

Lesson dtvd3d: some extras

GEO1004: 3D modelling of the built environment

[https://3d.bk.tudelft.nl/courses/
geo1004](https://3d.bk.tudelft.nl/courses/geo1004)



3D geoinformation

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Incremental construction

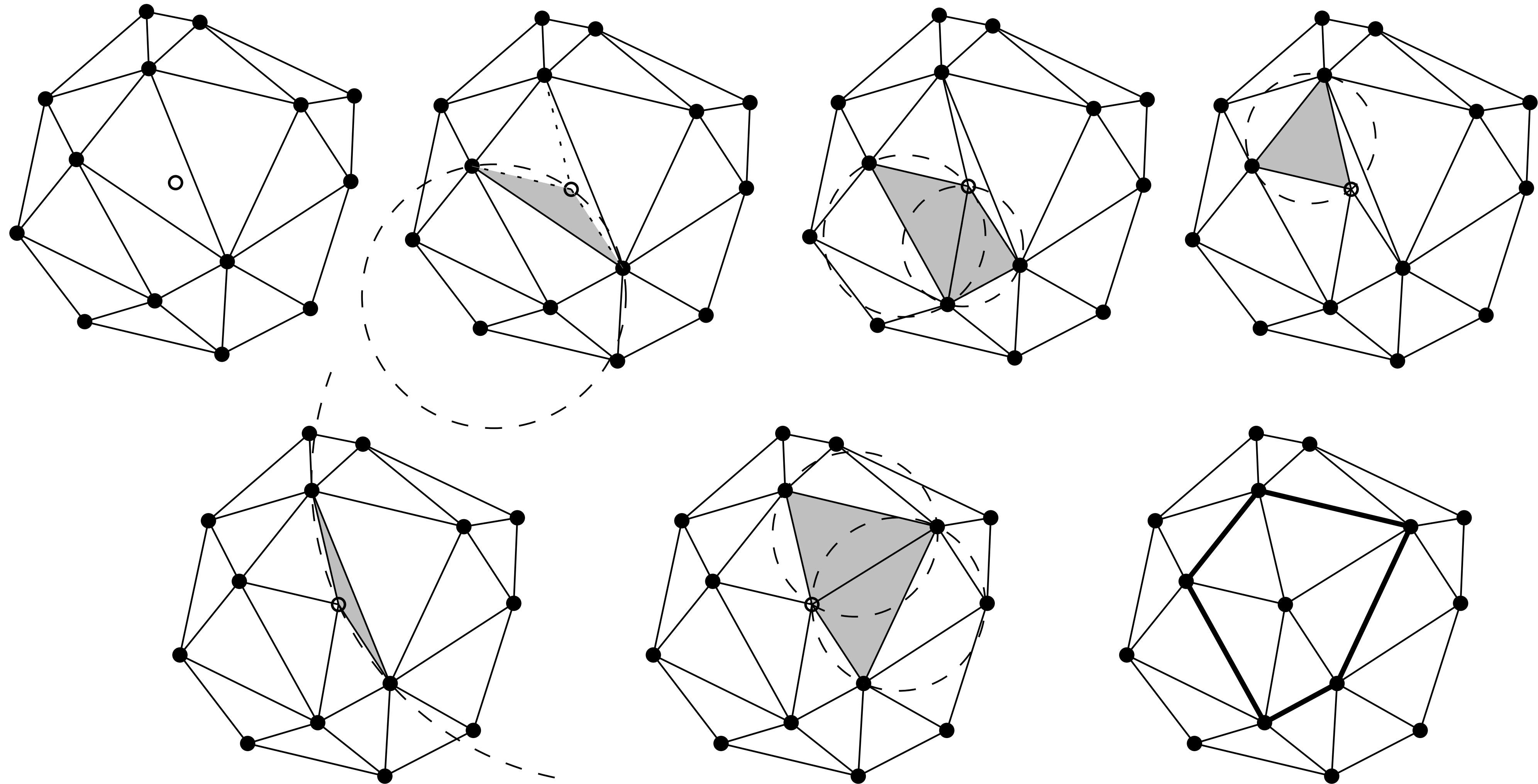


Figure 7: Step-by-step insertion, with flips, of a single point in a DT in two dimensions.

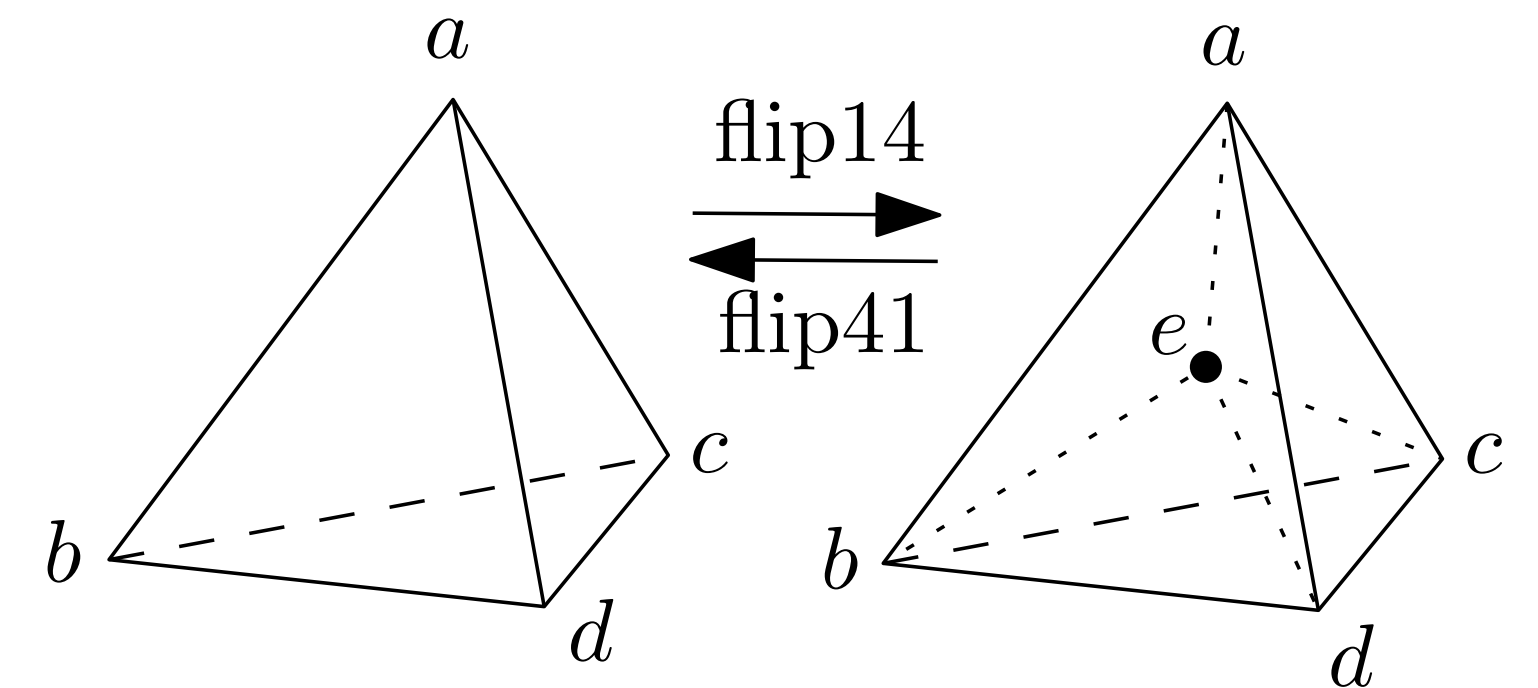
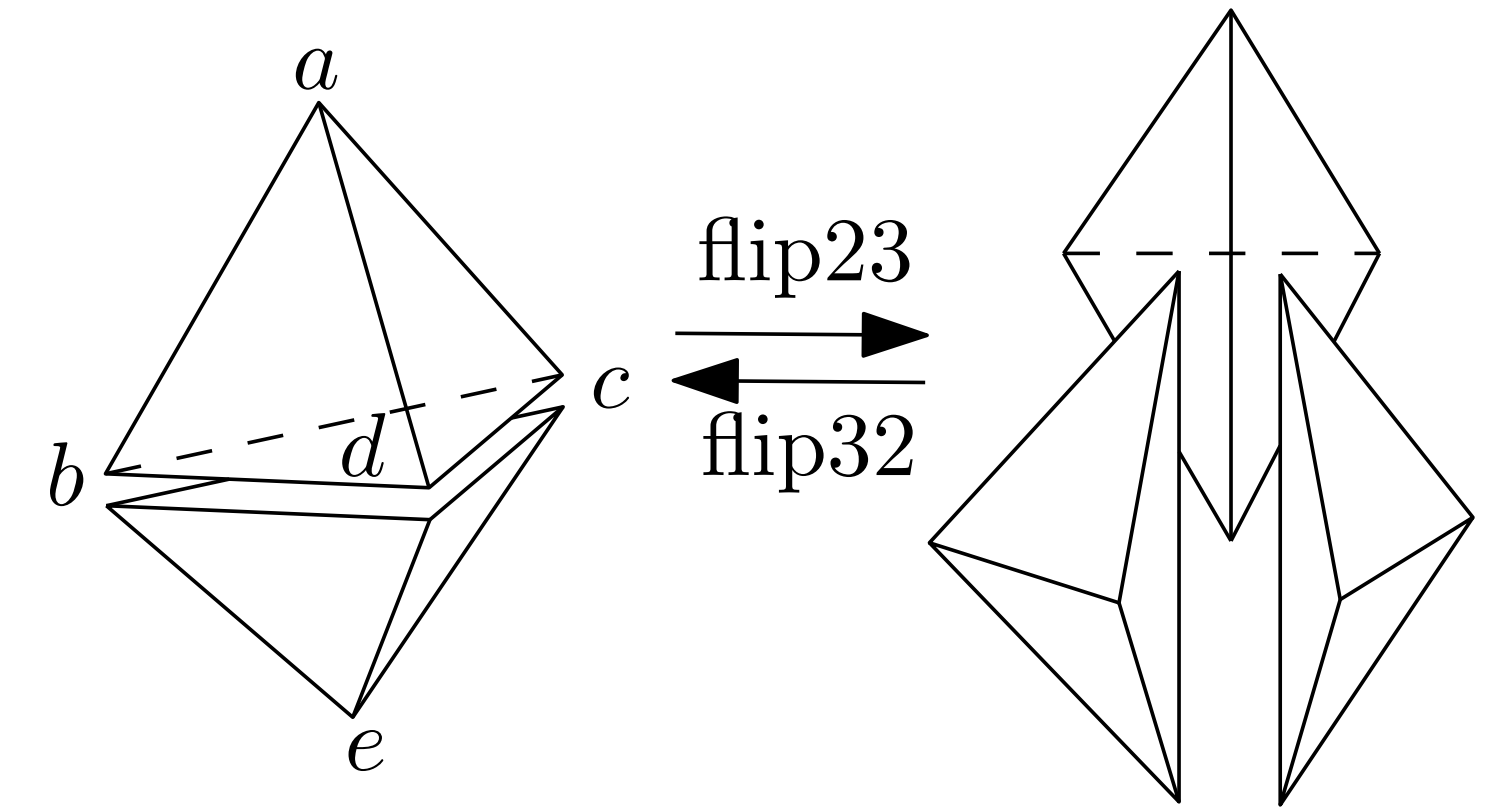
Incrementation construction

Algorithm 1: Algorithm to insert one point in a DT

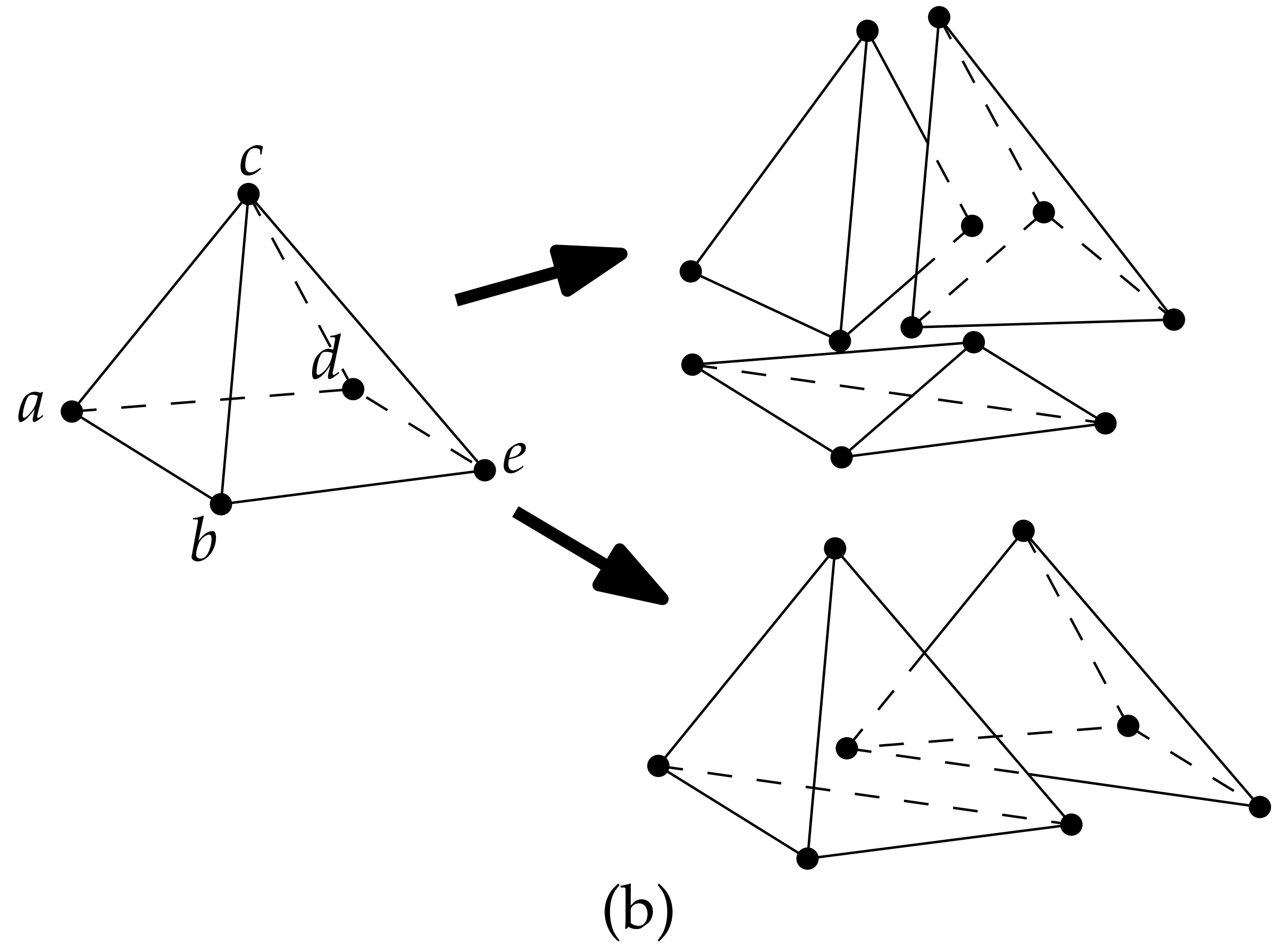
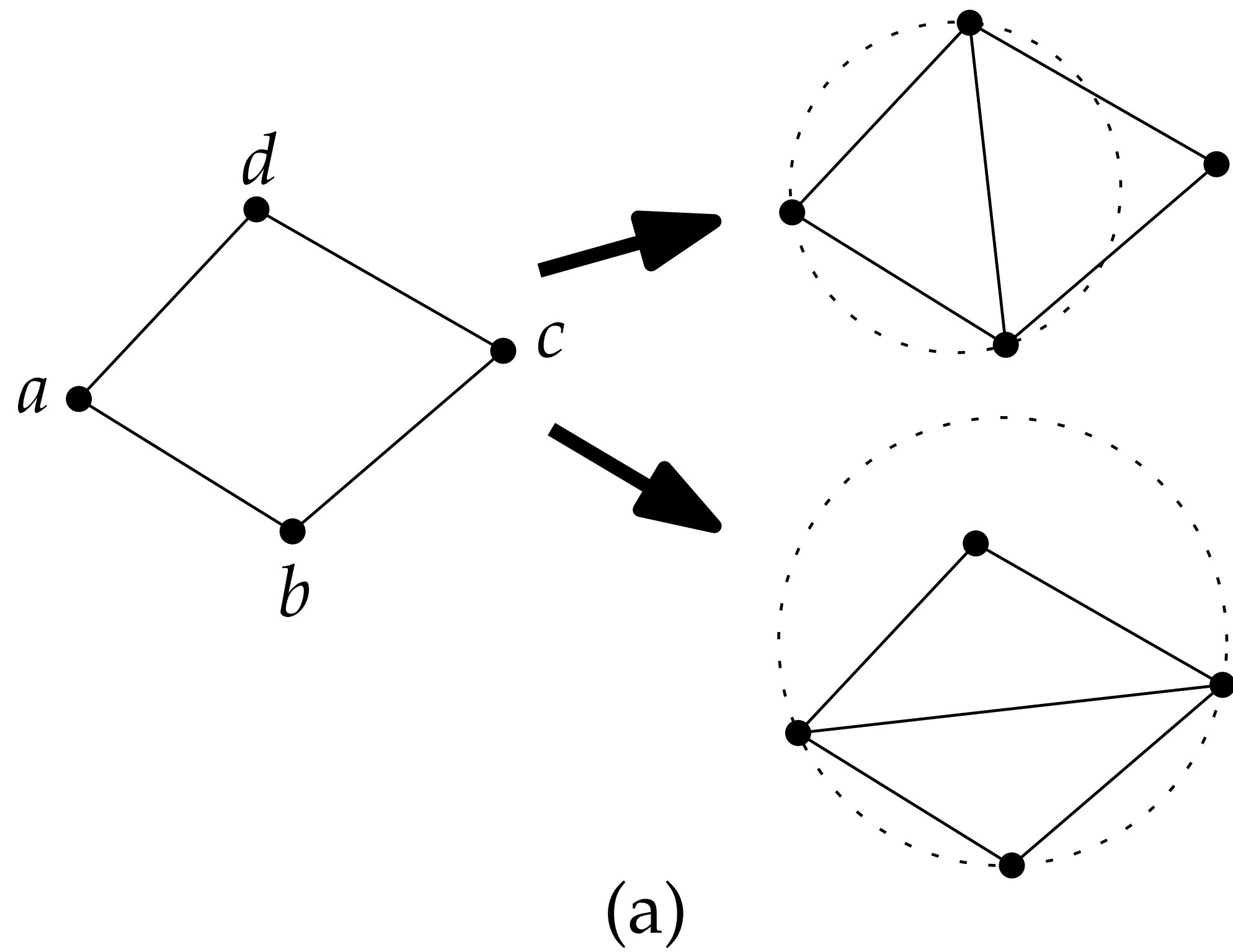
Input: A DT(S) \mathcal{T} in \mathbb{R}^3 , and a new point p to insert

Output: $\mathcal{T}^p = \mathcal{T} \cup \{p\}$

- 1 find tetrahedron τ containing p
 - 2 insert p in τ by splitting it in to 4 new tetrahedra (flip14)
 - 3 push 4 new tetrahedra on a stack
 - 4 **while** stack is non-empty **do**
 - 5 $\tau = \{p, a, b, c\} \leftarrow$ pop from stack
 - 6 $\tau_a = \{a, b, c, d\} \leftarrow$ get adjacent tetrahedron of τ having the edge abc as a face
 - 7 **if** d is inside circumsphere of τ **then**
 - 8 **if** configuration of τ and τ_a allows it **then**
 - 9 flip the tetrahedra τ and τ_a (flip23 or flip32)
 - 10 push 2 or 3 new tetrahedra on stack
 - 11 **else**
 - 12
 - Do nothing
-



Slivers in DT



3D DT \equiv 4D convex hull

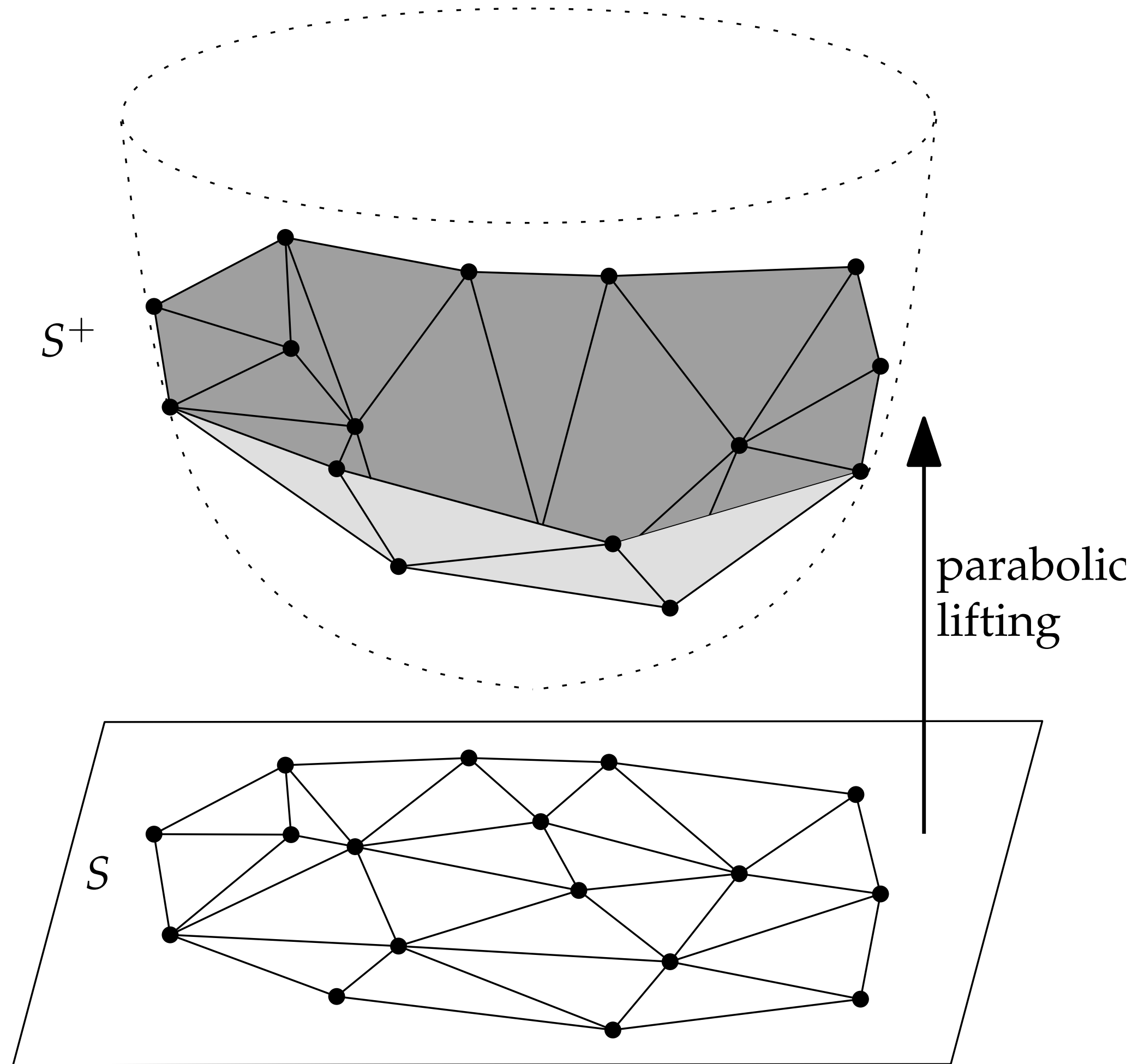
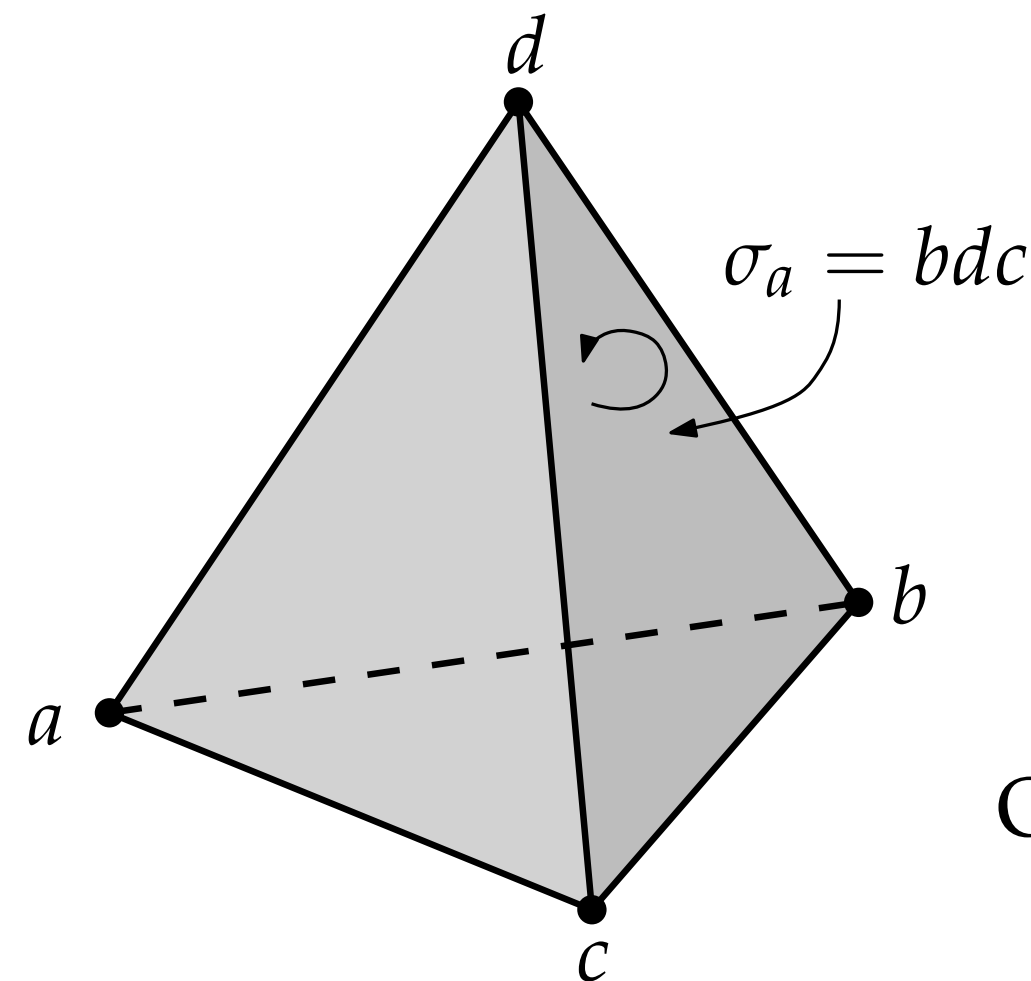


Figure 6: The parabolic lifting map for a set S of points \mathbb{R}^2 .

3D == no “fixed” orientation

3.3.2 Predicates

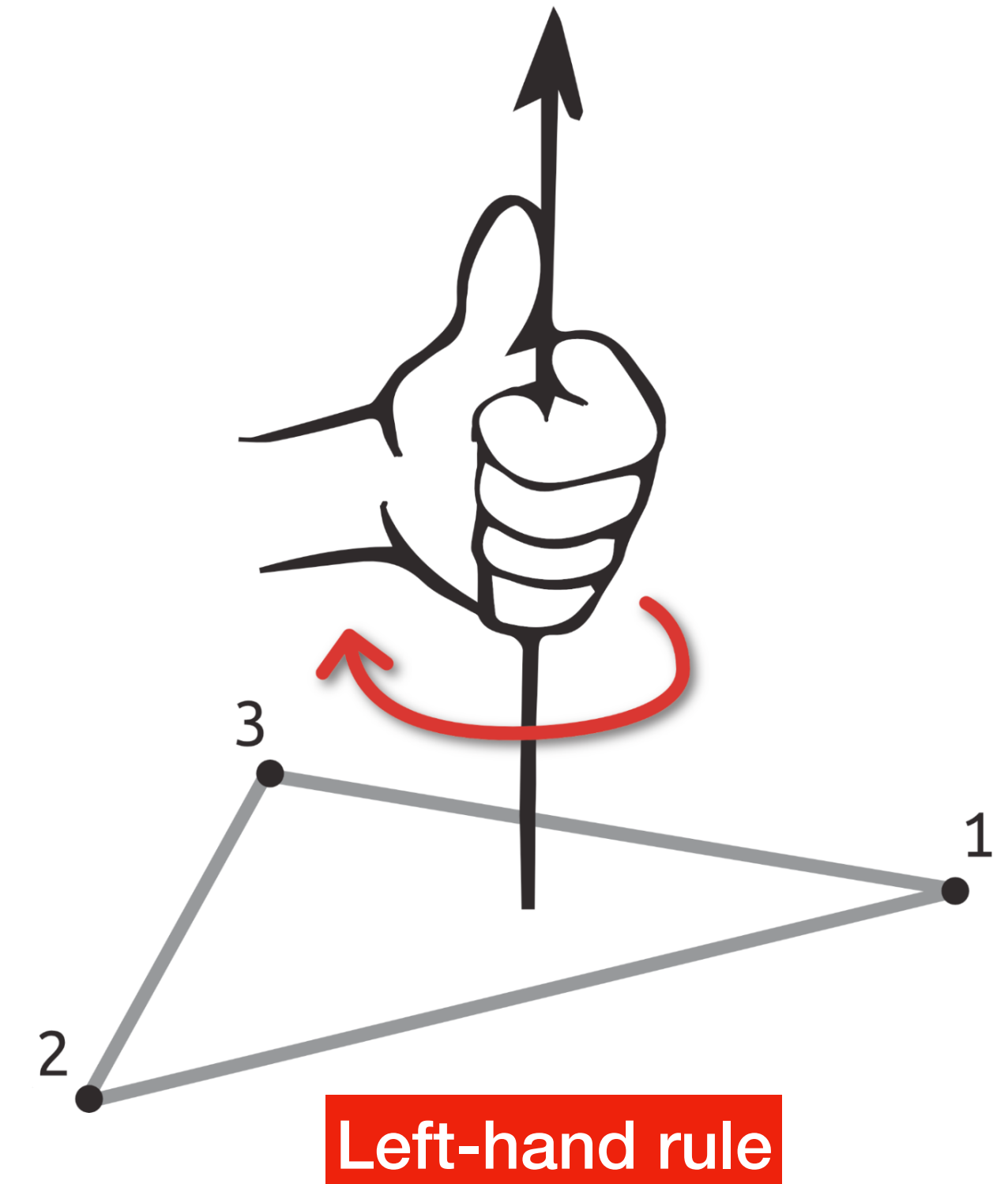
The ‘orientation’ of points in three dimensions is somewhat tricky because, unlike in two dimensions, we can not simply rely on the counter-clockwise orientation. In three dimensions, the orientation is always relative to another point of reference, ie given three points we cannot say if a fourth one is left of right, this depends on the orientation of the three points.



ORIENT can be implemented as the determinant of a matrix:

$$\text{ORIENT}(a, b, c, p) = \begin{vmatrix} a_x & a_y & a_z & 1 \\ b_x & b_y & b_z & 1 \\ c_x & c_y & c_z & 1 \\ p_x & p_y & p_z & 1 \end{vmatrix} \quad (3.2)$$

Figure 3.13: The tetrahedron $abcd$ is correctly oriented since $\text{ORIENT}(a, b, c, d)$ returns a positive result. The arrow indicates the correct orientation for the face σ_a , so that $\text{ORIENT}(\sigma_a, a)$ returns a positive result.



Duality $VD \leftrightarrow DT$ in 3D

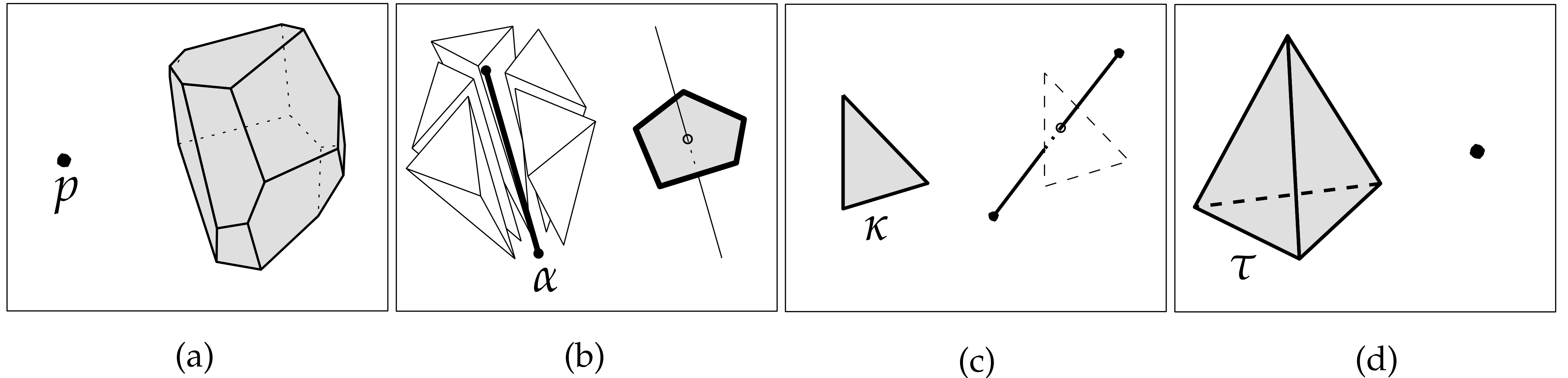


Figure 3: Duality in \mathbb{R}^3 between the elements of the VD and the DT.

App#1: 3DVD as alternative to voxels

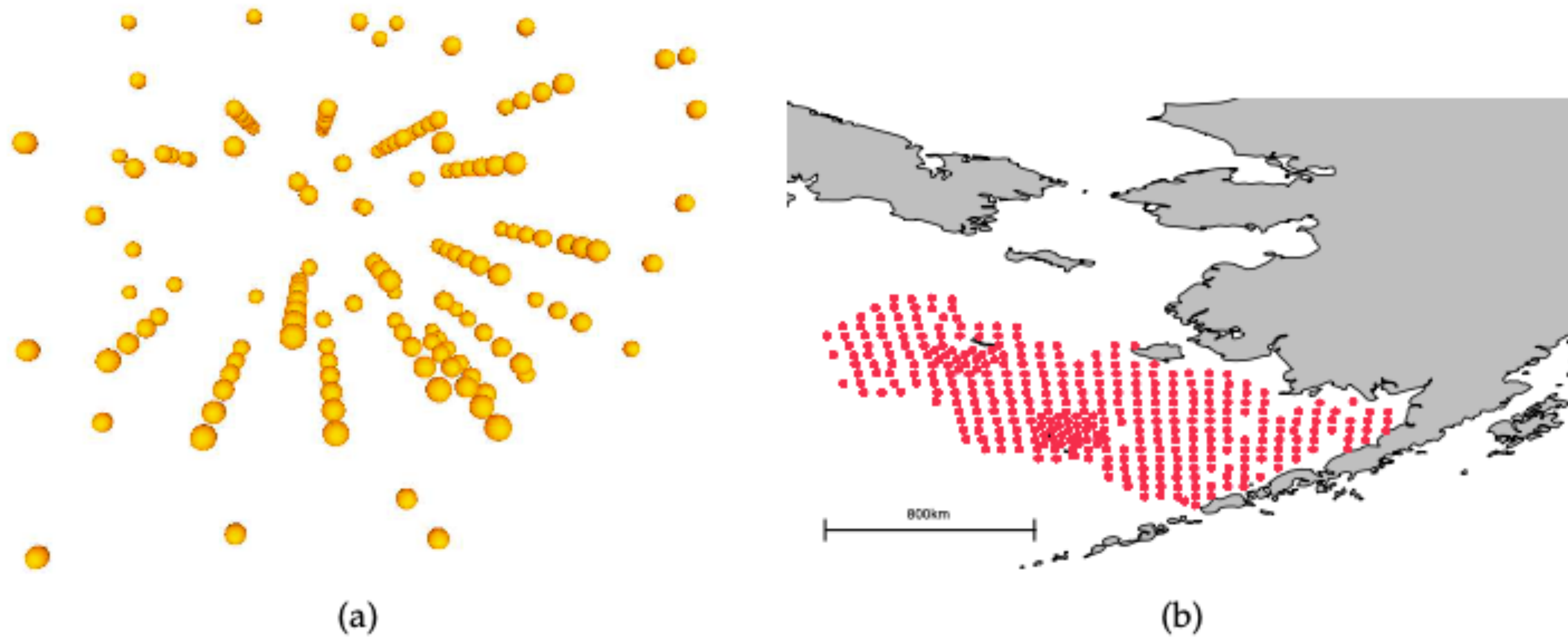


Figure 10: **(a)** Example of a dataset in geology, where samples were collected by drilling a hole in the ground. Each sample has a location in 3D space ($x - y - z$ coordinates) and one or more attributes attached to it. **(b)** An oceanographic dataset in the Bering Sea in which samples are distributed along water columns. Each red point represents a (vertical) water column, where samples are collected every 2m, but water columns are about 35km from each other.

App#2: spatial interpolation

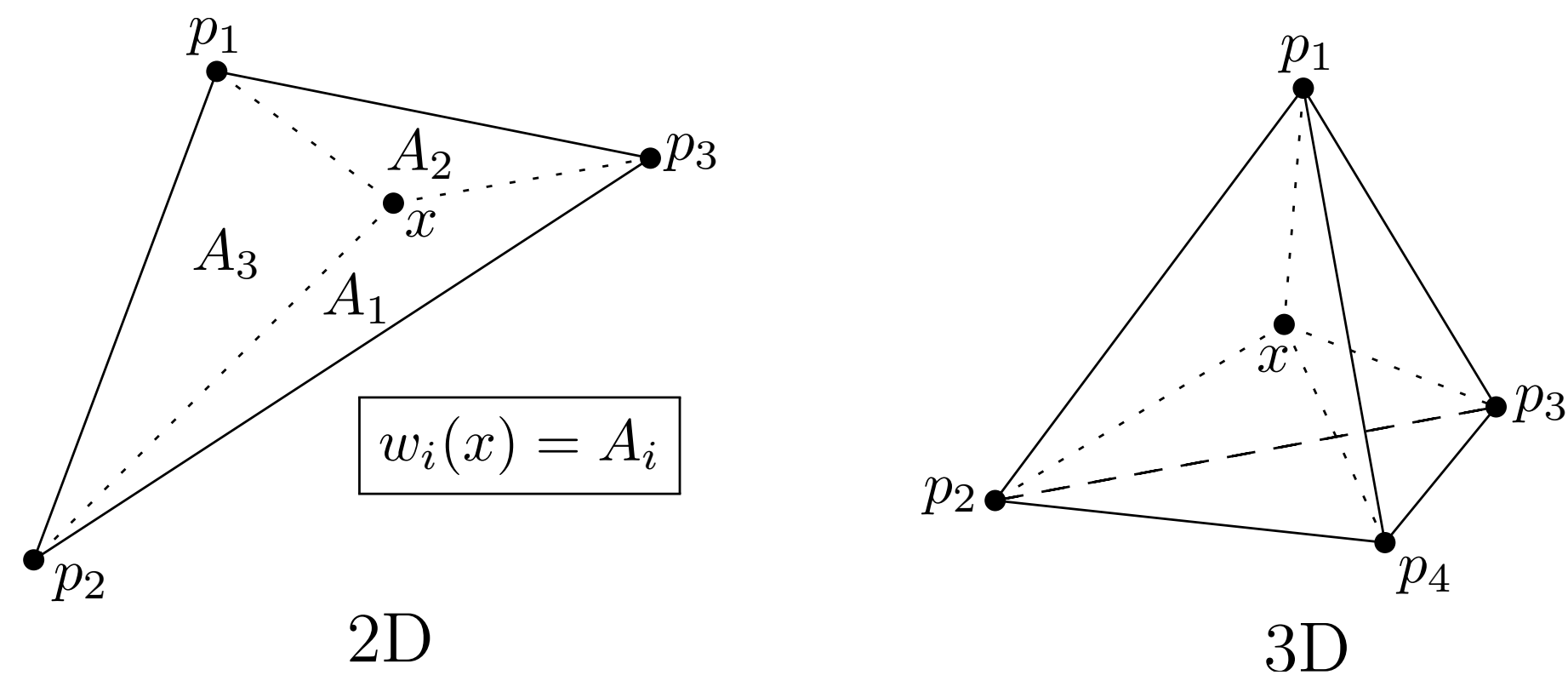


Figure 11: Barycentric coordinates in two and three dimensions. A_i represents the area of the triangle formed by x and one edge.

$$\text{vol}(\sigma) = \frac{1}{d!} \left| \det \begin{pmatrix} v^0 & \dots & v^d \\ 1 & \dots & 1 \end{pmatrix} \right|$$

App#2: spatial interpolation

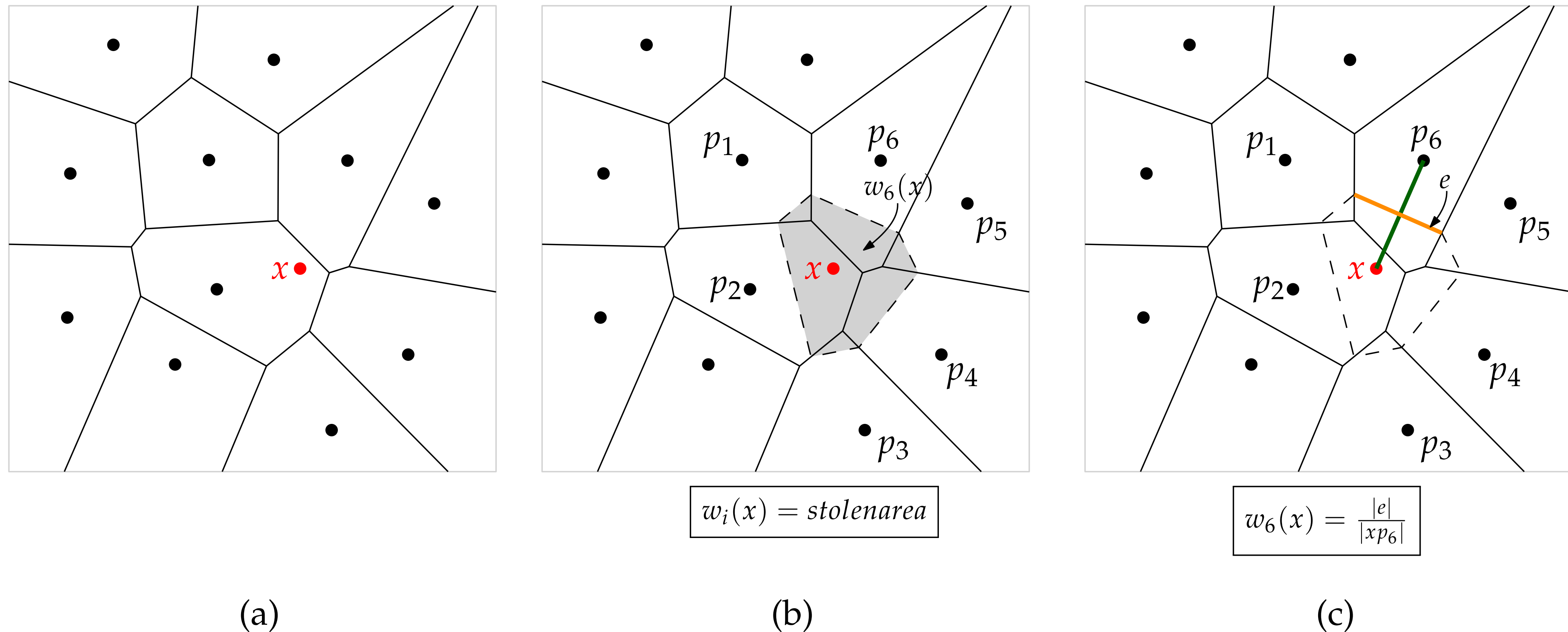


Figure 4.7: (a) The VD of a set of points with an interpolation location x . (b) Natural neighbour coordinates in 2D for x . The shaded polygon is \mathcal{V}_x^+ . (c) The weight for the Laplace interpolant.

App#3: visualisation with iso-surfaces

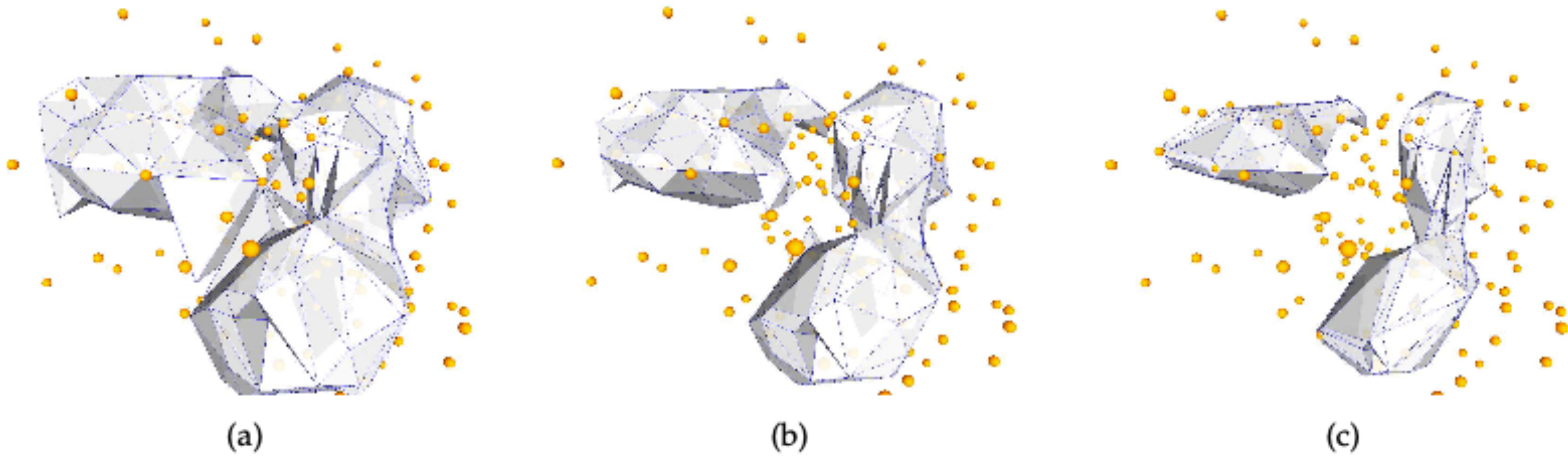
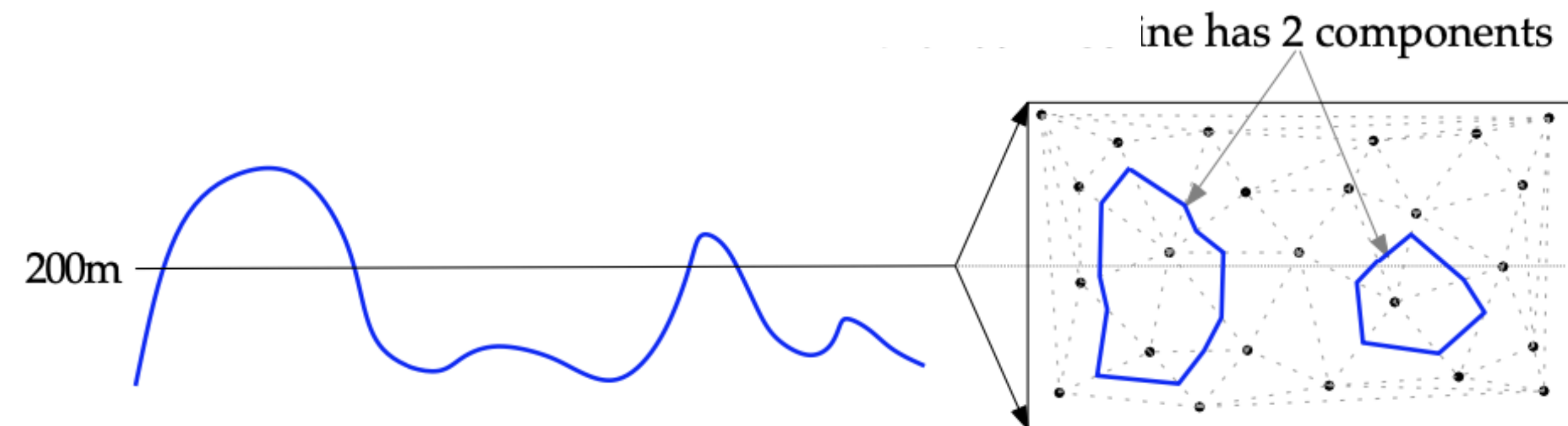
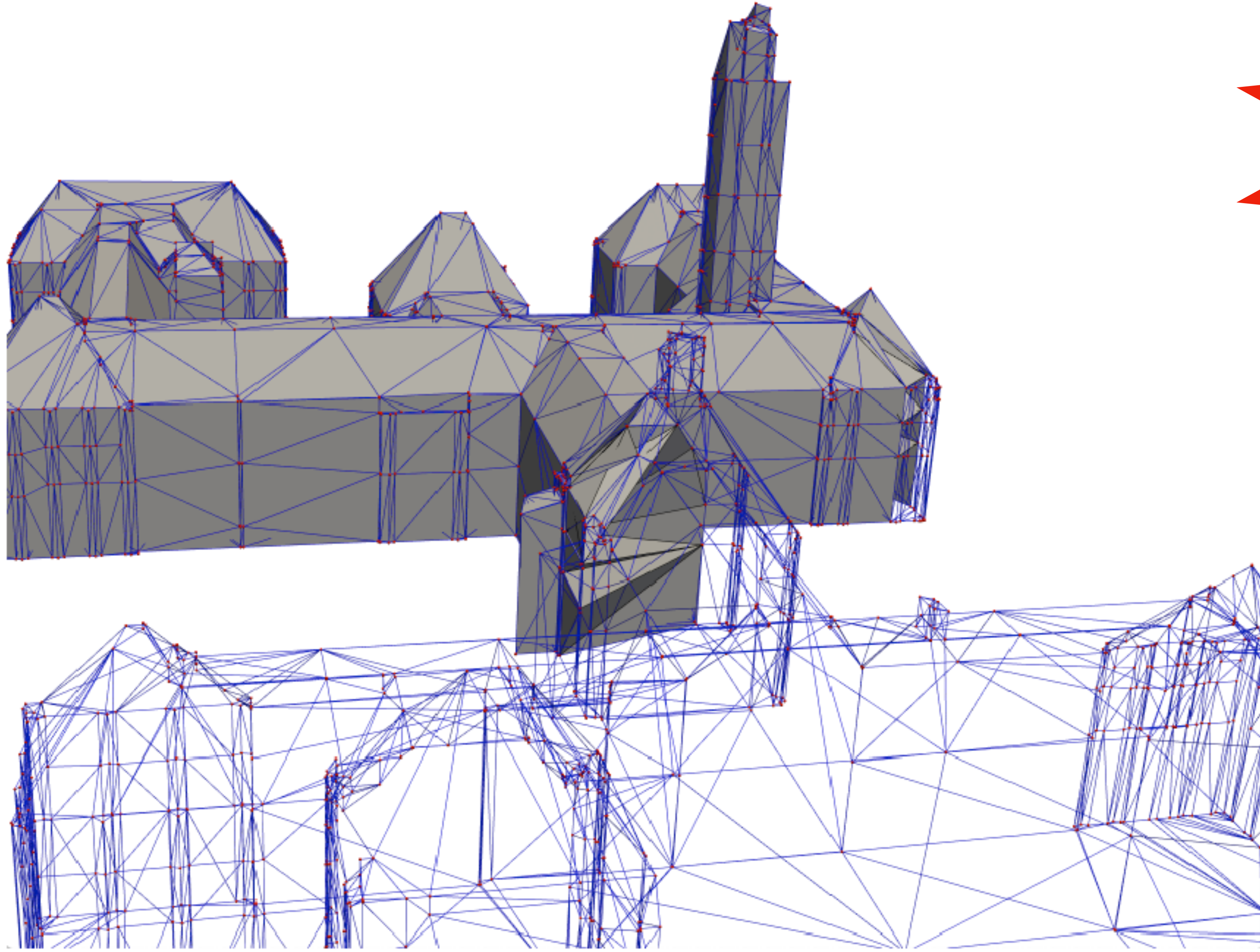


Figure 12: An example of an oceanographic dataset where each point has the temperature of the water, and three isosurface extracted (for a value of respectively 2.0, 2.5 and 3.5) from this dataset.



Triangulating a building (or any 3D model)



Two very different
cases

demo with one building

- MeshLab: <https://www.meshlab.net>
- TetGen: <http://tetgen.org>
- ParaView: <https://www.paraview.org>

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