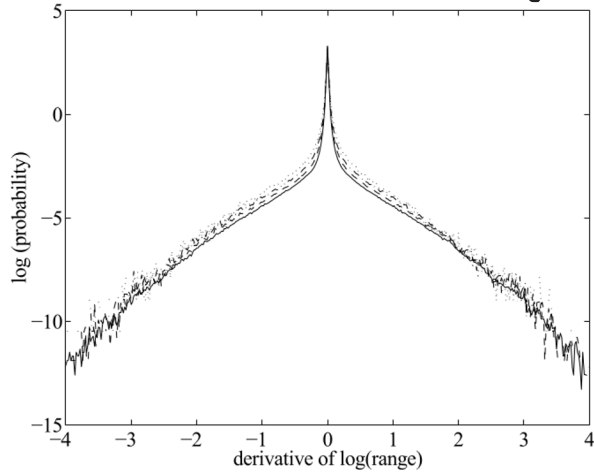
$$p(\mathbf{D}) \propto \exp \left\{ - \sum_i \psi_{data}(d_i) - \lambda \sum_{i \sim j} \psi_{smooth}(d_i, d_j) \right\}$$



Y. Boykov, O. Veksler, and R. Zabih, "Fast approximate energy minimization via graph cuts". PAMI(1999)

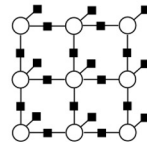
Zbontar and LeCun: Stereo Matching by Training a Convolutional Neural Network to Compare Image Patches. JMLR, 2016.

Block matching

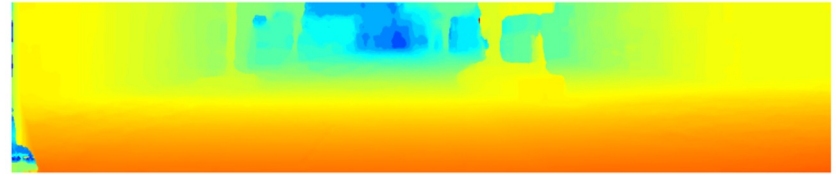


Huang, Lee and Mumford: Statistics of Range Images. CVPR, 2000.

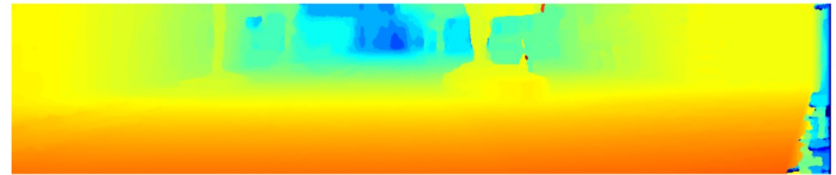
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Y. Boykov, O. Veksler, and R. Zabih, "Fast approximate energy minimization via graph cuts". PAMI(1999)



Left Disparity Map

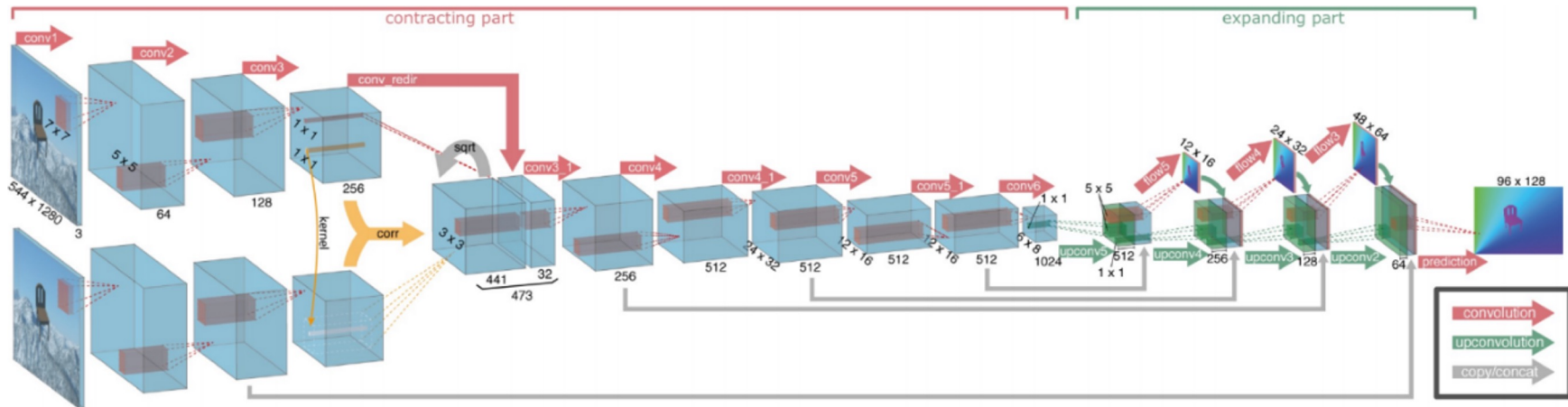


Right Disparity Map



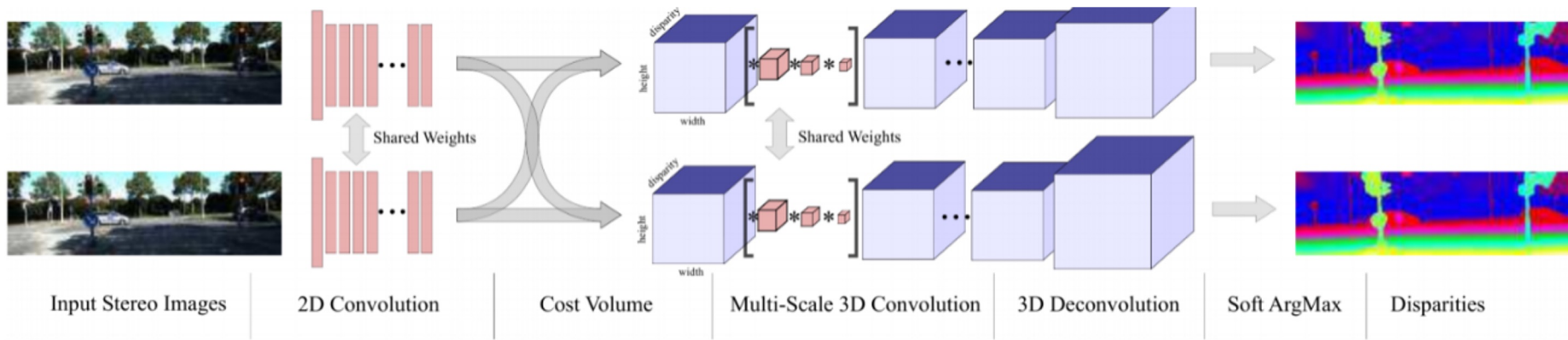
Left-Right Consistency Test

DISPNET



- DispNet was one of the first end-to-end trained deep neural network for stereo disparity
- It used a U-Net like architecture with skip-Connections to retain details
- It introduces correlation layer
- Multi-scale loss (disparity error in pixels), curriculum learning (easy-to-hard)

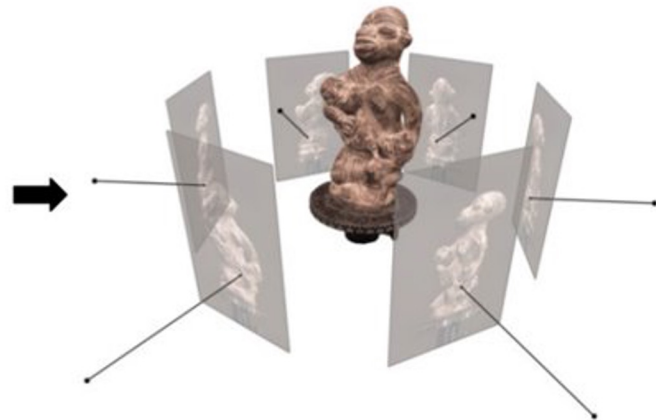
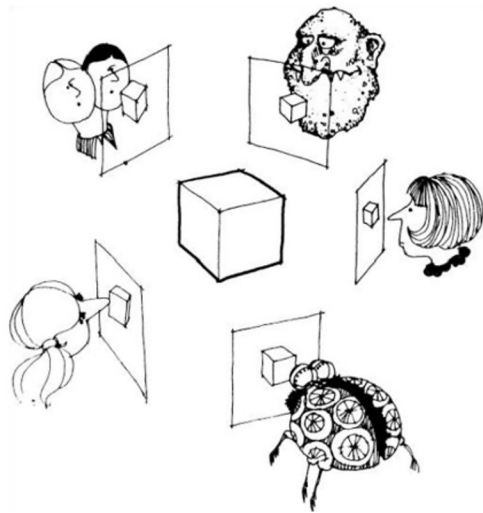
GC-net



$$d^* = \mathbb{E}[d] = \sum_{d=0}^D \underbrace{\text{softmax}(-c_\theta(d))}_{p(d)} \cdot d$$

- Key idea: calculate disparity cost volume and apply 3D convolutions on it
- Convert the learned matching cost c to disparity via the expectation(probability volume)
- Slightly better performance but large memory requirements (3D feature volume)

Multi-view stereo



MVS Goal: To find a 3D shape that explains the images.

PMVS in one slide :)



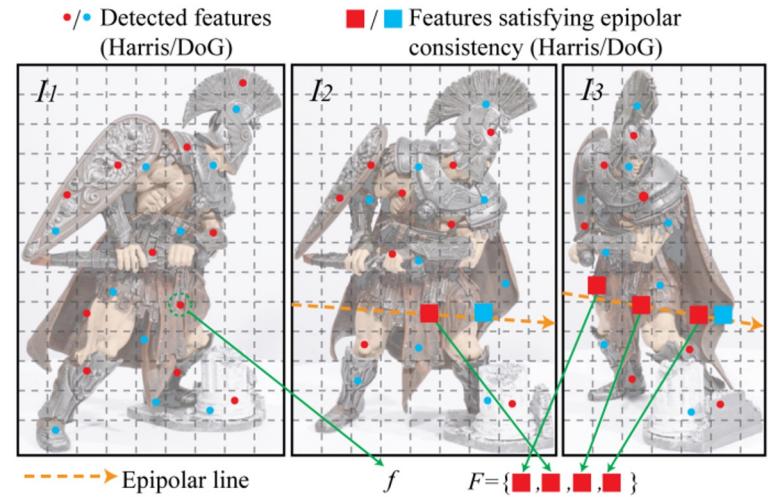
1. Detect keypoints
2. Triangulate a sparse set of initial matches
3. Iteratively expand matches to nearby locations
4. Use visibility constraints to filter out false matches
5. Perform surface reconstruction

Feature Detection

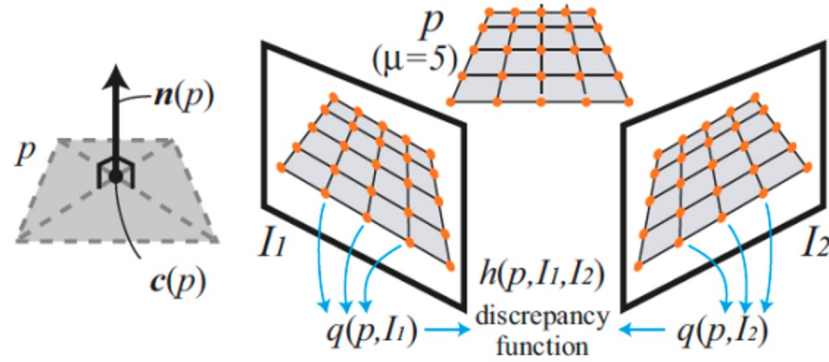
1. Divide grid to cells (32x32)

2. Use Harris Detector and DoG to find corners

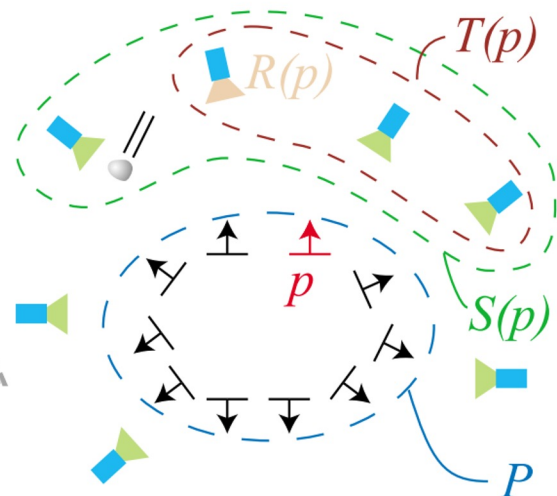
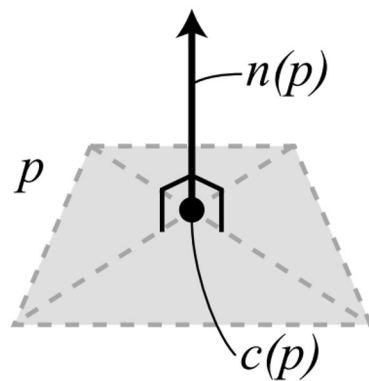
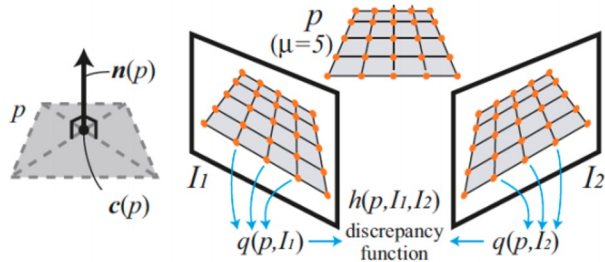
3. Try to find 4 good corners in each cell (uniform overage)



Patch Geometry



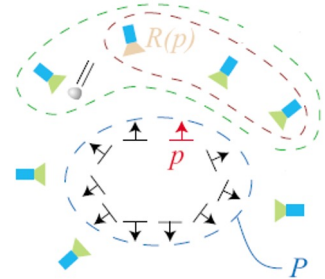
Patch Model



$$\begin{aligned} \mathbf{c}(p) &\leftarrow \{\text{Triangulation from } f \text{ and } f'\}, \\ \mathbf{n}(p) &\leftarrow \frac{\mathbf{c}(p)O(I_i)}{|\mathbf{c}(p)O(I_i)|}, \\ R(p) &\leftarrow I_i. \end{aligned}$$

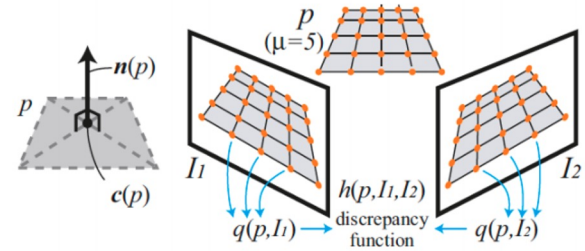
$\mathbf{c}(p)$: center of the patch
 $\mathbf{n}(p)$: normal of the patch
 $R(p)$: reference image with p

Photometric Discrepancy Function



$$h(p, I, R(p)) = 1 - \text{NCC}(p, I, R(p))$$

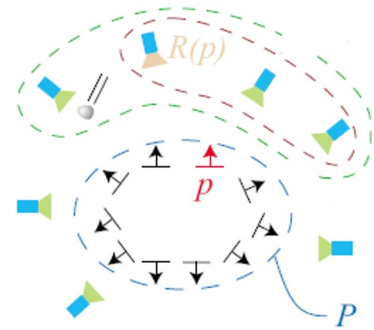
$$g(p) = \frac{1}{|V(p) \setminus R(p)|} \sum_{I \in V(p) \setminus R(p)} h(p, I, R(p))$$



$V(p)$: initial set of images where patch p is potentially visible

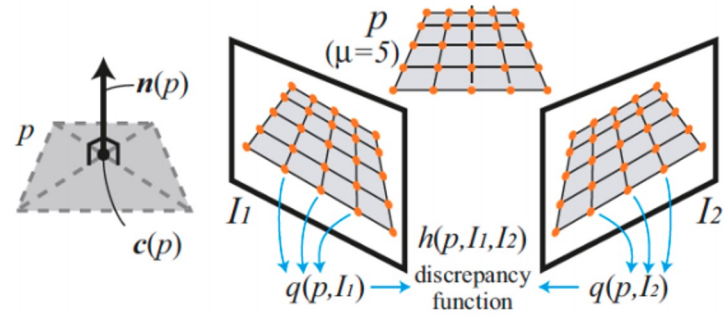
Photometric Discrepancy Function

$$V^*(p) = \{I | I \in V(p), h(p, I, R(p)) \leq \alpha\},$$
$$g^*(p) = \frac{1}{|V^*(p) \setminus R(p)|} \sum_{I \in V^*(p) \setminus R(p)} h(p, I, R(p)).$$



$V(p)$: set of images where patch is truly visible

Patch optimization



$$h(p, I, R(p)) = 1 - \text{NCC}(p, I, R(p))$$

$$g^*(p) = \frac{1}{|V^*(p) \setminus R(p)|} \sum_{I \in V^*(p) \setminus R(p)} h(p, I, R(p))$$

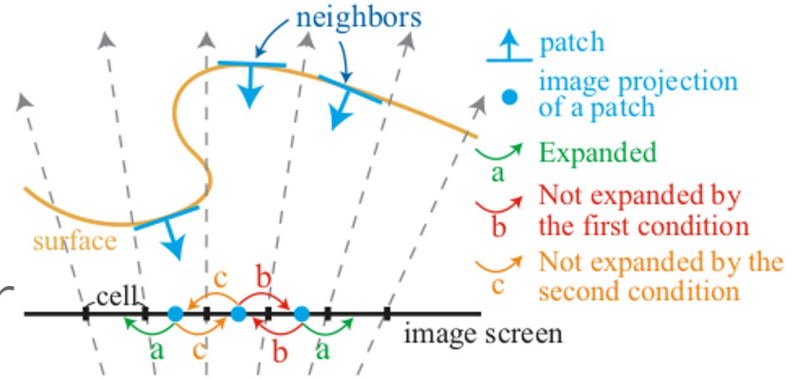
Optimize over $c(p)$ and $n(p)$ that minimizes $g^*(p)$

Expansion

1. Identify neighboring cells for possible expansion
2. Test if there is already patch very close to that region
3. Test for depth discontinuity

Filtering

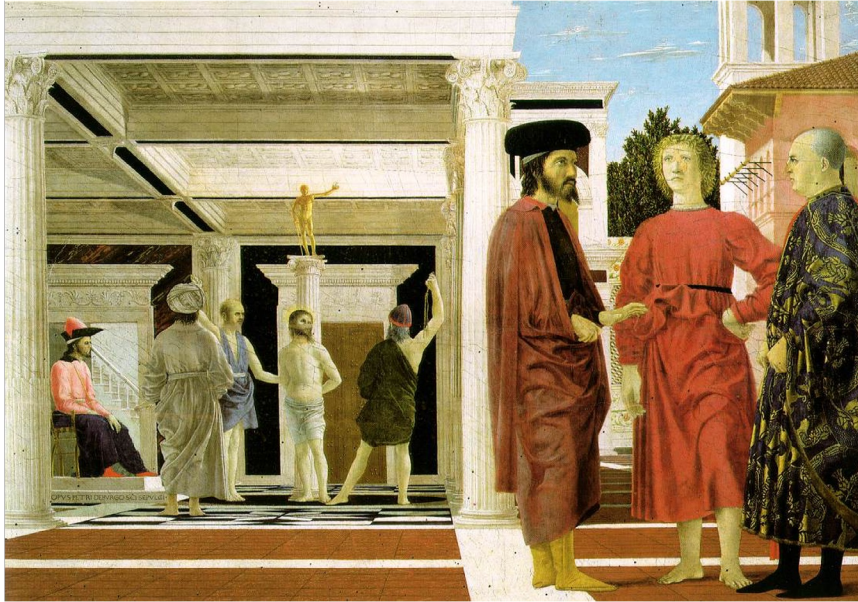
1. Photometric consistency filter
2. Geometric consistency filter
3. Occlusion check



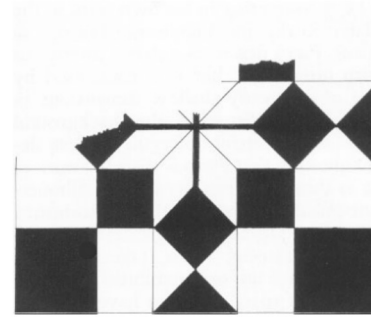
VisualSFM+PMVS



Differential homography



a



b

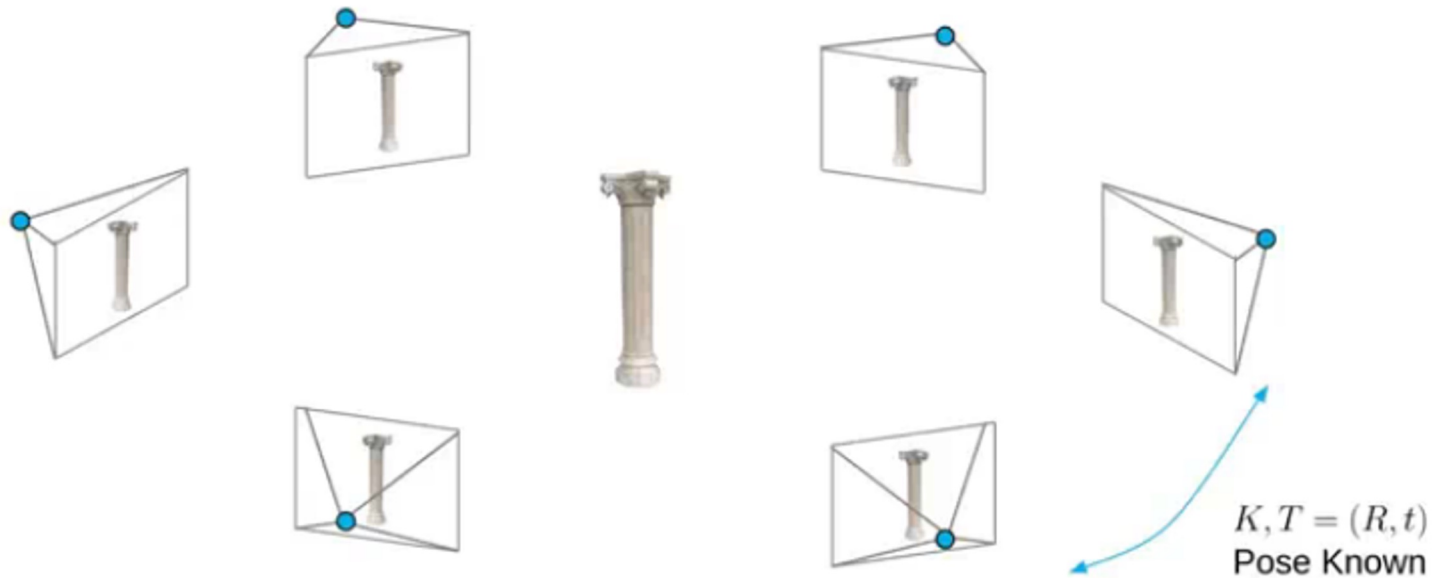


a) crop b) manual labeling c) homography

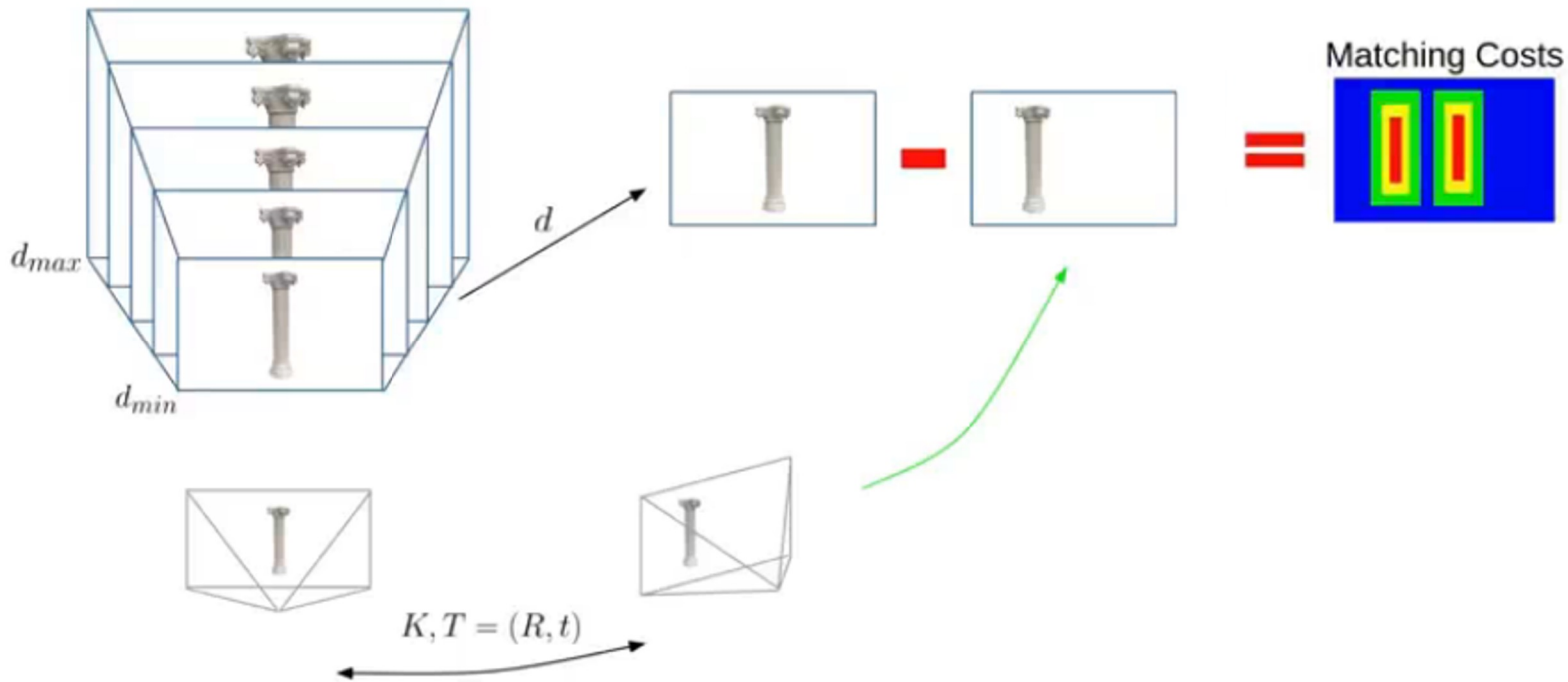
Flagellation
Piero della Francesca

$$\mathbf{p}_{i,j} = \mathbf{K}_i \cdot (\mathbf{R}_{0,i} \cdot (\mathbf{K}_0^{-1} \cdot \mathbf{p} \cdot d_j) + \mathbf{t}_{0,i})$$

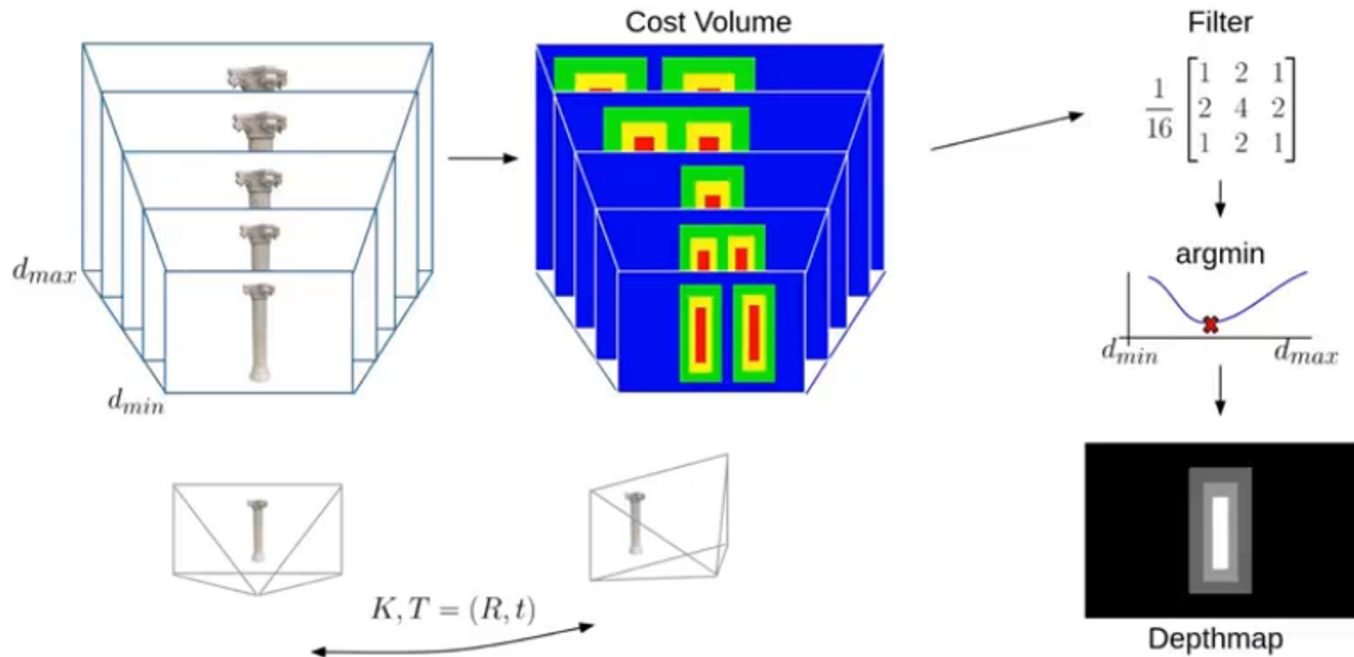
Multi-view stereo - plane sweep stereo



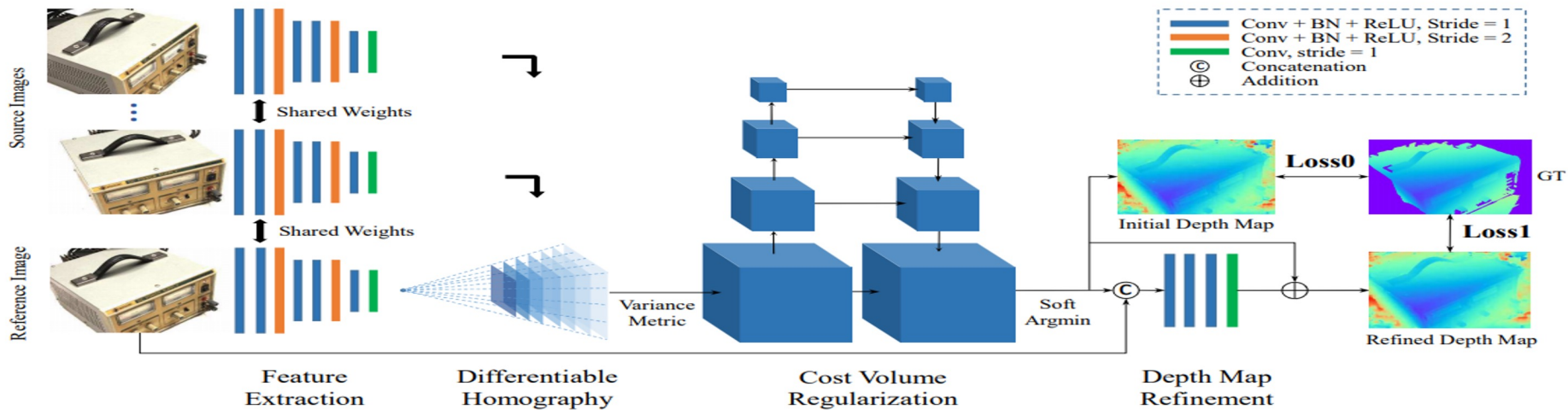
Multi-view stereo - plane sweep stereo



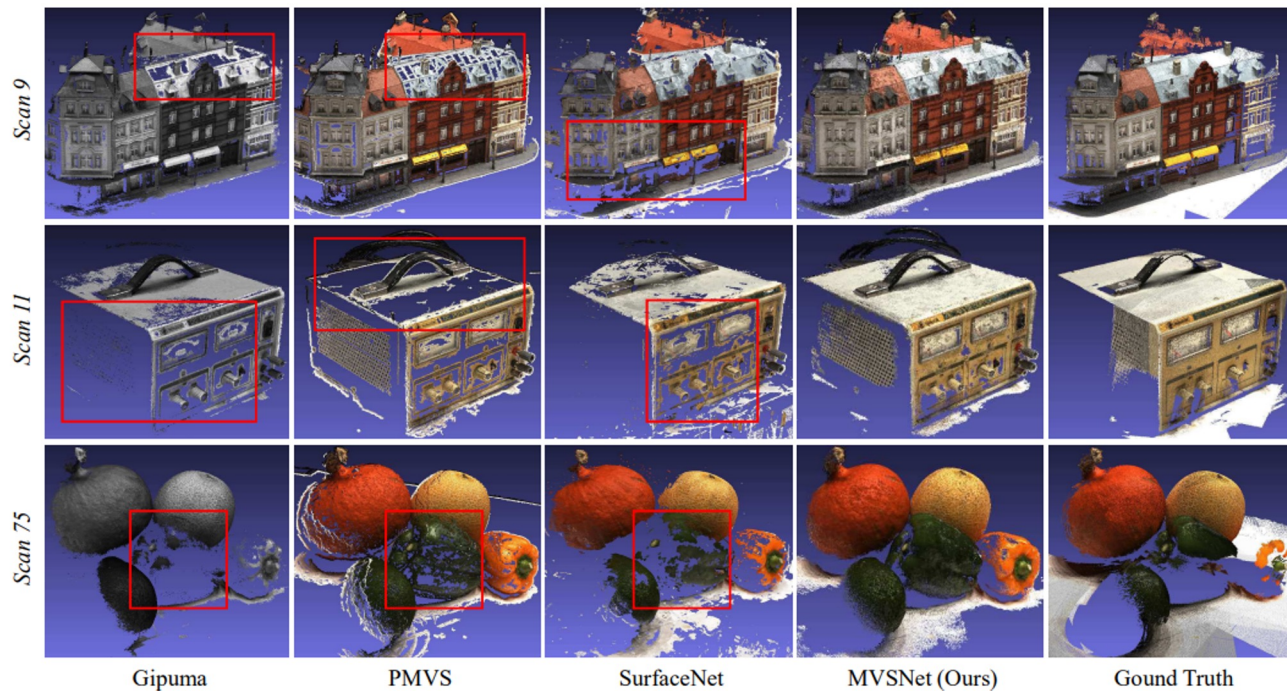
Multi-view stereo - plane sweep stereo



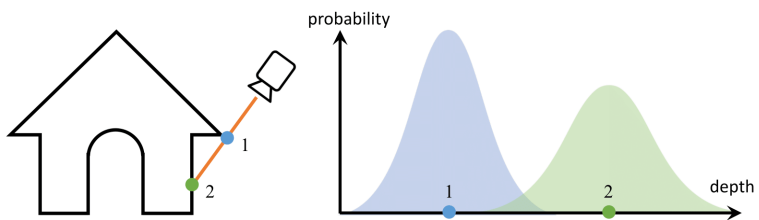
MVSNET



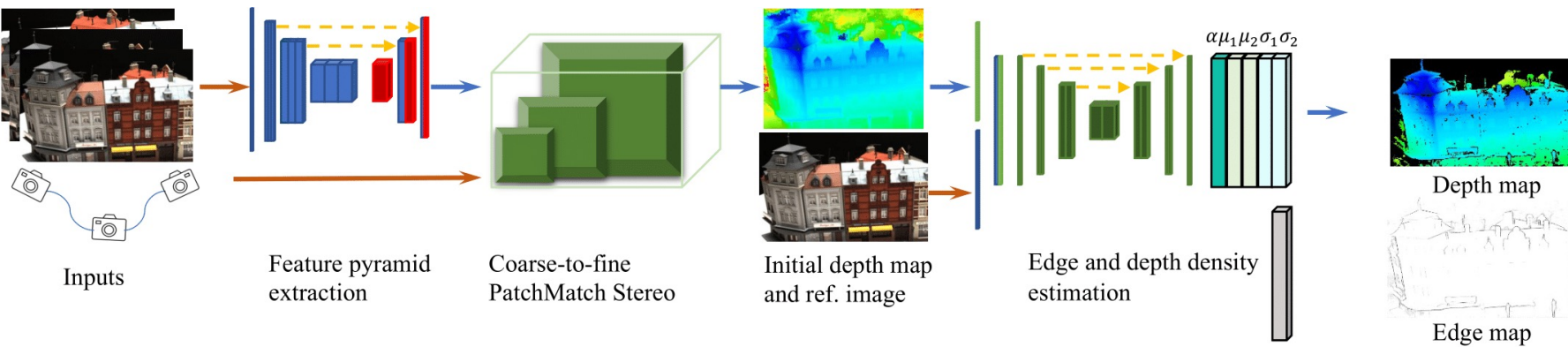
MVSNET



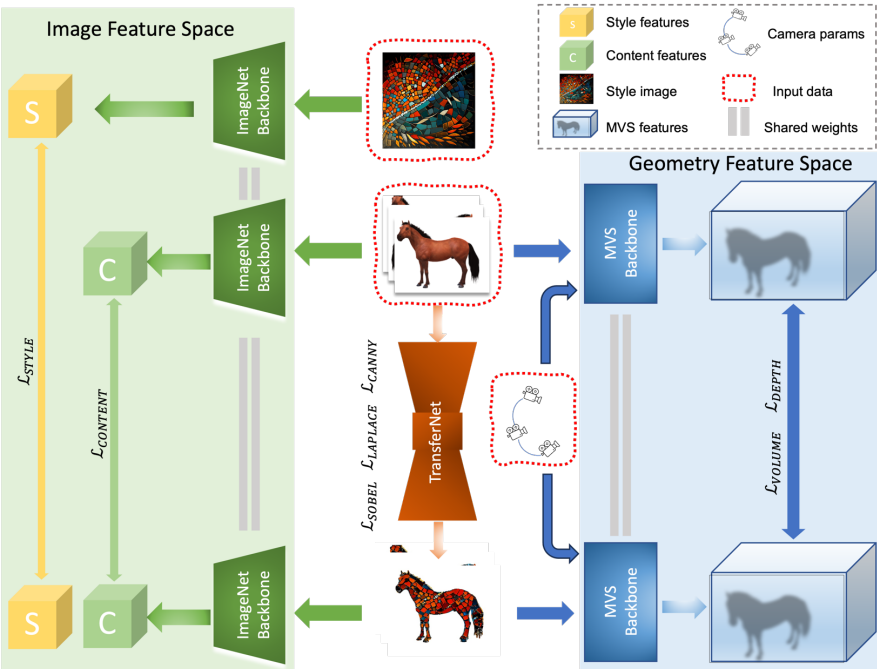
DDL MVS



This video demonstrates visual comparisons with COLMAP and PatchmatchNet



MVCAST





THANKS FOR LISTENING.