

Boundary representation, surfaces and meshes

GEO1004:
3D modelling of the built environment

<https://3d.bk.tudelft.nl/courses/geo1004>

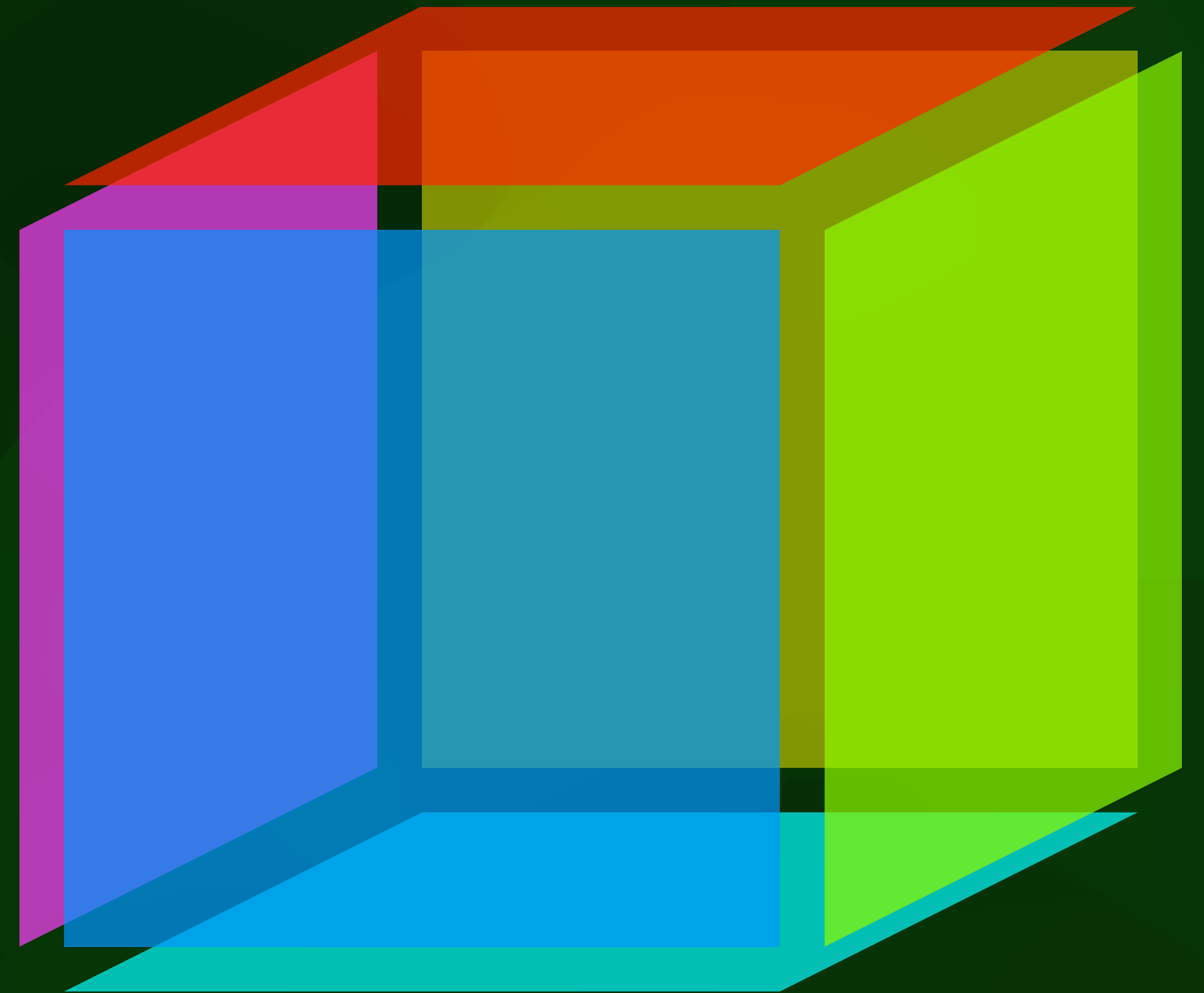


3D geoinformation

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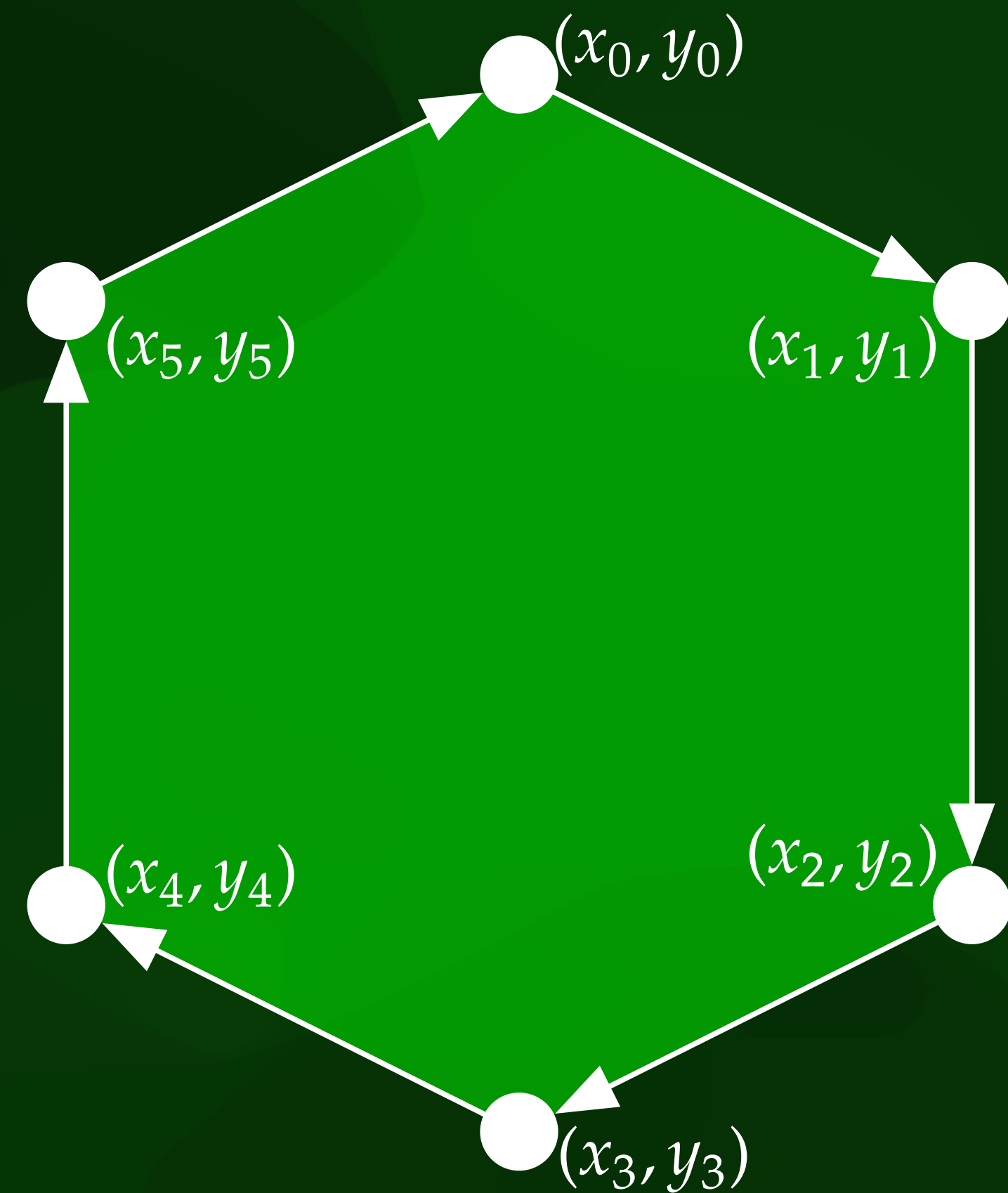
What is boundary representation?

- Also known as b-rep or surface modelling
- Representing an n -dimensional object through its $(n - 1)$ -dimensional boundary
- Most of the time: a 3D object through its 2D boundary

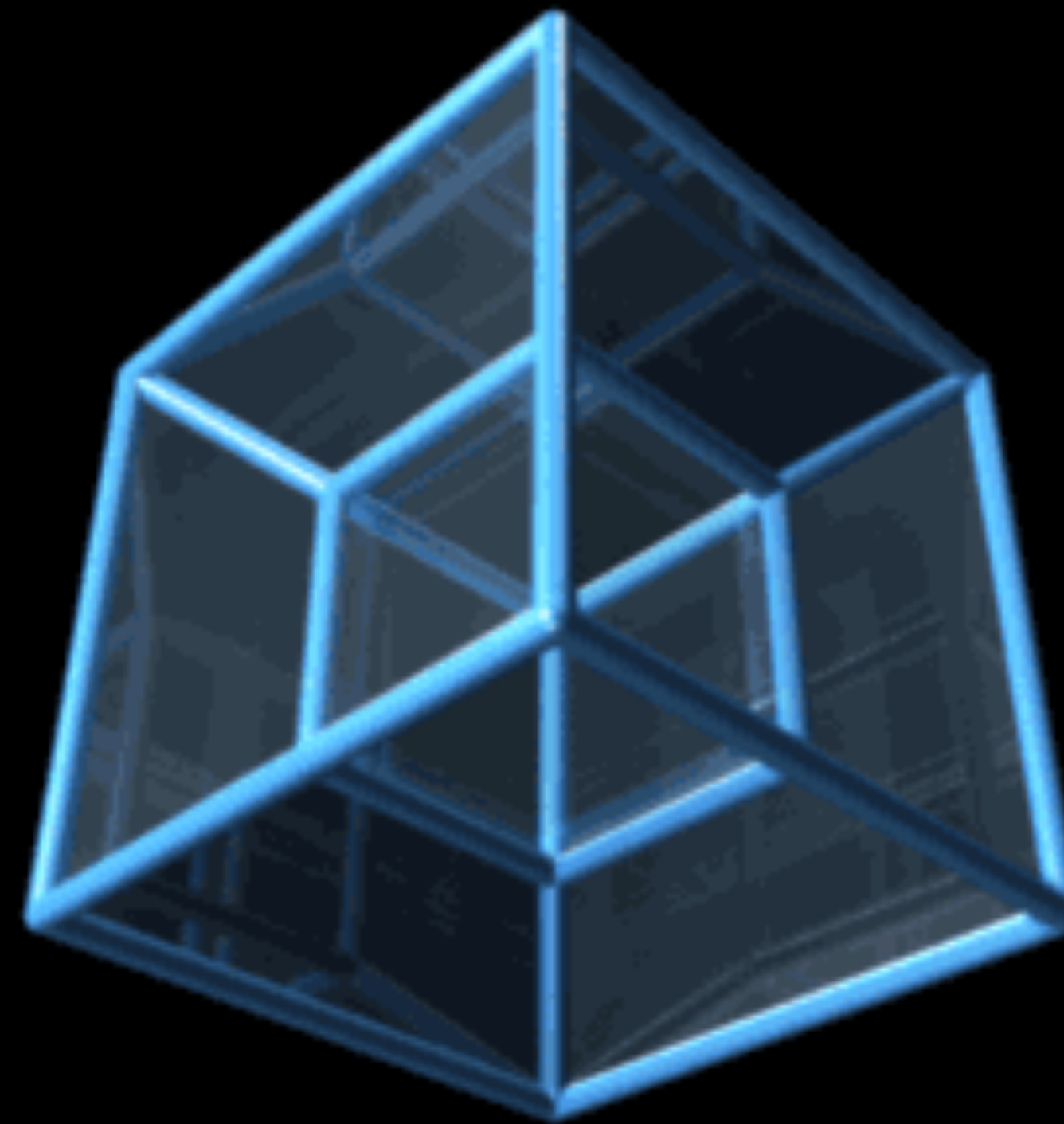
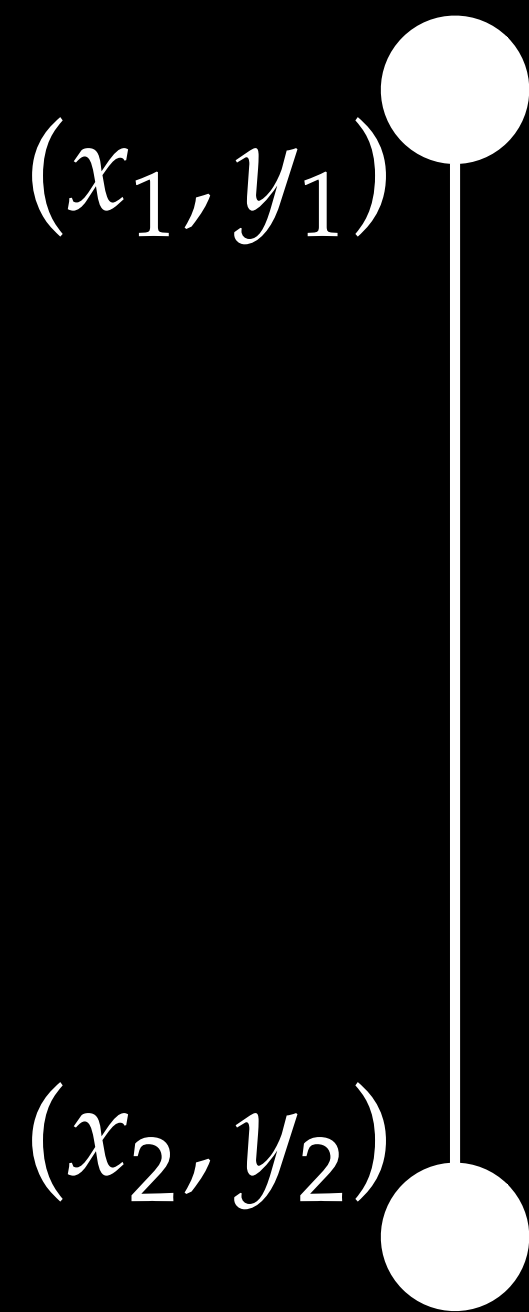


Why do it?

- Data structures for 2D are easier than data structures for 3D
- Representing 2D polygons: as simple as a list of (x, y) vertices
- Implicit assumption: there's a connection between each consecutive vertex and between the last and first



In any dimension



Why does it work?

- In 2D, the Jordan curve theorem says: a closed curve separates the plane into two parts: an interior surface and an exterior surface
- In n D, the Jordan-Brouwer theorem, which in 3D says: a closed surface separates 3D space into two parts: an interior volume and an exterior volume.

b-rep in the 3D context

- store 3D objects by storing their 2D boundary
- ... which can be split into a set of **surfaces** (in GIS usually triangles or polygons)
- ... which can be represented using a (2D) **mesh**, i.e. a repetitive arrangement of simpler elements
- note: not the same as a 3D mesh (e.g. TEN)

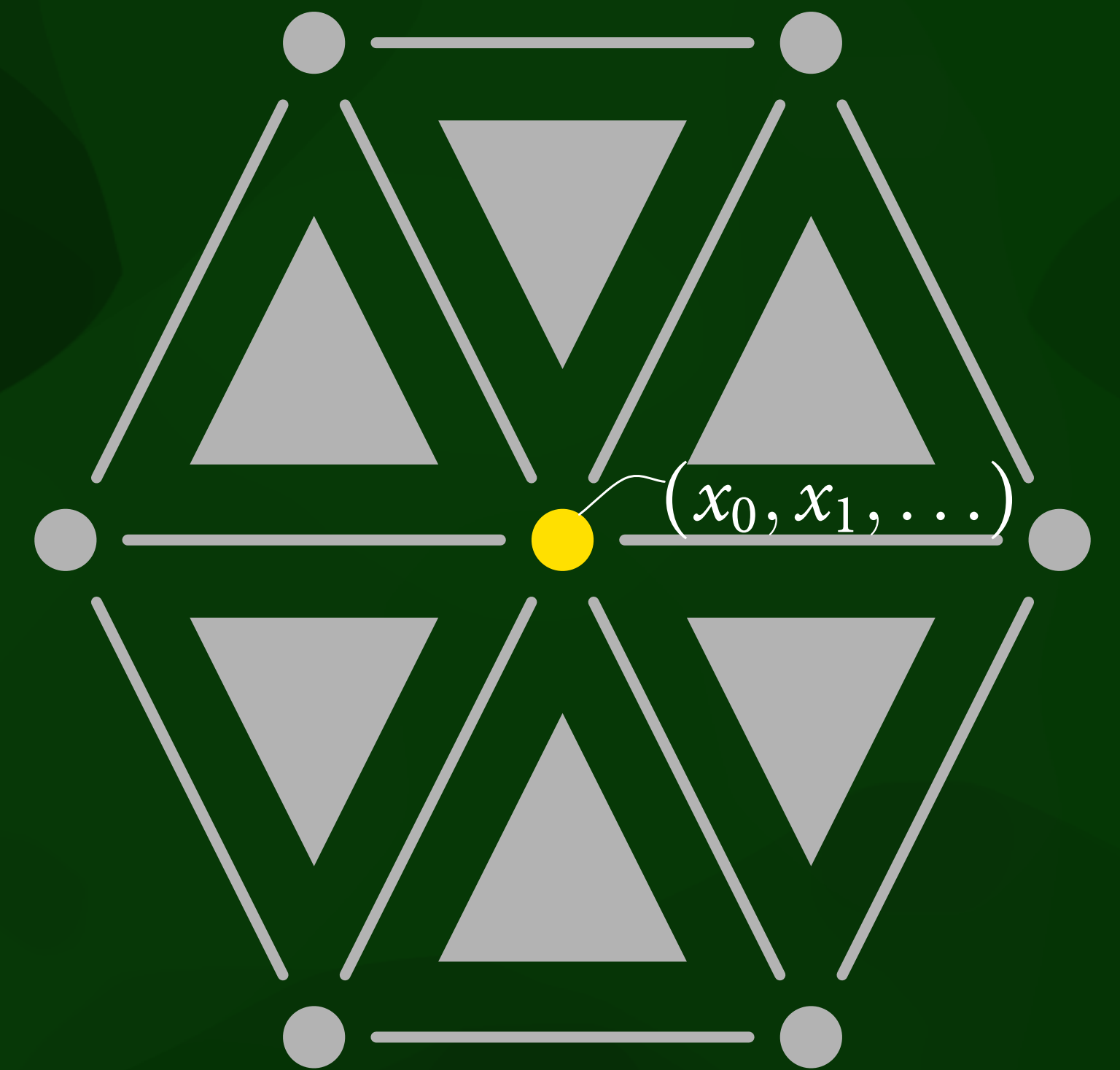
Where?

- Every traditional GIS format (Shapefiles, GML, KML, GeoJSON, etc.)
- Most formats for 3D graphics (OBJ, PLY, VRML, COLLADA, glTF, etc.)
- Most implementations in DBs (PostGIS, Spatialite, MySQL, Oracle Spatial, etc.)
- Part of what is internally used in 3D modelling and 3D animation software, CAD and BIM, 3D games and game engines, etc.

Storing a 2D mesh

- Three basic approaches:
 - Split into triangles, then use a triangle-based structure
 - Keep as polygons, then use:
 - edge-based structures or
 - incidence graphs

Triangle-based structures



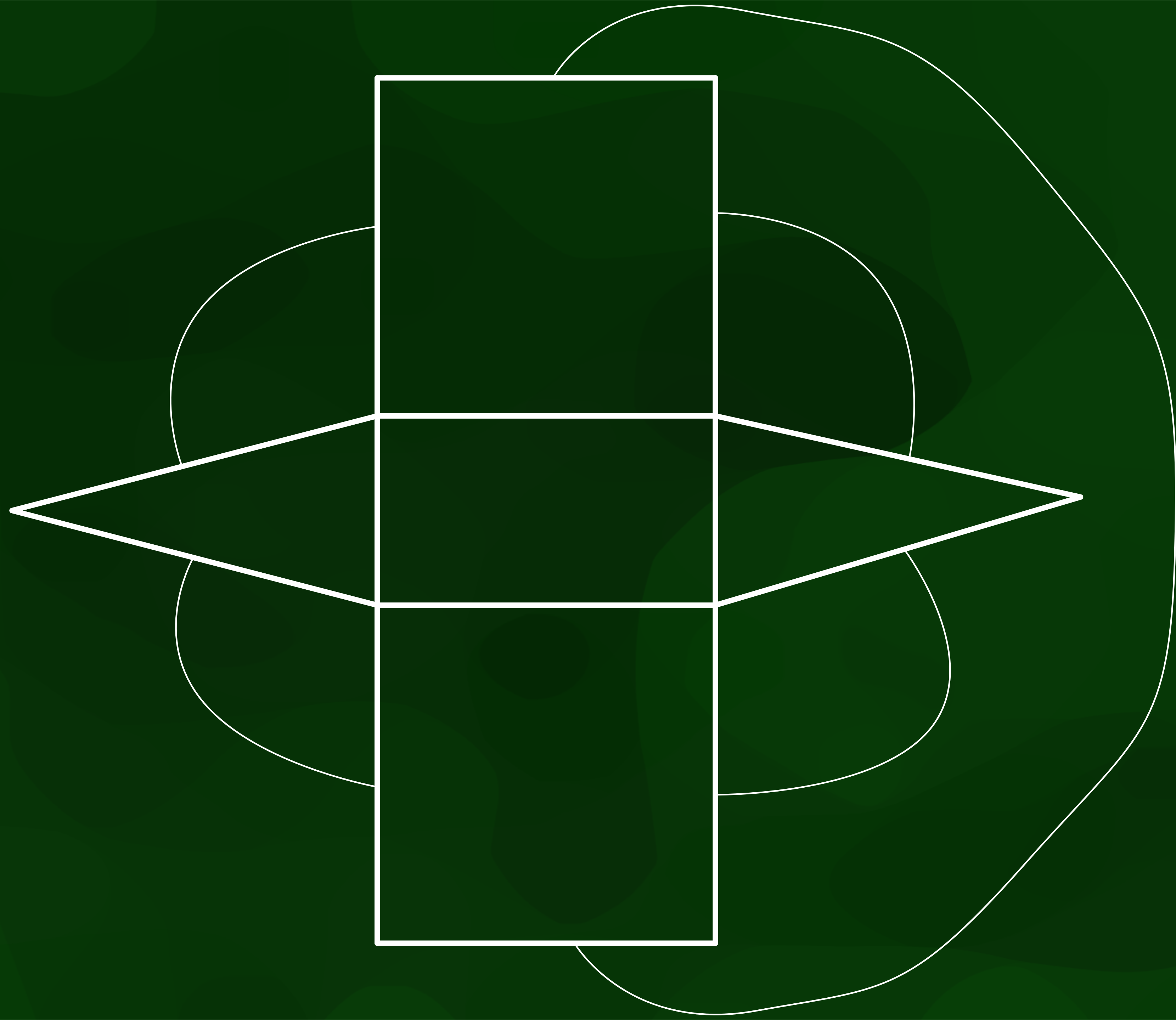
Some examples

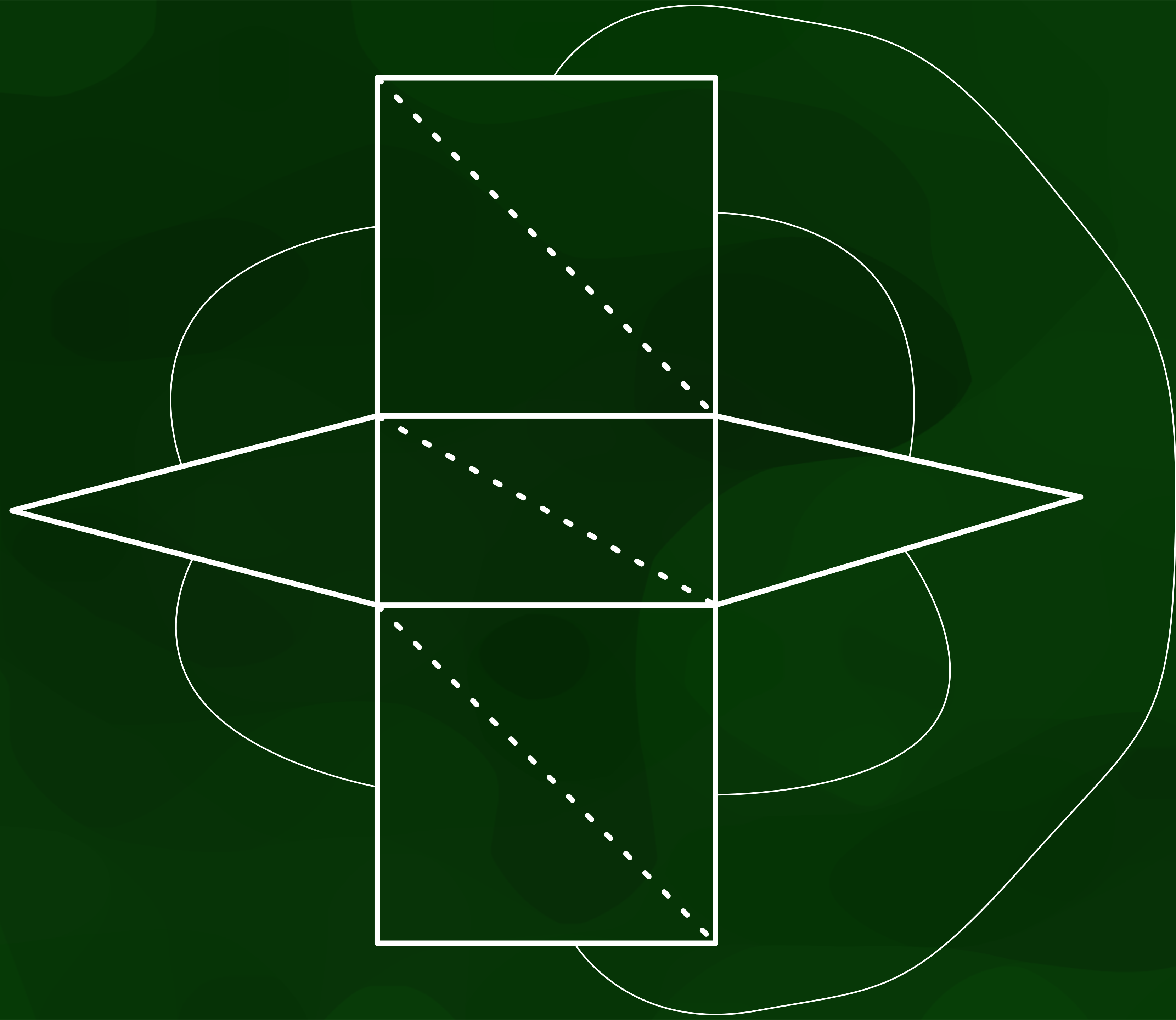
- Triangle DS as 3 points, i.e. coordinates of its 3 vertices (no topology)
- Triangle DS pointing to 3 vertex DS (vertex DS has coordinates)
- Triangle DS pointing to: 3 adjacent triangle DS and 3 vertex DS
- Triangle DS pointing to 3 adjacent triangle DS, 3 edge DS and 3 vertex DS

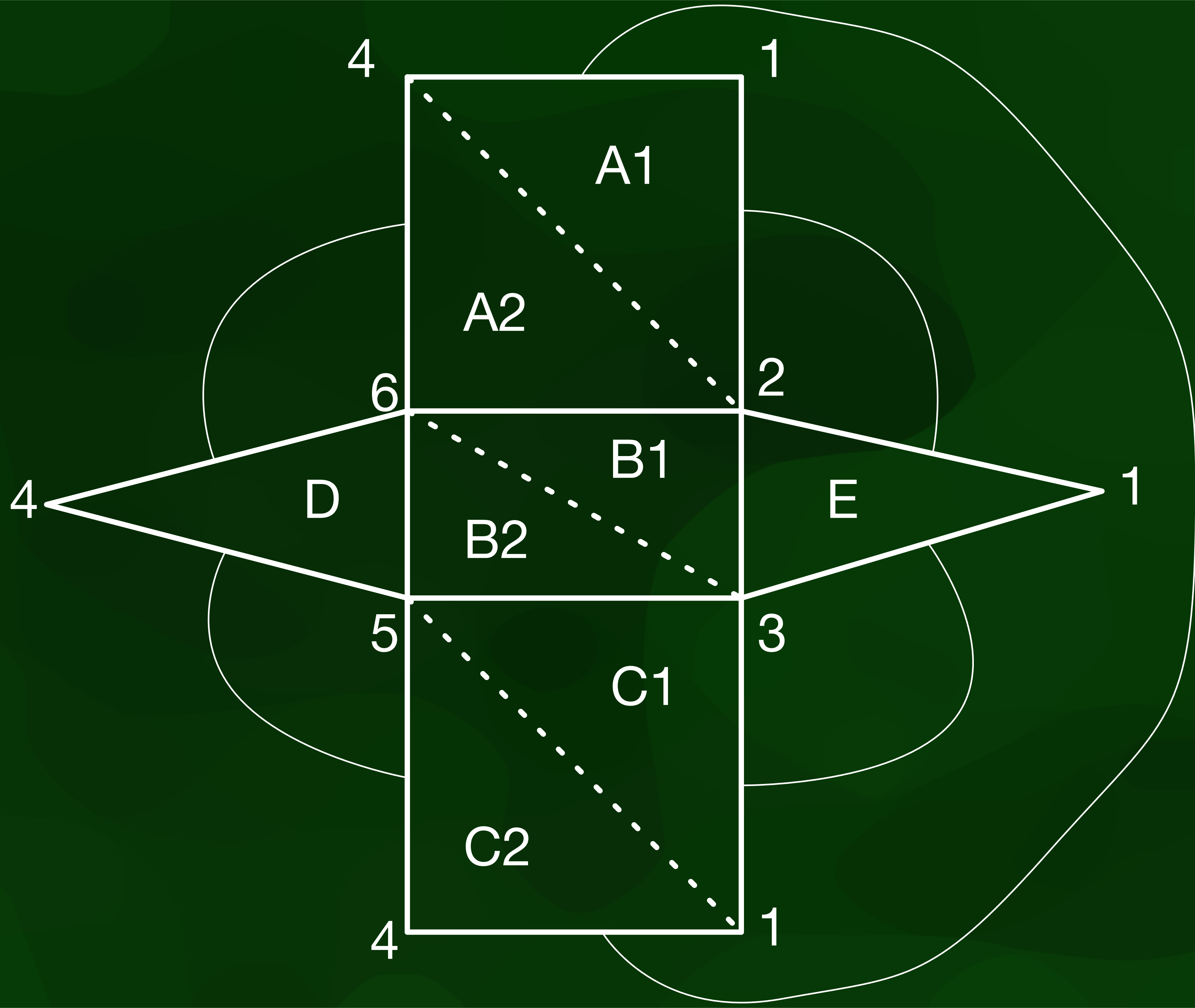
Example from CGAL

https://doc.cgal.org/latest/TDS_2/index.html



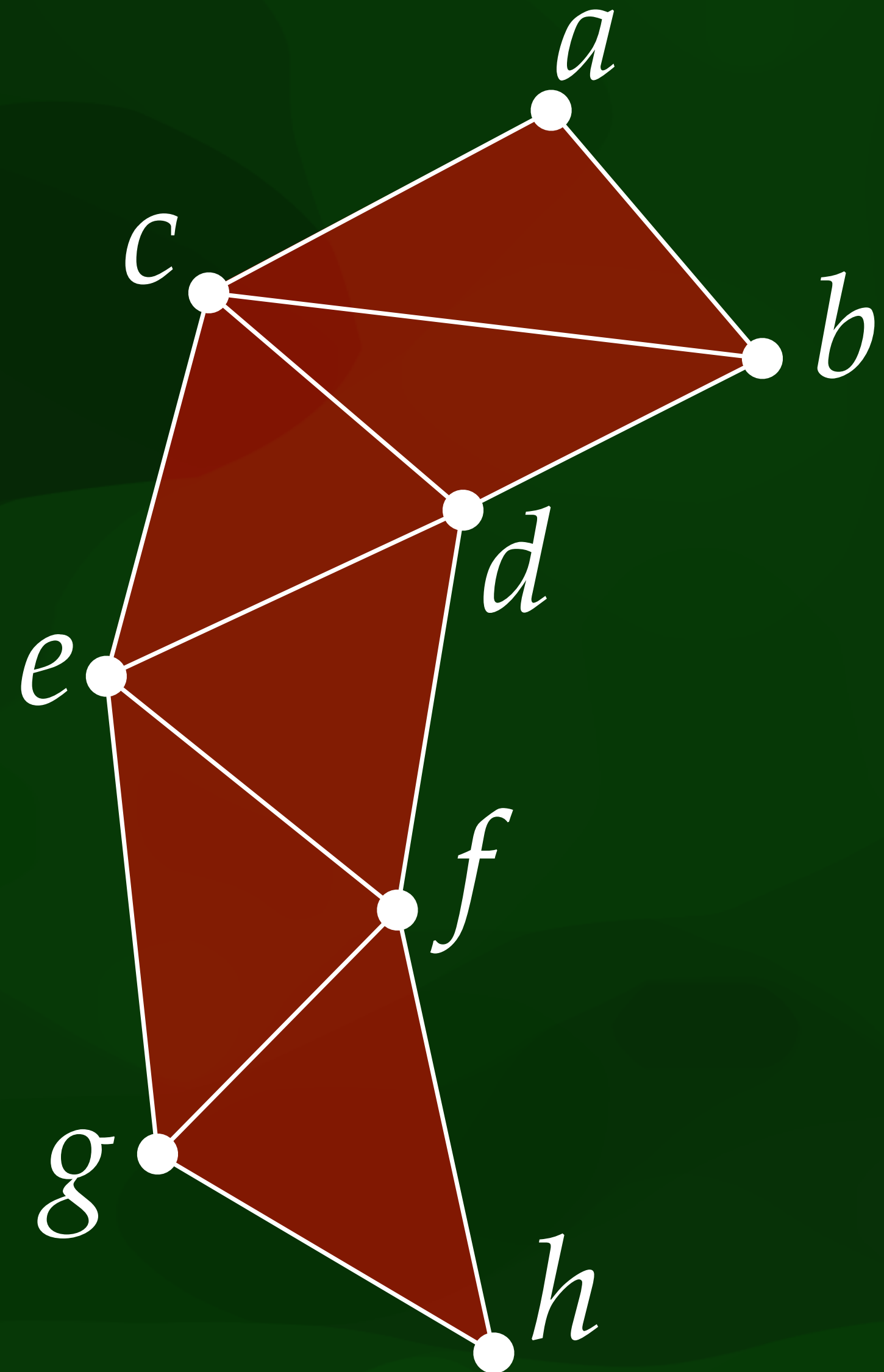






Compression of triangle DS

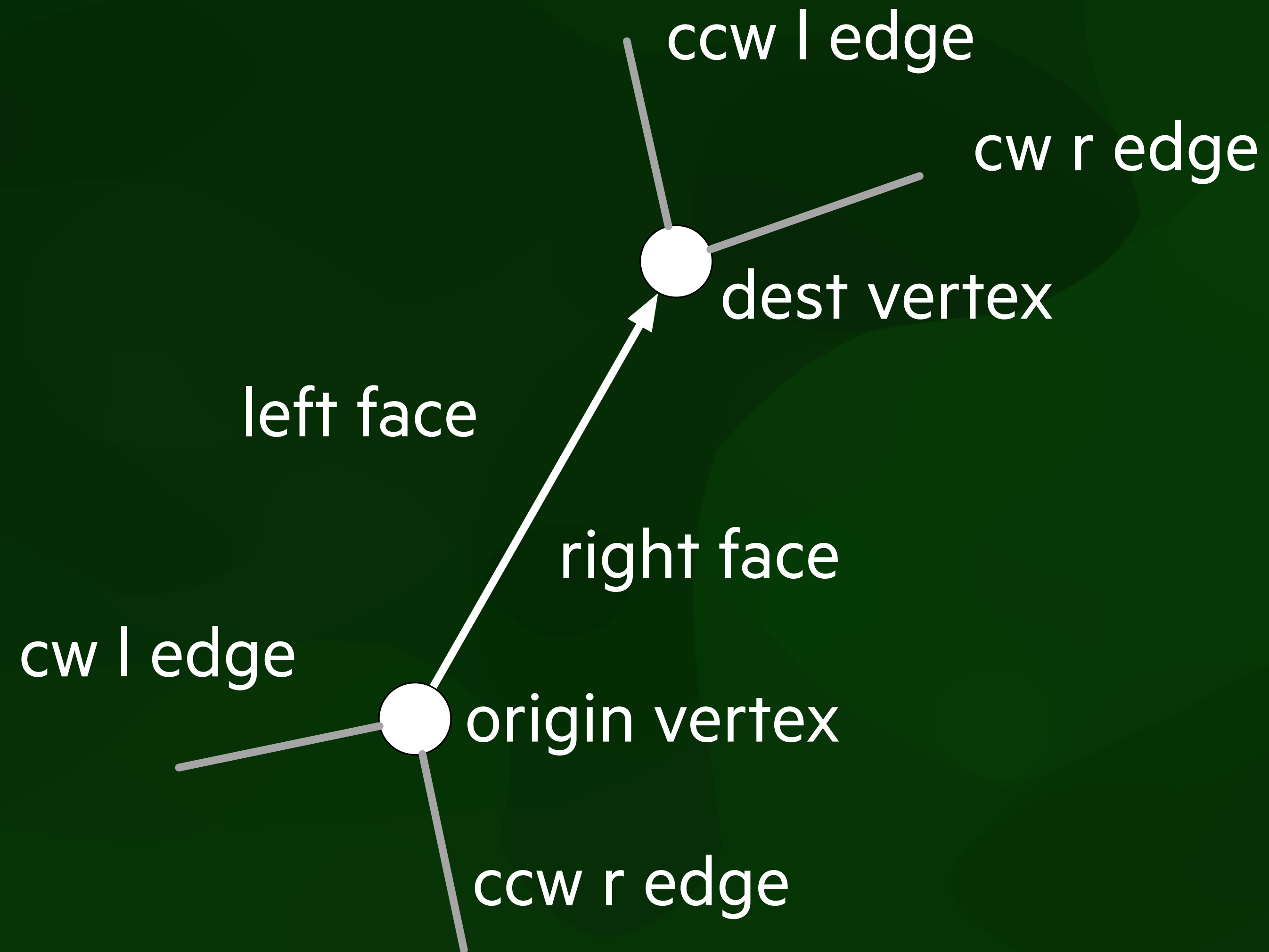
- Triangle strips
- Triangle fans
- Triangle stars
- ...

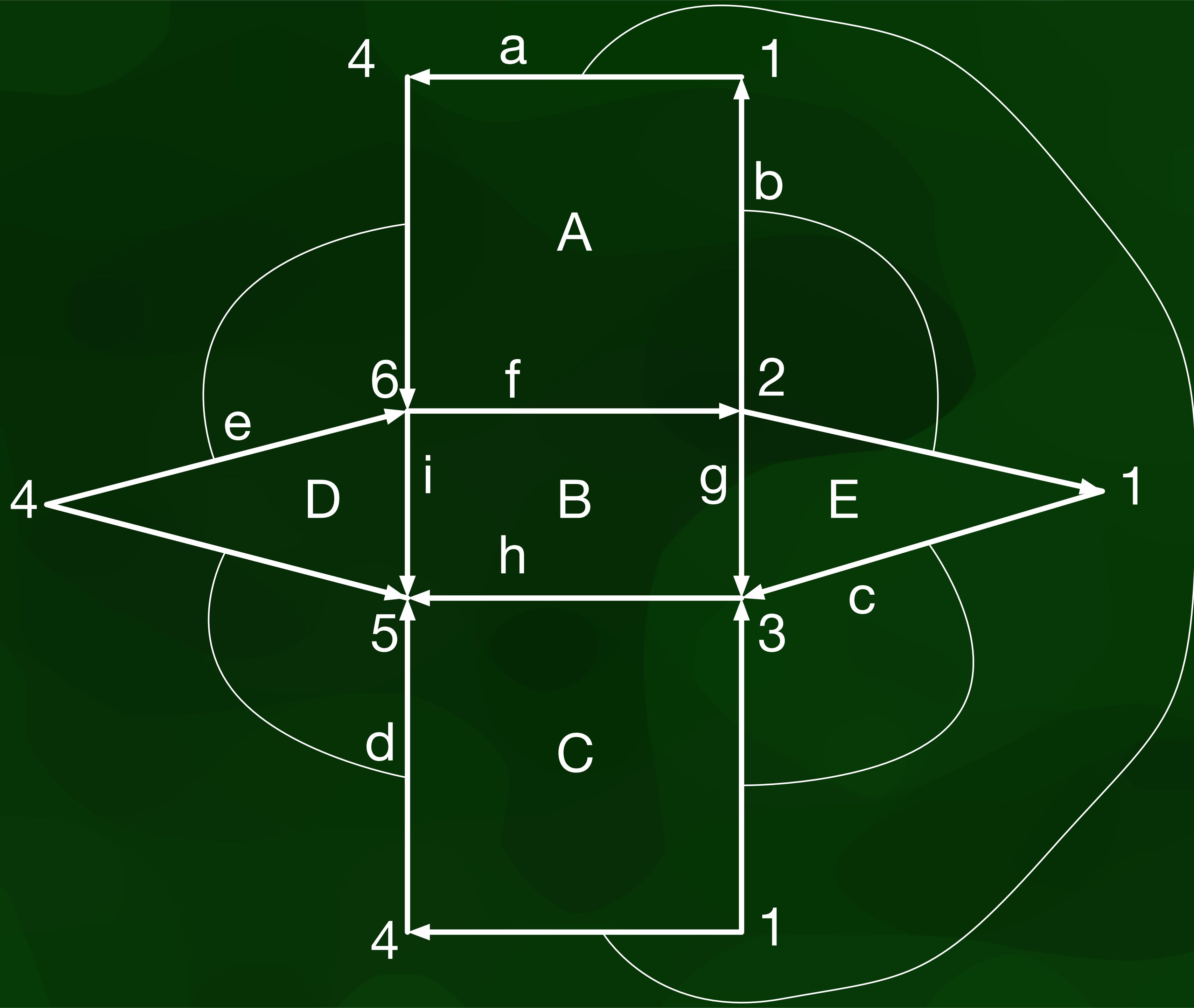


Edge-based structures

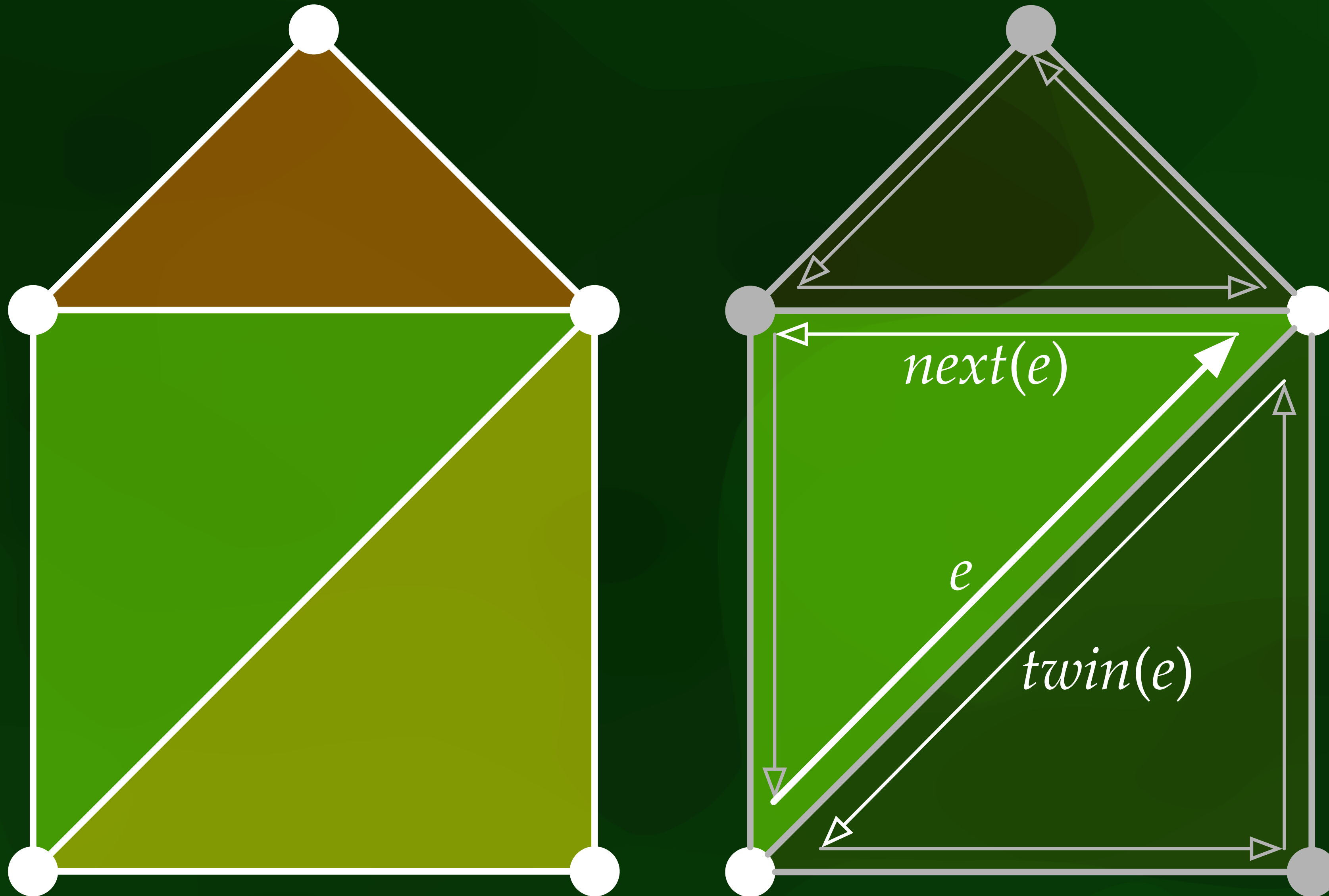
- Essentially two types:
 - Full edges (e.g. winged edge, quad edge)
 - Half-edges (e.g. DCEL, 2D combinatorial maps)

Edge-based structures



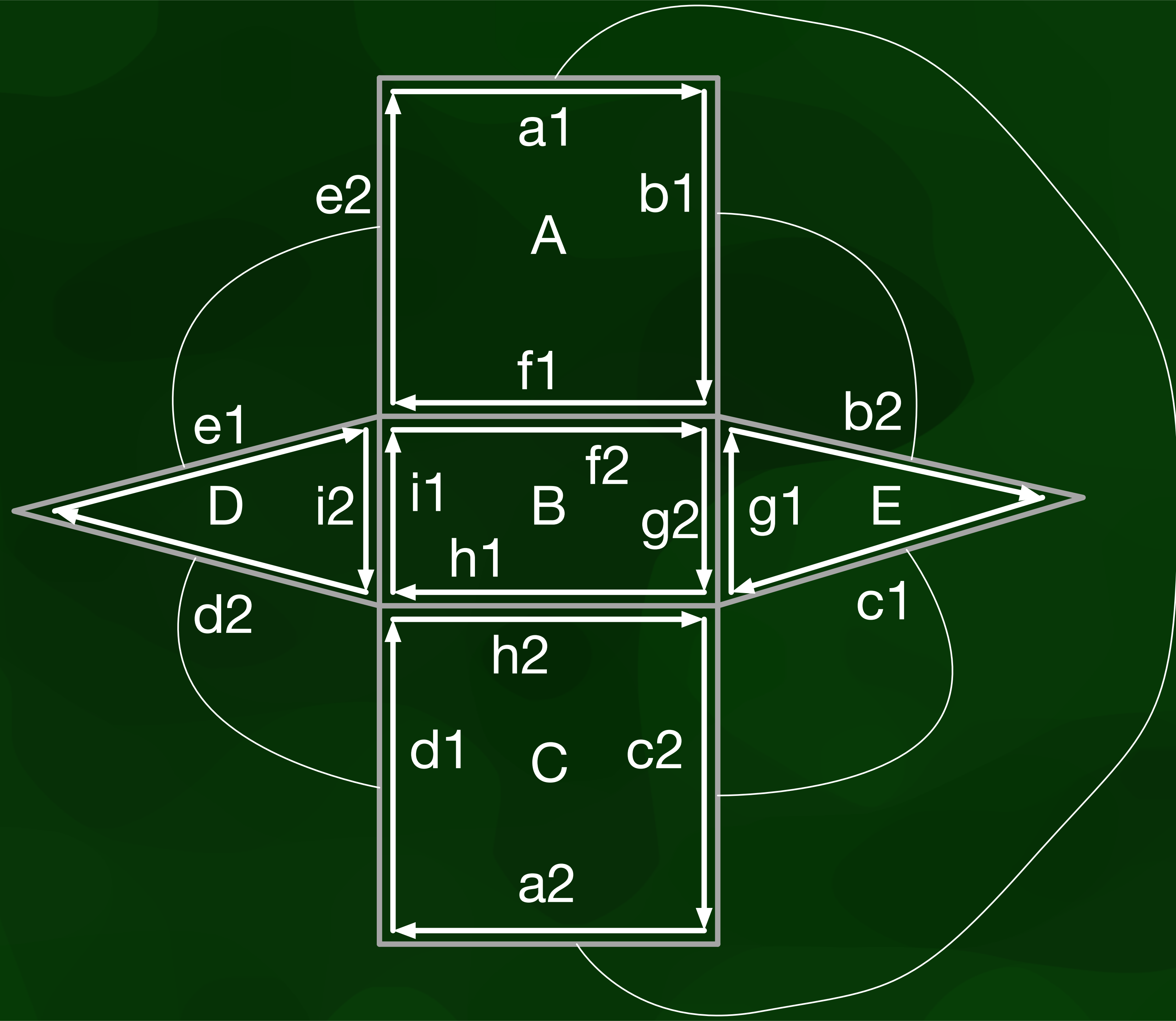


Edge-based structures



Example from CGAL

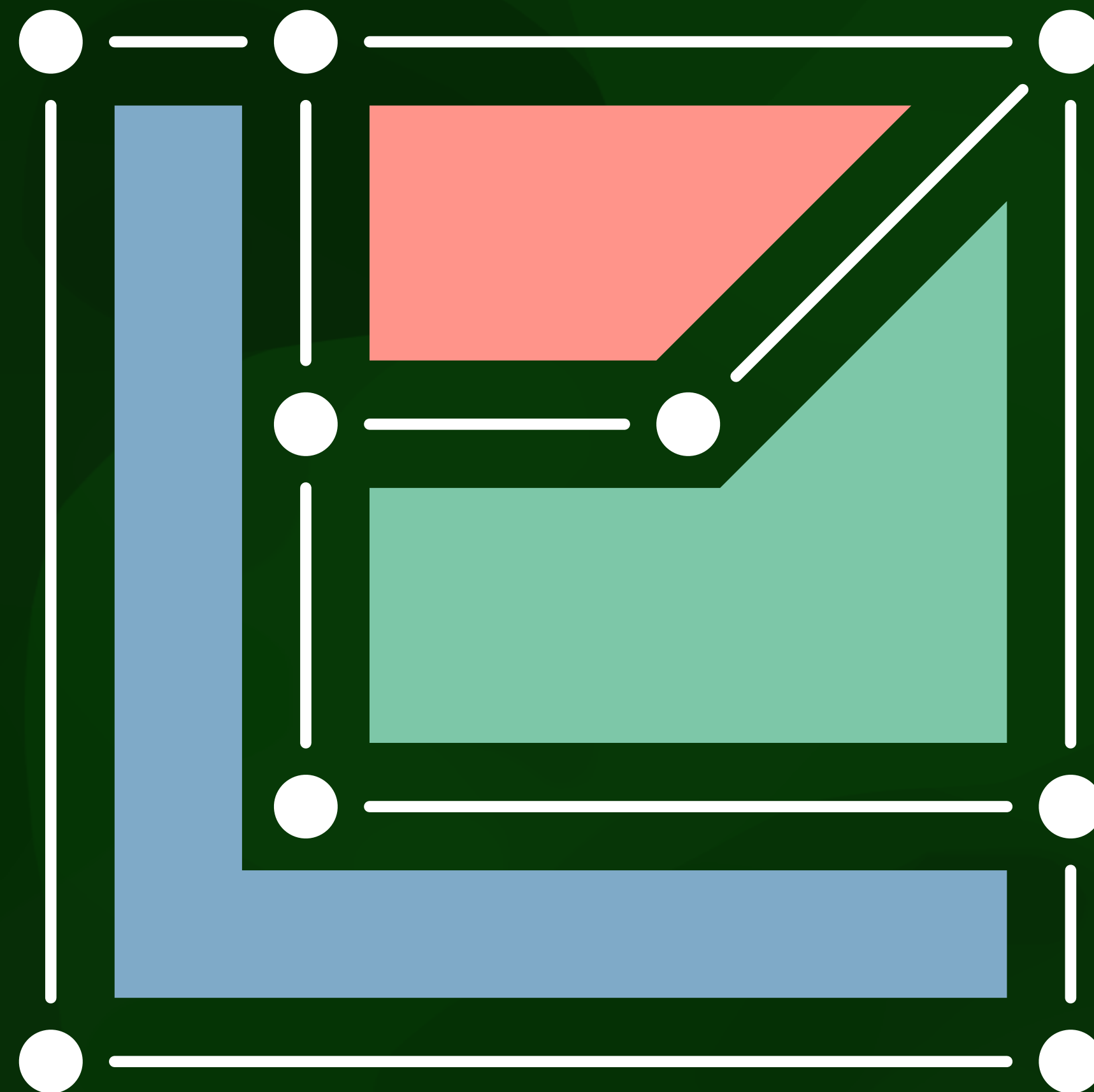
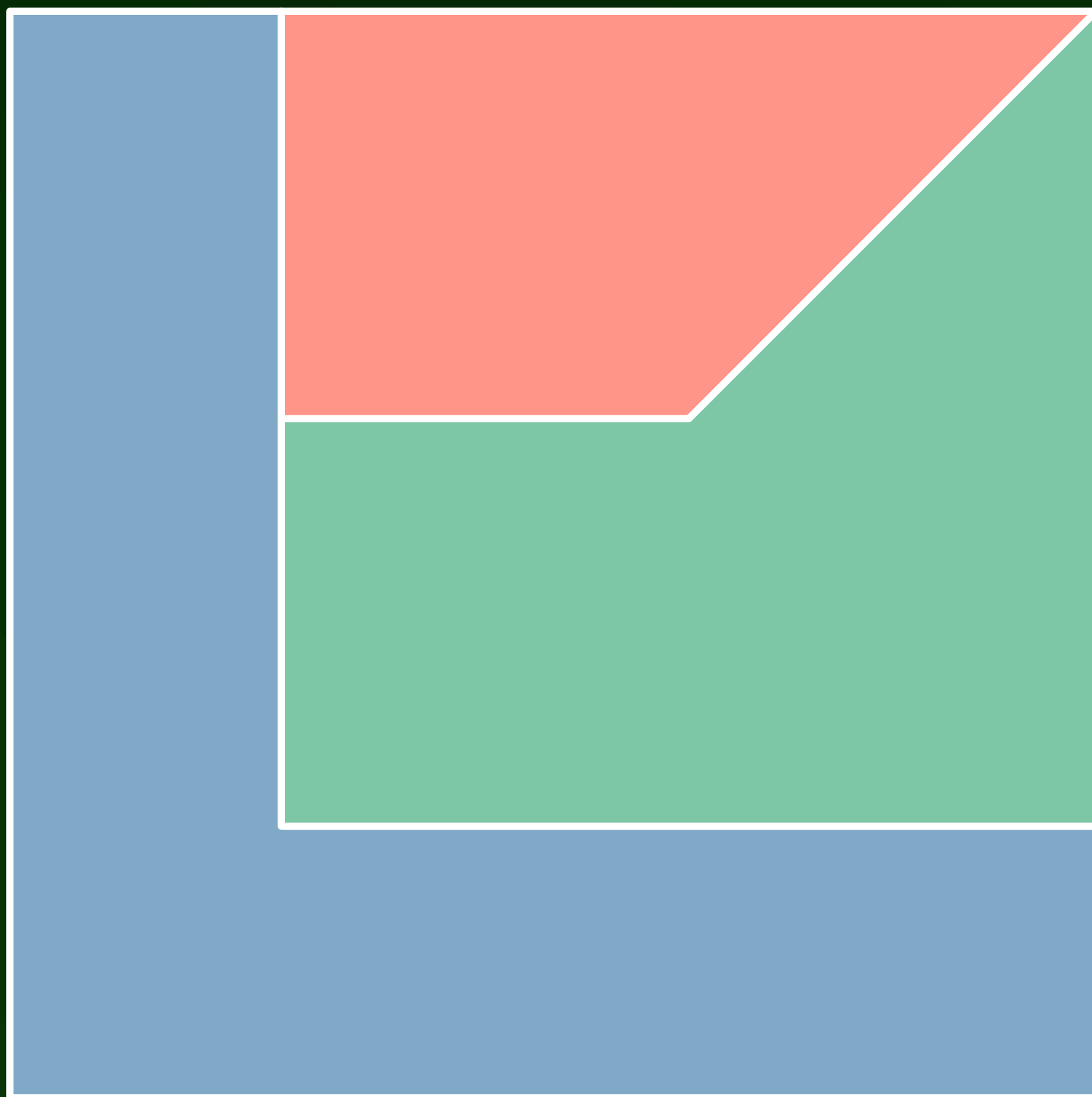
<https://doc.cgal.org/latest/HalfedgeDS/index.html>



Incidence graphs

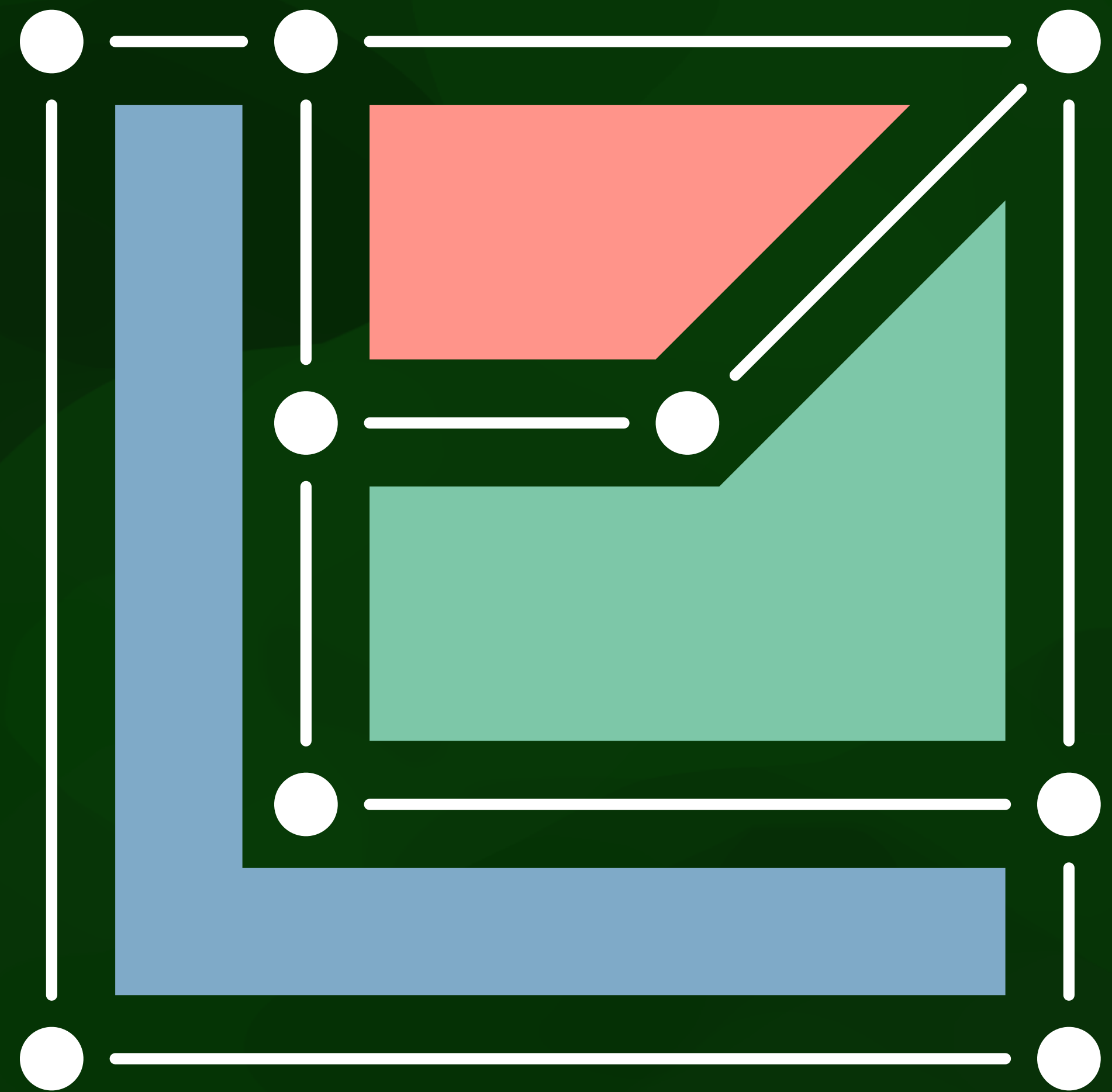
- Adjacency/incidence? neighbouring objects
 - Adjacency: same dimension
 - Incidence: different dimension

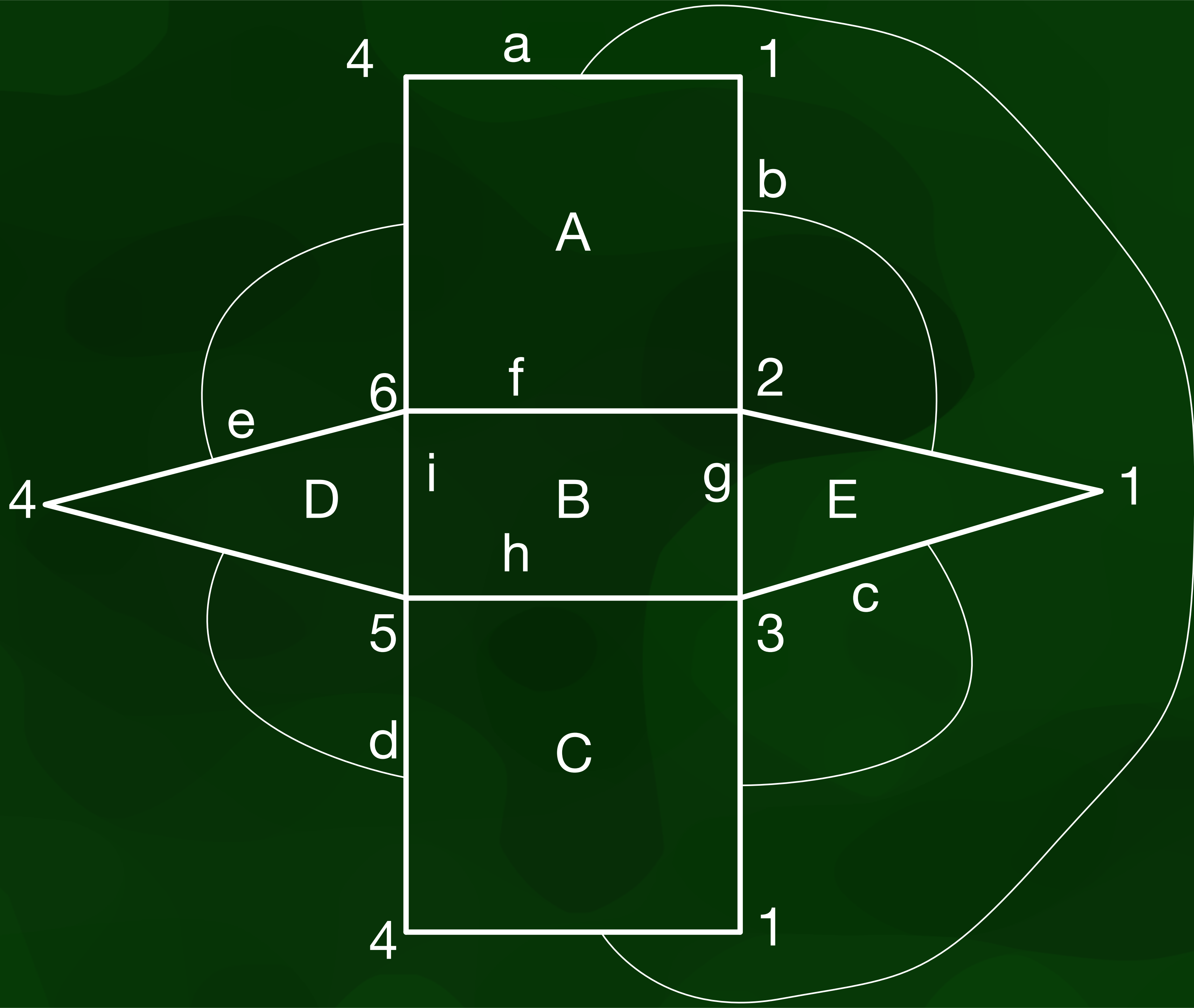
Incidence graphs



Incidence graphs

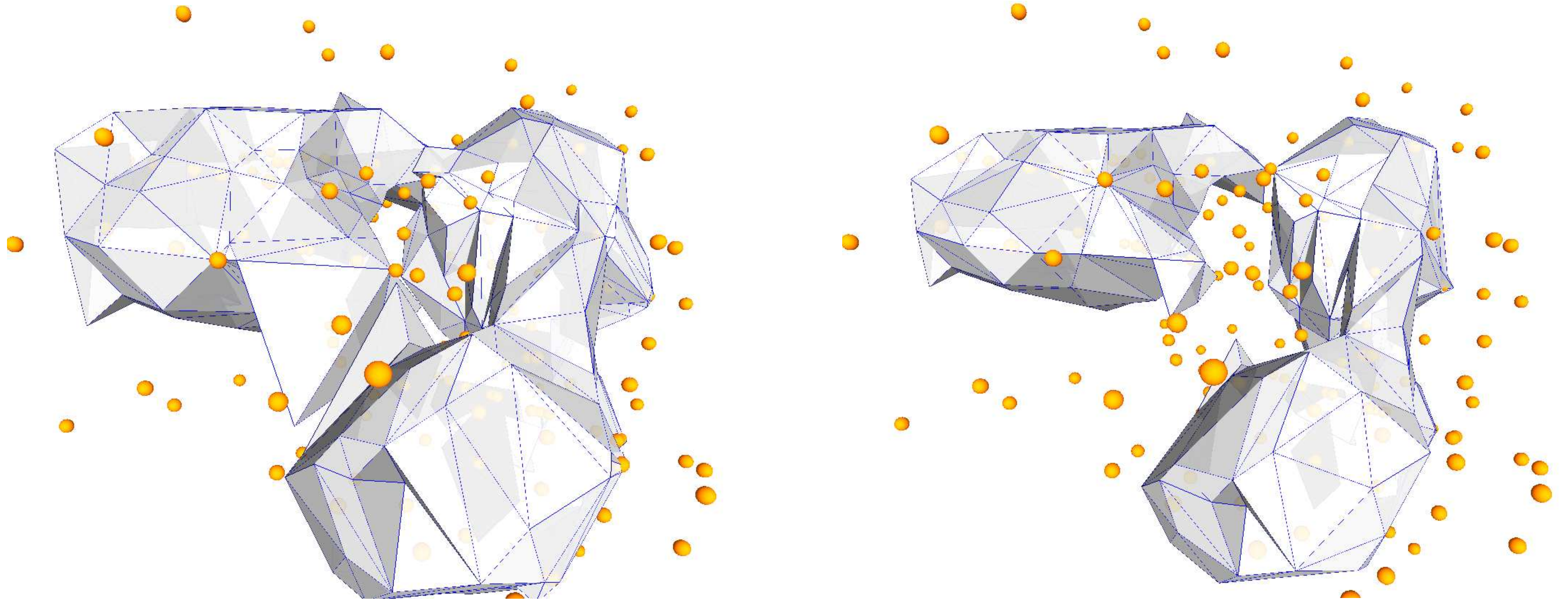
- Two edges are adjacent if they share an incident vertex
- Two faces are adjacent if they share an incident edge
- Less common but also:
 - Two vertices are adjacent if they share an incident edge
 - Two edges are adjacent if they share an incident face





B-rep in fields: isosurfaces

- Not boundary of object -> boundary of level set



Homework 1 intro

What to do next?

1. Today:
 - Go to geo1004 website and study today's lesson (3D book Chapter 2)
 - Get started with Homework 1
2. Friday: help session in A+BE Hall U
3. Next **Wednesday**: 3D Voronoi demos, then help with lessons or Hw 1

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